

# THREE ESSAYS IN LABOUR ECONOMICS AND THE ECONOMICS OF EDUCATION

by

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## Abstract

This thesis consists of three empirical essays. The first chapter is focused on the economics of gender, and the other two chapters are focused on the economics of education. A common theme in all these three chapters is studying the outcomes of disadvantaged groups in society, with an eye to policy interventions that could improve these outcomes.

The first chapter examines whether women face a glass ceiling in the labour market, which would imply that they are under-represented in high wage regions of the wage distribution. I also measure the extent to which the glass ceiling comes about because women are segregated into lower-paying firms (glass doors), or because they are segregated into lower-paying jobs within firms (within-firm glass ceilings). I find clear evidence that women experience a glass ceiling that is driven mainly by their disproportionate sorting across firm types rather than sorting across jobs within firms. I find no evidence that gender differences in sorting across firms can be accounted for by compensating differentials. However, my results are consistent with predictions of an efficiency wage model where high-paying firms discriminate against females.

The second chapter estimates the effect of publicly-disseminated information about school achievement on school choice decisions. We find that students are more likely to leave their school when public information reveals poor school-level performance. Some parents' respond to information soon after it becomes available. Others, including non-English-speaking parents, alter their school choice decisions only in response to information that has been disseminated widely and discussed in the media. Parents in low-income neighbourhoods are most likely to alter their school choice decisions in response to new information.

The third chapter measures the extent to which cross-sectional differences in schools' average achievement on standardized tests are due to transitory factors. Test-based measures of school performance are increasingly used to shape education policy, and recent evidence shows that they also affect families' school choice decisions. There are, however, concerns about the precision of these measures. My results suggest that

sampling variation and one-time mean reverting shocks are a significant source of cross-sectional variation in schools' mean test scores.

**Keywords:** Gender Wage Gap; Glass Ceiling; Inter-Firm Gender Segregation; Test-Based School Achievement Measures; School Choice; Transitory Factors

## Dedication

*To my patient wife, Shabnam, for her love and  
support every step of the way.*

*And to my lovely parents, Hamid and Laleh,  
for their encouragement and support.*

*I love you.*



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# 1. Glass Ceilings or Glass Doors? The Role of Firms in Gender Wage Disparities

## 1.1. Introduction

As in many countries, women earn lower wages than men in Canada. Despite modest improvement in the late 1980s, this gap has been largely unchanged since 1992 (Baker and Drolet, 2009). Designing effective policies to improve women's labor market outcomes requires knowledge about the mechanisms that underlie this persistent gender wage gap. Previous studies of the gender wage gap have mainly focused on gender differences in conditional mean wages. While this comparison is interesting, it is only indicative of the wage outcomes of "average" workers in each group. More recently, there has been a growing interest in examining the gender wage gap throughout the wage distribution. This has been mainly motivated by a popular notion that females face a "glass ceiling" in the labor market; that is, females are over-represented (under-represented) in low (high) wage regions of the wage distribution, and their under-representation becomes more pronounced as we move to the top of the wage distribution. As a consequence, the gap between male and female wages will be larger at the top of the wage distribution than at the middle or bottom.

Developing policies that effectively address potential barriers that block the advancement of women in the labor market requires knowledge about the magnitude of any glass ceiling, and about the underlying mechanisms that give rise to it. For instance, if the glass ceiling is driven by barriers to employment at "high-paying firms", then policies like employment equity policies that target employment decisions directly will be more effective. On the other hand, if the glass ceiling is driven by gender wage disparities within firms, then policies like pay equity policies that target wages directly will be more effective.

This study uses quantile regression methods to estimate the gender wage gap at different points of the conditional wage distribution in order to examine whether females in Canada face a glass ceiling. I extend the previous empirical literature on glass ceilings faced by women by applying a methodology developed by Pendakur and Woodcock (2010) in the context of native-immigrant wage disparities. I quantify the extent to which the observed economy-wide glass ceiling is driven by female segregation into low-paying firms (defined as a “glass door” effect) versus female segregation into low-paying jobs within firms (defined as a within-firm glass ceiling effect).

Focusing on gender wage gaps at various quantiles is only partly informative of women’s representation at high-paying and low-paying jobs, which might be of direct policy importance. Therefore, following Pendakur et al. (2008), I also construct a measure of female workers’ representation at high-paying and low-paying jobs. This “representation index” measures the proportion of female workers in different regions of the wage distribution, especially the tails, conditional on their personal and job characteristics. I extend their methodology by estimating the extent to which these patterns of over-representation and under-representation are driven by gender segregation across high-paying and low-paying firms.

Finally, I investigate some of the potential underlying sources of inter-firm wage differentials and inter-firm sex segregation. I empirically test the implications of two competing theoretical models, the compensating differentials model and the efficiency wage model with gender discrimination. The results help to illuminate some of the underlying mechanisms that generate the observed difference in male-female sorting across high-paying and low-paying firms.

I find clear evidence that females face an economy-wide glass ceiling: the gender wage gap increases from -0.12 log points at the 10<sup>th</sup> percentile of the conditional wage distribution to -0.20 log points at the 90<sup>th</sup> percentile. I find strong evidence that the economy-wide glass ceiling is mainly driven by glass doors. Three quarters of the increase in the gender wage gap between the 10<sup>th</sup> and 90<sup>th</sup> percentile of the conditional wage distribution is due to differential sorting of males and females across high- and low-paying firms (glass doors). I find no evidence that inter-firm wage differences, and



inter-firm gender differences in sorting, can be accounted for by compensating differentials. However, my results are consistent with predictions of an efficiency wage model where high-paying firms discriminate against females. My results also suggest that after controlling for observables and inter-firm sorting, females still experience a sizeable within-firm wage gap (about 11 percent) throughout the wage distribution.

## 1.2. Previous Literature

Beginning with the seminal contribution of Albrecht et al. (2003), there has been a growing interest in how the gender wage gap varies throughout the wage distribution. In contrast with most of the previous studies that compare gender differences in average wages, this approach informs us about places in the wage distribution where these wage gaps appear, and are more pronounced.<sup>1</sup> This recent literature generally finds larger gender wage gaps at the top of the wage distribution than in lower parts of the wage distribution, even after controlling for observable person, job and firm characteristics (Garfeazabal and Ugidos 2005; Nordman and Wolff 2007; Datta Gupta et al. 2006; Arulampalam et al. 2007; de la Rica et al. 2008 ; Jellal et al. 2008). These results, all of which are obtained using data from European labor markets, are consistent with what is referred to as a *glass ceiling* effect. It is of substantial interest to learn whether wage patterns are similar in Canada, where government policies, wage-setting institutions, women's relative market qualifications and the wage structure differ in important ways from European environments.

The economy-wide glass ceilings found by these studies could stem from the fact that females face glass ceilings within firms. However, as suggested by Dickens and Katz (1987), Groshen (1990 and 1991a), Bronars and Famulari (1997), Wooden (1998),

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<sup>1</sup> For instance, any observed gender differences in average wages could be driven by large wage gaps faced by females at the top of the wage distribution, or at the bottom of the wage distribution, or a uniform wage gap faced by females throughout the wage distribution. These different wage patterns have different implications and require different remedies.

Salvanes et al. (1998), Abowd, Kramarz and Margolis (1999), and Woodcock (2007), inter-firm wage differentials explain a large portion of variation in individuals' wages. Therefore, an alternative explanation for the observed economy-wide glass ceiling experienced by females is disproportionate sorting of men and women across high-paying versus low-paying firms (the glass door effect). Similar to the glass ceiling effect that truncates the distribution of wages for female workers, the glass door effect may truncate the distribution of firms at which female workers might find employment. No previous studies of the glass ceiling faced by females distinguish between within-firm versus economy-wide wage outcomes, and the extent to which the glass ceiling faced by females operates between firms versus within firms.

A separate literature focuses on inter-firm sex segregation and its effect on the average gender wage gap. Early studies of inter-firm sex segregation use specialized samples that are not representative of the national economy and cover only a narrow range of industries, occupations or regions. They found that women are typically segregated into lower-paying firms, even within occupations, and this inter-firm sex segregation accounts for a considerable portion of the average gender wage gap (McNulty 1967; Buckley 1971; Blau 1977; Pfeffer and Davis-Blake 1987; Groshen 1991b; Reilly and Wirjanto 1999; Carrington and Troske 1995; Griffin and Trejo 1995, 1997 and 1998). More recent studies (Milgrom *et al.* 2001; Bayard *et al.* 2003; Gupta and Rothstein 2005; Amuedo-Dorantes and De la Rica 2006) use nationally representative matched employer-employee data sets to quantify the contribution of sex segregation by industry, occupation, establishment and occupation-establishment cell (job cell) to the average gender wage gap. All these studies find that segregation of females into lower-paying occupations, industries, establishments and occupations within establishments accounts for a substantial portion of the average gender wage gap. With the exception of Milgrom et al. (2001), they also find that there remains a considerable within-job-cell average gender wage gap even after controlling for observed worker characteristics and accounting for segregation of females into lower-paying occupations, industries, establishments and occupations within establishments.

Pendakur and Woodcock's (2010) methodology, which is developed in the context of native-immigrant wage disparities, has several advantages over methodologies used in other recent studies (Bayard *et al.* 2003; Gupta and Rothstein

2005; Amuedo-Dorantes and De la Rica 2006). First, it provides a way to measure the effect of inter-firm segregation throughout the wage distribution, not only at the mean. Second, it does not rely on estimates of the proportion female in the firm to quantify the effects of inter-firm gender segregation on the gender wage gap.<sup>2</sup> As pointed out by Bayard *et al.* (2003), because only a sample of firm's employees are observed in these data, sampling error in these estimates can be severe. In addition, using the estimates of the proportion of females in each firm to study the inter-firm sex segregation assumes a particular functional form on the way segregation affects wages.

### 1.3. Empirical Methodology

I start by comparing average log wages of males and females, conditional on their observed individual and job characteristics, using the following linear regression model:

$$(1) \quad E[W_i|X_i, g_i] = X_i'\beta + g_i\delta,$$

where  $W_i$  is the log hourly wage of worker  $i$ ;  $X_i$  is a vector of observable job-related characteristics that influence wages (e.g. education, labor market experience, ethnicity, etc.);  $g_i$  is a gender indicator which is equal to one for females; and  $\delta$  measures the difference in average log wages of males and females with the same observed characteristics  $X_i$ .

To assess the existence of an economy-wide glass ceiling experienced by females, I estimate the gender wage gap at several quantiles of the conditional wage distribution. The existence of an economy-wide glass ceiling would imply that females are over-represented (under-represented) in low (high) wage regions of the wage distribution, and their under-representation becomes more pronounced as we move to

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<sup>2</sup> For example, to quantify the effect of inter-firm gender segregation, Bayard *et al.* (2003) use a regression of wages on the estimates of the proportion of females in worker's firm, as well as usual observable characteristics.

the top of the wage distribution. As a consequence, in the presence of an economy-wide glass ceiling, the gap between male and female wages will be larger at the top of the wage distribution than at the middle or bottom.

I measure the wage gap at the  $\tau^{th}$  conditional quantile of the wage distribution using the quantile regressions that satisfies

$$(2) \quad \Pr[W_i \leq X_i' \beta^\tau + g_i \delta^\tau | X_i, g_i] = \tau,$$

where  $\beta^\tau$  measures the returns to individual characteristics at the  $\tau^{th}$  quantile, and  $\delta^\tau$  measures the difference between the  $\tau^{th}$  quantile of log wages of males and females, conditional on  $X_i$ . Comparing estimates of  $\delta^\tau$  at different quantiles enables me to study how gender wage differentials vary over the conditional wage distribution and allows me to examine the existence of a glass ceiling faced by females.

### **1.3.1. Glass Doors**

The glass door effect arises if women are disproportionately sorted into lower-paying firms, compared to their male counterparts. Such sorting may contribute to the gender wage gap. I apply the methodology developed by Pendakur and Woodcock (2010) in the context of native-immigrant wage differentials, to measure the glass door effect by comparing within-firm and economy-wide gender wage gaps. The intuition behind their methodology is that if females experience better wage outcomes within firms than they do economy-wide, it implies that their low wage outcomes, relative to their male counterparts, are partly due to segregation into lower-paying firm.

I consider three features of the conditional wage distribution in my investigation of the glass door effect: conditional means, conditional quantiles and conditional representation. I examine the effect of glass doors on conditional mean wages to assess whether female workers are, on average, employed in firms that pay lower wages relative to their male counterparts. I also estimate the glass door effect at different quantiles of the conditional wage distribution to quantify the extent to which the gender wage gap in different parts of the wage distribution, and its pattern of change throughout the wage distribution, is driven by gender differences in sorting across firms. This enables me to measure the contribution of glass doors to the economy-wide glass

ceiling. Finally, I measure the contribution of glass ceiling and glass doors to the representation of females in different regions of the conditional wage distribution, adopting and extending a methodology proposed by Pendakur et al. (2008).

To measure the glass door effect, I first need to construct within-firm measures of average gender wage disparity, which could be obtained by adding firm effects to equation (1). These firm effects will capture both observed and unobserved employer characteristics that are common to all employees and constant over time. In the mean regression case, we have

$$(3) \quad E[W_i|X_i, g_i, f_i] = X_i'\beta + g_i\delta + f_i'\psi,$$

where  $f_i$  is a vector of indicators for each firm and  $\psi$  is a vector of firm effects that measure inter-firm differences in average wages, conditional on worker and job characteristics  $X_i$  and gender  $g_i$ .<sup>3</sup> Compared to equation (1),  $\delta$  in equation (3) measures the average gender wage gap conditional on observed individual characteristics and both observed and unobserved employer characteristics that are constant over time. Since  $\delta$  is identified within firms, it measures the gender wage gap taking into account gender differences in sorting across high-paying and low-paying firms.

Pendakur and Woodcock (2010) define the glass door effect as  $\delta_f$  in the hypothetical regression:

$$(4) \quad E[f_i'\psi|X_i, g_i] = X_i'\beta_f + g_i\delta_f.$$

The coefficient  $\delta_f$  in this hypothetical regression would measure the average firm effect of female workers relative to males, conditional on their characteristics.<sup>4</sup> This

<sup>3</sup> An implicit assumption in equation (3) is that firm effects are similar for all employees of a firm, conditional on  $X_i$ , and therefore the firm effects are a location shift of the conditional wage distribution. In other words, conditional on worker characteristics and gender, the shape of the wage distribution is the same at every firm, and it is only its mean (location) that differs across firms.

<sup>4</sup> This is a hypothetical regression because we do not observe the true firm effects.

measures how wages are affected by gender differences in sorting across firms, conditional on worker's observed characteristics. Pendakur and Woodcock (2010) show that  $(\hat{\delta} - \tilde{\delta})$  is an unbiased estimator of  $\delta_f$ , where  $\hat{\delta}$  and  $\tilde{\delta}$  are estimates of  $\delta$  from equation (3) and (1), respectively. This is due to the well-known result that omitted variable bias can be recovered as least squares coefficient in an artificial regression (see, e.g., Greene 2003, pp. 148-149).

It should be noted that a zero glass door effect does not imply that firm effects do not belong to the model. Rather, it implies that, conditional on worker characteristics, firm effects are uncorrelated with gender. In other words, conditional on their characteristics, male and female workers are similarly sorted across firms. Therefore, under the null hypothesis of no glass door effect ( $H_0: \delta_f = 0$ ), both specifications produce consistent estimates of the gender wage gap,  $\delta$ , but the estimate in the specification with firm effects is inefficient. However, under the alternative hypothesis of a nonzero glass door effect ( $H_1: \delta_f \neq 0$ ), only estimates from the specification that includes firm effects are consistent. This motivates a Hausman test for the presence of a glass door effect.<sup>5</sup>

$$(5) \quad H = \frac{(\hat{\delta} - \tilde{\delta})^2}{\text{var}[\hat{\delta}] - \text{var}[\tilde{\delta}]} \sim \chi_1^2.$$

I measure the contribution of glass doors to the gender wage gap at different points of the wage distribution in an analogous fashion. I estimate quantile regression with firm effects:<sup>6</sup>

$$(6) \quad \Pr[W_i \leq X_i' \beta^\tau + g_i \delta^\tau + f_i' \psi | X_i, g_i, f_i] = \tau.$$

<sup>5</sup> See Pendakur and Woodcock (2010) for the proof.

<sup>6</sup> I use an estimator proposed by Canay (2011) to implement the quantile regressions with firm effects. Pendakur and Woodcock (2010) use Koenker and Ng's (2005) Frisch-Newton algorithm and subroutines in R to implement the quantile regression model with firm effects. However, the large number of firms and surveyed employees poses some computational challenge and creates some constraints for them. Canay's proposed estimator, however, is quite simple to compute and can be implemented in standard econometrics packages.

Pendakur and Woodcock (2010) show that if equation (6) is correctly specified, then  $(\hat{\delta}^\tau - \tilde{\delta}^\tau)$  has a similar interpretation as the mean regression case, where  $\hat{\delta}^\tau$  and  $\tilde{\delta}^\tau$  are coefficients on  $g_i$  in quantile regressions that include and exclude firm effects, respectively. Specifically,  $(\hat{\delta}^\tau - \tilde{\delta}^\tau)$  estimates the gender coefficient in a hypothetical least square regression of  $f_i'\psi$  on  $X_i$  and  $g_i$  using quantile-specific weights.<sup>7</sup> This provides a measure of the glass door effect at the  $\tau^{th}$  quantile of the conditional wage distribution. As in the mean regression case, I can also test for the glass door effect at a particular quantile using a Hausman test.

### 1.3.2. *Conditional Representation*

The location of a particular wage quantile for males and females does not provide much information about their prevalence in (or access to) a region of the wage distribution. For instance, knowing that the conditional top decile of earnings is \$20,000 lower for women than men tells us that females are under-represented in the top decile of the population conditional wage distribution, but it does not tell us the magnitude of their under-representation. Since the glass ceiling effect causes women to be under-represented in high-wage regions of the wage distribution, it would be interesting to quantify their degree of under-representation as another measure of women's labor market outcomes.

I use an index developed by Pendakur et al. (2008) to measure females' representation in different regions of the wage distribution, conditional on their observed personal and job characteristics. To construct this index, I estimate quantiles of the population wage distribution, conditional on characteristics  $X_i$ , from the quantile regression that satisfies

$$(7) \quad \Pr[W_i \leq X_i'\beta^\tau] = \tau.$$

<sup>7</sup> These weights are large (small) for employees of firms with large (small)  $\psi$  at upper quantiles of the conditional wage distribution, and the opposite at lower quantiles. For a more detailed description of these weights, see the discussion following the proof of Proposition 1 in Pendakur and Woodcock's (2010) appendix.

The conditional representation of female workers above the  $\tau^{th}$  quantile of the population wage distribution is:

$$(8) \quad \widehat{R}_f^\tau = \frac{1}{N_f} \sum_{i \in f} I(W_i \geq \widehat{W}_i^\tau),$$

where  $N_f$  is the number of females,  $I$  denotes the indicator function, and  $\widehat{W}_i^\tau$  is the  $\tau^{th}$  quantile of the population wage distribution conditional on  $X_i$  estimated by (7).  $\widehat{R}_f^\tau$  measures the proportion of female workers who earn more than the  $\tau$ th quantile of the population conditional wage distribution, given their characteristics  $X_i$ .<sup>8</sup>

I extend this methodology to quantify the effect of gender differences in sorting across high-paying and low-paying firms on females' representation in different parts of the wage distribution. I estimate quantiles of the population wage distribution, conditional on characteristics,  $X_i$ , and firm affiliation from the quantile regression that satisfies:

$$(9) \quad \Pr[W_i \leq X_i' \beta^\tau + f_i' \psi] = \tau.$$

The representation of females above the  $\tau^{th}$  quantile, conditional on their observed characteristics and their firm affiliation, is:

$$(10) \quad \widetilde{R}_f^\tau = \frac{1}{N_f} \sum_{i \in f} I(W_i \geq \widetilde{W}_i^\tau).$$

Pendakur et al. (2008) show that comparing conditional and unconditional representation indices is informative of the contribution of individual characteristics to female's over- or under-representation in different regions of the income distribution. Using the same intuition, it follows that comparing females' representation conditional on their characteristics  $X_i$ , and females' representation conditional on their characteristics

<sup>8</sup> If  $\widehat{R}_f^\tau > 1 - \tau$ , the proportion of females above the  $\tau$ th quantile exceeds the population proportion and the group is overrepresented in that region. Similarly, if  $\widehat{R}_f^\tau < 1 - \tau$ , the group is underrepresented in that region. For example, if the conditional representation of female workers in the top decile of income is 0.08, then we can conclude that there are 20 percent less females in the top decile of income than we would expect given their characteristics.



and firm affiliation is informative of how inter-firm gender segregation affects females' representation in different regions of the wage distribution.<sup>9</sup> The value of  $\widehat{R}_f^{0.9}$  measures the proportion of females in the top decile of the economy-wide population wage distribution, given their characteristics  $X_i$ . In contrast, the value of  $\widetilde{R}_f^{0.9}$  measures the proportion of females in the top decile of the within-firm population wage distribution, given their characteristics  $X_i$ . If  $\widetilde{R}_f^T > \widehat{R}_f^T$ , then females' segregation into low-paying firms explains part (or if  $\widetilde{R}_f^T \geq 0.1$ , all) of their under-representation in the top decile.

## 1.4. Data and Sample Characteristics

My estimates are based on the Workplace and Employee Survey (WES). This is one of a few linked employer-employee databases worldwide, and the only such data for Canada. The survey was administered from 1999 to 2005. The employer sample is longitudinal and refreshed every second year (i.e. in 2001, 2003 and 2005) to maintain a representative cross section. The target population of employers is all business locations in Canada that have paid employees in March of each surveyed year, except employers in Yukon, Nunavut and Northwest Territories and employers operating in crop

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<sup>9</sup> I run a simulation to confirm the validity of this interpretation. I assign males and females randomly to high-paying and low-paying firms (no inter-firm gender segregation). I then use a DGP to construct an artificial economy-wide gender wage gap. In this new dataset, the estimated economy-wide and within-firm gender wage gap are the same since there is no inter-firm gender segregation. Estimating females' representation using equations (8) and (10), I find that the difference between these two indices is zero. In other words, the glass door effect has no effect on over- or under-representation of female workers in different regions of the wage distribution if there is no inter-firm gender segregation.

production and animal production; fishing, hunting and trapping; private households, religious organizations and public administration<sup>10</sup>.

A maximum of twenty-four employees were sampled from each firm in each odd year, and were followed the next year.<sup>11</sup> My analysis is based on the pooled 1999, 2001, 2003 and 2005 cross-sections. The data from even-numbered years are not used to avoid sample selection problems associated with employee attrition in these years.

I restrict the sample to non-Aboriginal workers between the age of 24 and 65. I also restrict the sample of firms to those that report on average 6 employees or more per year, and that have at least two workers sampled over the entire period they appear in the data. The restricted sample comprises 73,251 employees of 6,584 firms. I observe between 2 and 63 employees of each firm; the mean number is 16 and the median is 15. I observe 2,373 firms in all 4 years, 1,519 firm in three years, 1,262 firms in two years and the remaining 1,430 in one year.

I estimate wage differentials and representation indices for the sample of all workers, as well as for five different subgroups including workers with at least one dependent child, workers without dependent children, workers younger than 44 years of age, workers older than 43 years of age, and single workers without dependent children.<sup>12</sup>

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<sup>10</sup> Public Administration comprises establishments primarily engaged in activities of a governmental nature, that is, the enactment and judicial interpretation of laws and their pursuant regulations, and the administration of programs based on them. Legislative activities, taxation, national defence, public order and safety, immigration services, foreign affairs and international assistance, and the administration of government programs are activities that are purely governmental in nature (Industry Canada: <http://www.ic.gc.ca/cis-sic/cis-sic.nsf/IDE/cis-sic91defe.html>). Public Administration's share of employment in Canada is around 6.5 percent (Statistics Canada, Table 281-0024).

<sup>11</sup> The number of workers sampled for each firm was proportional to firm's size except workplaces with fewer than four employees where all employees are selected.

<sup>12</sup> I use the sample of all workers and appropriate interactions with gender to identify the wage differentials for these subgroups. For instance, to estimate the average wage gap for workers younger than 44 and older than 43, I use the following regression:  $E[W_i|X_i, g_i] = X_i\beta +$

My outcome measure is the natural logarithm of hourly wages.<sup>13</sup> The individual characteristics used in my main regression specification are: highest level of schooling (8 categories), marital status (6 categories), age (9 categories), number of dependent children (5 categories), a quartic in years of (actual) full-time labor market experience, a quadratic in years of seniority with the current employer, an indicator for full-time employment, occupation (6 categories), an indicator for membership in a union or collective bargaining agreement, and indicators for being a Canadian born visible minority, white immigrant, or a visible minority immigrant.

I estimate all specifications using employee sample weights provided by Statistics Canada. Standard errors are estimated following Statistics Canada's recommended procedure, using 100 sets of bootstrap sample weights.<sup>14</sup>

Table 1.1 reports weighted sample means for males and females. In comparison to males, the average female is more educated, less likely to have children, and has fewer years of fulltime labor market experience. In terms of job characteristics, the average female has fewer years of employer seniority, is less likely to work fulltime, more likely to be a member of union or collective bargaining agreement, less likely to work flexible hours, less likely to be able to carry out work duties at home and less likely to be a manager. In terms of employer characteristics, the average female is more likely to work for a non-profit enterprise, and more likely to work for an employer with an employment or pay equity program.

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*FEMALE \* YOUNGER44 + FEMALE \* OLDER43 + YOUNGER44* Where "YOUNGER44" and "OLDER43" are indicators for workers younger than 44 and older than 43, respectively.

<sup>13</sup> The hourly wage measure includes extra earnings such as over-time, bonus, profit sharing, etc.

<sup>14</sup> The bootstrap weights will consider the potential non-independence of error terms for workers within the same firm. They will also correctly adjust for the variation due to the two-stage sampling of employees, as well as the complex survey design of the WES (Drolet 2002).

## 1.5. Results

### 1.5.1. *Glass Ceilings and Glass Doors*

Figure 1.1 illustrates the distribution of the proportion of female employees at firms in which male and female workers are employed, separately.<sup>15</sup> As the figure suggests, firms tend to be quite segregated by gender. Males on average are employed at firms where only 32 percent of workers are female, while females are on average employed at firms where 62 percent of workers are female. Figure 1.2 illustrates the distribution of estimated firm effects from equation (3) for four different categories of firms: firms with proportion of female employees below 25 percent, between 25 and 50 percent, between 50 and 75 percent, and above 75 percent. Firm effects are on average larger in firms that employ fewer females. Together, figure 1.1 and 1.2 suggest that there is significant gender segregation at the firm level, and firms that employ fewer females tend to pay higher wages, conditional on observed individual and job characteristics. This result highlights the importance of studying the effect of gender segregation across firms on gender wage gap.

Table 1.2 presents mean and quantile estimates of economy-wide and within-firm gender wage gaps, and estimates of the glass door effect. Table 1.2 also reports females' representation index in different parts of the population wage distribution, conditional on their characteristics, and firm affiliation.

Females face substantial economy-wide and within-firm average wage gaps compared to their male counterparts: about -0.16 log points and -0.11 log points, respectively, in the sample of all workers. Almost one-third (-0.05 log points) of the economy-wide average wage gap that females face is due to the glass door effect. There is also strong evidence that females face an economy-wide glass ceiling: the wage gap increases from -0.12 log points at the 10<sup>th</sup> percentile of the conditional wage

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<sup>15</sup> Both figure 1.1 and figure 1.2 are generated using data from 2003 and 2005. This is because the total number of female workers in each firm is a new variable added to WES in 2003.

distribution to -0.16 log points at 50<sup>th</sup> percentile and -0.20 log points at the 90<sup>th</sup> percentile.

Females also face within-firm glass ceilings, but their effects are much less pronounced than the economy-wide glass ceiling (-0.10 log points at the 10<sup>th</sup> percentile versus -0.12 log points at the 90<sup>th</sup> percentile). Most of the economy-wide glass ceiling, therefore, is due to the glass door effect. For example, out of an 8 percentage point increase in the economy-wide wage gap experienced by females between the 10<sup>th</sup> and 90<sup>th</sup> percentiles of the conditional wage distribution, only one-fourth is due to the increase in the within-firm gender wage gap. The remaining three-fourths is due to the increasing contribution of gender differences in sorting across firms (i.e. glass door effect). The same pattern holds when we compare the 50<sup>th</sup> and 90<sup>th</sup> percentiles.

Figure 1.3 further illustrates the importance of the glass door effect. The vertical distance between the red line (the estimated economy-wide gender wage gap) and the blue line (the estimated within-firm gender wage gap) measures the glass door effect at different points of the conditional wage distribution. The upward slope of the economy-wide gender wage gap across different quantiles is mostly due to the glass door effect. Altogether, these results suggest that, conditional on their observed personal and job characteristics, females tend to sort into lower-paying firms than their male counterparts, and this differential sorting explains a substantial part of the gender wage gap. Moreover, this differential sorting contributes more to the gender wage gap at the top of the wage distribution and hence drives the economy-wide glass ceiling. As the other panels of table 1.2 suggest, this general pattern holds for different subgroups of workers.

To assess the sensitivity of my estimates to the presence or absence of dependent children for females, I present estimates of the gender wage gap for female workers with and without dependent children, compared to all male workers, in panels 3 and 4 of table 1.2. Both groups face wage gaps similar to the overall sample of workers, although economy-wide wage gaps are slightly larger for women with dependent children than women without dependent children. Both groups face a substantial economy-wide glass ceiling that is mostly due to the glass door effect.

Panel 2 of table 1.2 presents estimates for all single workers without dependent children. In this group, there are fewer concerns regarding self-selection of females into lower-paying jobs due to child or family responsibilities, which some might argue are partly responsible for the observed gender wage gaps. The estimates reveal that single female workers also experience a substantial, though smaller economy-wide mean wage gap (-0.07 log points). Interestingly, the average glass door effect is small and statistically insignificant for this group, so that the average within-firm gender wage gap is about as large as the economy-wide wage gap. One might therefore conclude that the sole source of the average economy-wide wage gap that single females experience is the within-firm wage gap. Estimated wage gaps at different quantiles of the conditional wage distribution, however, contradict such a conclusion. Single female workers experience an economy-wide glass ceiling that is mainly driven by the glass door effect. The economy-wide wage gap is small and statistically insignificant at the bottom decile of the conditional wage distribution, while there exists a significantly large within-firm gender wage gap. This large within-firm gender wage gap is offset by a positive glass door effect. This result suggests that at the bottom of the conditional wage distribution, single females tend to be employed at higher-paying firms than their male counterparts. At the 50<sup>th</sup> percentile of the conditional wage distribution, females face substantial economy-wide and within-firm wage gaps (-0.06 log points and -0.09 log points, respectively). Again, a positive glass door effect offsets part of the within-firm gender wage gap. At the top decile of the conditional wage distribution, however, the economy-wide gender wage gap is more than twice as large as the median economy-wide gender wage gap (-0.14 log points), which is mainly attributed to a large negative glass door effect (-0.08 log points).

Single females without children are the only group of female workers that are sorted into higher-paying firms than their male counterparts at lower parts of the conditional wage distribution. To investigate the potential sources behind this difference, I estimate the gender wage gap for single females without children and non-single females, using non-single male workers as the comparison group. These estimates are illustrated in figure 1.10 and suggest there are no significant differences between wage outcomes of these two groups of female workers when compared with the same comparison group. Hence, the difference in results reported for single workers without

children at lower parts of the wage distribution might be driven by poor wage outcomes of single males without children. To test this hypothesis, I estimated economy-wide and within-firm wage gaps between single males without children and non-single males. These results are illustrated in figure 1.11 and suggest that single males without children face substantial economy-wide wage gaps with non-single males that are mainly driven by the glass door effect, except at the top of the wage distribution.<sup>16</sup> This result suggests that single males without children are sorted into lower-paying firms than non-single males. Therefore, it seems reasonable to conclude that different wage outcomes and the glass door effect faced by single females without children at lower parts of the wage distribution are driven mainly by poor wage outcomes of the single males without children that they are compared with.

As Albrecht et al. (2003) point out, a potential explanation for an economy-wide glass ceiling is a compositional effect. If females' labor market prospects have improved over time relative to males, then the wage gap between older men and women will be larger than the gap between younger men and women. On the other hand, since wages increase with experience in the labor market, older workers tend to have higher wages than younger workers. The combination of these two factors could generate an increasing gender wage gap as we move to the top of the wage distribution, which looks like a glass ceiling. The estimates reported in panels 5 and 6 of table 1.2 rule out this hypothesis. Here we see that younger workers experience larger economy-wide wage gaps than older workers. Therefore, the observed economy-wide glass ceiling in my data cannot be explained through the compositional effect described.

The mean glass door effect is larger for younger female workers than older female workers (-0.06 log points versus -0.03 log points, respectively). This result suggests that younger workers are more under-represented in high-paying firms compared to their male counterparts. Both younger and older women experience a substantial economy-wide glass ceiling that is mainly driven by the glass door effect.

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<sup>16</sup> This result is consistent with findings of Peterson et al. (2011).

The estimates illustrated in figure 1.8 suggest that the magnitudes of the economy-wide wage gap and the glass door effect are almost identical in the top half of the conditional wage distribution for both younger and older female workers. In lower parts of the conditional wage distribution, however, younger females face a glass door effect while older females face no glass doors. This result could be due to an age effect or a cohort effect. The age effect hypothesis suggests that as female workers stay longer in the labor market, they sort into higher-paying firms in lower parts of the wage distribution, thus eliminating the glass door effect they face. The cohort effect hypothesis suggests that labor market conditions have deteriorated over time in ways that have reduced females' access to high-paying firms in lower parts of the wage distribution. Therefore, younger females face glass doors at lower parts of the conditional wage distribution.

Appendix A presents estimates of a number of additional robustness checks. In each case, these alternative specifications yield estimates similar to those reported in the main text.<sup>17</sup>

### **1.5.2. Conditional Representation of Females and the Contribution of Glass Doors**

As it was explained before, I also examine the representation of females at different regions of wage distribution, conditional on their characteristics. Furthermore, I examine the extent to which females' representation in different parts of the wage

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<sup>17</sup> Table 1.A1 re-estimates the above regressions by adding some additional control variables including family income from employment (excluding worker); family income from other sources; four indicators for people who are willing but unable to work more hours due to unavailability of childcare, family responsibilities, going to school and transportation problems; an indicator for possibility to work flexible hours; and an indicator for possibility to carry out work duties at home. Table 1.A2 exclude the immigrant workers from the sample. Table 1.A3 allows the returns to observable characteristics to differ across different subgroups. Table 1.A4 decomposes the glass door effects to sorting across firms and across industries and sorting across firms and within industries. Following De la Rica et al. (2008), I also estimate the gender wage differentials for subsamples of workers stratified by education level. These results are not reported here but are available upon request. I find the same qualitative results for these subsamples.



distribution is influenced by their differential sorting across high-paying and low-paying firms. These results are also summarized in table 1.2.

Looking at the sample of all workers, females are over-represented at the bottom decile of the economy-wide population wage distribution by 21 percent ( $\widehat{R}_f^{0.1} = 0.121$ ), and under-represented at the top decile by 32 percent ( $\widehat{R}_f^{0.9} = 0.067$ ), conditional on their observed personal and job characteristics. This result is partly explained by gender differences in sorting across firms. Adding firm effects to equation (7) reduces females' representation index at the bottom decile to 15 percent ( $\widetilde{R}_f^{0.1} = 0.115$ ) and increases it at the top decile to 20 percent ( $\widetilde{R}_f^{0.9} = 0.080$ ). These findings are consistent with wage patterns I found before.

Similar results are found for the other subsamples. Females are consistently over-represented (under-represented) in the bottom (top) decile of the economy-wide population wage distribution, conditional on their characteristics. These patterns of over-/under-representation are less pronounced for females when I take into account the differential sorting of males and females across firms by looking at females' representation in different parts of the within-firm population wage distribution. Single females without dependent children are the only group of females, however, who are under-represented at the bottom decile of the population wage distribution ( $\widehat{R}_f^{0.1} = 0.093$ ). Their representation index increases to  $\widetilde{R}_f^{0.1} = 0.109$ , however, when we look at within-firm population wage distribution. This result suggests that compared to other female workers, single females without children are sorted into higher-paying firms at the bottom of the wage distribution. This is consistent with the gender wage gap estimates illustrated in figure 1.10.

### **1.5.3. Possible Explanations: Compensating Differentials versus Efficiency Wages**

My measure of glass ceiling is based on gender differences that are not explained by other job-relevant characteristics that affect wages. Ideally, inequalities that are generated by past discrimination in education or training, or from choices that people make regarding market and nonmarket goals should not be considered part of the glass ceiling. Obviously, it is impossible to measure and control for all job-relevant

characteristics that could affect wages. Therefore, part of the residual gender difference in wages may reflect differences in productivity or preferences, not discrimination.

If unobserved gender differences in productivity are driving the observed glass ceiling effect, this would imply that men are more productive than women, and this productivity gap becomes larger as we move to the top of the wage distribution. As a result, females will become increasingly under-represented in higher-paying firms. To the best of my knowledge, this explanation does not have any theoretical or empirical support. Moreover, as different studies suggest, women have smaller probabilities of promotion into high-paying jobs, and therefore reaching high-wage regions of the wage distribution, compared to their male counterparts.<sup>18</sup> Regardless of the underlying reasons behind this gender difference in promotion opportunities (such as superior ability in non-market activities, discrimination or unmeasured differences in preferences, commitment, and other unspecified factors), the sequential selection effect generated through this process should reduce the unobservable differences between men and women by the time they make it to the top of wage distribution.<sup>19</sup> Therefore, if anything, we would expect these unobservable differences in productivity to have smaller effects on residual male-female wage gaps, and gender differences in sorting across firms, as we move to the top of wage distribution.

Finally, as it is discussed below in more details, I find some evidence that suggests there is a positive relationship between firm's profitability and the proportion of

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<sup>18</sup> For instance, Lazear and Rosen (1988) develop a model of jobs where men and women have the same distribution of labor market ability, but women have superior ability in non-market activities. Their results suggest that "a woman must have greater ability than a man to be promoted. Some women are denied a promotion that goes to a lower ability man."

<sup>19</sup> Imagine that we have 120 male and 120 female workers, and there are 2 levels of management hierarchy. Women have two-thirds the chance of being promoted. Therefore, 80 women and 120 men will be promoted to the second level. If females lower chance of promotion was purely due to discrimination, since these 80 females were more stringently selected compared to their male colleagues, they will have better job-related characteristics than their male counterparts, and therefore should face lower wage gaps. If the lower odds of promotion were purely due to differences in unobserved factors such as productivity or preferences, these differences should be on average smaller between men and women in the second level, and again women should face lower wage gaps.

females employed at the firm. If females' under-representation in high-paying firms is only a reflection of their lower productivity compared to their male counterparts, we should not observe any relationship between profitability and the sex composition of workforce across firms.

The theory of compensating differentials could provide an alternative explanation for inter-firm wage differentials and subsequently gender differences in sorting across firms, which could be used to explain the observed glass ceiling effect. In the context of a compensating differentials model, the inter-firm wage differentials stem from inter-firm differences in working conditions. High-paying firms offer higher wages on average, but also have relatively harder working conditions. If men and women value job characteristics differently, then gender pay differentials may be compensated by other characteristics of female jobs such as more pleasant working conditions.<sup>20</sup> Females will choose low-paying firms because they care more about non-pecuniary aspects of a job, while men will choose high-paying firms because they care more about wages. As a result, females' under-representation in high-paying firms will become more pronounced, and gender wage gap will grow larger, if inter-firm differences in working conditions get larger as we move to the top of the wage distribution. This will generate an increasing gender wage gap that looks like a glass ceiling.

To test this possibility, I estimate a specification that controls for job characteristics including flexible work hours; possibility to carry out work duties at home; indicators of inability to work more hours due to unavailability of childcare, personal and family responsibilities, going to school, or transportation problems. I also control for total family income from employment and other sources. These results are reported in

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<sup>20</sup> The theory of compensating differentials is usually applied to explain the inter-occupational gender segregation and wage differentials while this study already controls for different occupations and looks at the segregation of females within occupations but across different firms. Filer (1985) and Jacob and Steinberg (1990) show that there are no significant differences in average measures of working conditions within occupations (even very broad categorization) and once we control for occupation the effect of these measures is not significant anymore. In addition, most of the studies that look at inter-industry wage differentials find no evidence in support of compensating differentials (Smith, 1979; Brown, 1980; Kruger and Summers, 1988).

appendix table 1.A1 and are quantitatively and qualitatively similar to the main results in table 1.2. This result suggests that these job characteristics do not explain the observed glass ceiling and glass door effects.

As a second and more comprehensive test, I examine whether reported job satisfaction differs on average between workers employed in high-paying and low-paying firms. If wages compensate for undesirable job characteristics, workers employed at lower-paying firms should report higher levels of job satisfaction, conditional on observed individual and job characteristics and worker's pay satisfaction.<sup>21</sup> I run a regression of estimated firm effects from equation (3) on the observable worker and job characteristics used in my main specification, as well as 4 indicators for pay satisfaction (very satisfied, satisfied, dissatisfied and indifferent, with very dissatisfied as the omitted category) and 2 indicators for job satisfaction (very satisfied or satisfied, and indifferent, with dissatisfied or very dissatisfied as the omitted category). I run this regression for the sample of all workers and for male and female workers separately.

The results are reported in table 1.3. Those employed at lower-paying firms do not report higher levels of job satisfaction, on average, than those employed at relatively higher-paying firms, conditional on observed characteristics and pay satisfaction.<sup>22</sup> Altogether, my results don't provide any evidence that compensating differentials contribute to the economy-wide glass ceiling through inter-firm gender differences in sorting.

Efficiency wage theory provides another potential explanation for inter-firm wage differentials. The efficiency wage hypothesis (See Shapiro and Stiglitz 1984, Stiglitz 1986, Bowles 1985, Bulow and Summers 1986, Yellen 1984 and Katz 1986) suggests that firms might find it profitable to pay above market clearing wages to increase effort, reduce shirking, lower turnover, attract a higher quality workforce, increase productivity,

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<sup>21</sup> The reason that I control for pay satisfaction rather than worker's wage is that wages will be mechanically correlated with the dependant variable.

<sup>22</sup> These results are consistent for the sample of all workers, and for the samples of male workers and female workers.

and improve worker morale and group work norms. If the conditions necessitating efficiency wage payments differ across firms, then the optimal wage will also differ across firms. This implies that workers with identical productive characteristics may be paid differently depending on their firm affiliations. These wage differences for similar workers might reflect firm characteristics that do not directly influence worker utility, and thus would not require compensating differentials in a competitive labor market. Kruger and Summers (1988), Katz and Summers (1989) and Groshen (1991a) find empirical support in favor of efficiency wage theory.

I test the predictions of efficiency wage theory regarding the relationship between firm-specific premium and firm's characteristics such as productivity and quit rates by regressing estimated firm effects from equation (3) on a wide set of firm-level characteristics including industry (14 categories), firm size (4 categories), an indicator for a pay equity program, an indicator for an employment equity program, foreign ownership (4 categories), degree of competition faced (4 categories), quit rate, proportion of full-time workers, an indicator for good labor-management relations, proportion of workers covered by a collective bargaining agreement, a standardized z-score measure for provision of non-wage benefits (e.g. dental care, life insurance, Supplemental medical, Pension plan, Group RRSP, Stock purchase, etc), an indicator for incentive compensation schemes (e.g. productivity/quality gain-sharing, individual incentive systems, merit pay and skill-based pay, or profit sharing, etc), the logarithm of training expenditures per worker, an indicator for innovative work practices in the firm (e.g. self-directed work groups, problem-solving teams, employee suggestion groups, etc), and productivity measured as the logarithm of value-added per worker.<sup>23</sup>

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<sup>23</sup> This regression is only run for the sample of for-profit firms since the productivity measure is only available for these firms. I have run the same regression for all firms, without including a productivity measure, and my results are similar to those reported here. I also use other alternative measures of training and provision of different benefits by the firm, and I find the same qualitative results. These results are available upon request. Refer to the data appendix for a more detailed description of the variables.

The results are reported in table 1.4. Firms that pay higher premiums to their employees (after accounting for inter-firm differences in workforce composition) are on average larger, more likely to have a pay equity program, face more competition, are more likely to provide non-wage benefits, have lower quit rates, have higher training expenditures, have higher productivity, are more likely to have incentive compensation schemes, and are less likely to have innovative work practices. These results support the predictions of the efficiency wage theory such as lower quit rates and higher productivity for higher-paying firms. In addition, the fact that higher-paying firms not only offer higher premiums to their employees, but also provide more non-wage benefits and training, provides further evidence against the compensating differentials theory.

The question that still remains is whether efficiency wage theory can help us to understand the glass ceiling effect faced by females arising from inter-firm gender differences in sorting? It is difficult to think of a supply-side reason that explains why women would avoid jobs with efficiency wages. On the other hand, since a central element in efficiency wage theory is wage differentials that are unrelated to productivity differentials across workers, it is natural to think that it can provide the basis for a theory of discrimination. Yellen (1984) argues that in the context of efficiency wage model, employers can costlessly discriminate against a group of workers with some observable characteristics. Bulow and Summers (1986) also develop an efficiency wage model that rationalizes discrimination based on group differences that are unrelated to productivity.

Firms paying efficiency wages would believe it is not optimal to hire women if they assume that females don't alter their behavior in response to higher wages, for instance because they are less career oriented or less productive. Or if they assume it takes a higher wage increment to deter women's behavior like shirking because they have higher quit rates and as a result the cost of losing their job is less than the cost for men. These assumptions could be based on stereotypes about female workers, considering them as more communal, caring and family oriented compared to males who might be considered as more assertive and work-oriented. If stereotype-based assumptions about females are incorrect, these lower wages are discriminatory and inefficient. Even if these assumptions about females are on average correct, it does not rule out the possibility of statistical discrimination against females that could lead to gender differences in sorting across firms. For instance, there could be statistical

discrimination against women based on beliefs in gender differences in turnover rates (Aldrich and Buchele, 1989).

I adopt an empirical test proposed by Hellerstein et al. (2002) to examine the presence of discrimination against women in the labor market in the context of efficiency wage theory, which would limit females' access to high-paying firms. I implement the test by examining the cross-sectional relationship between profitability and the sex composition of the workforce. If discrimination plays no role in gender differences in sorting across firms, then there should be no relationship between profitability and the sex composition of the workforce. In the absence of discrimination against females that blocks their access to high-paying firms, females' under-representation in high-paying firms, and the gender wage gap generated through this sorting, must reflect only observed or unobserved gender differences in productivity or preferences. Therefore, lower-paying firms with higher proportion of females should earn no higher profits than higher-paying firms with lower proportion of females. A finding that firms with higher proportion of females earn higher profits, in contrast, would be consistent with sex discrimination against females that limits their access to high-paying firms.

The profitability measure I use to test this hypothesis is the firm's gross operating revenue minus gross operating expenditures (including payroll and nonwage expenses, and the purchase of goods) divided by gross operating revenue.<sup>24</sup> The variable of interest, proportion of females in the firm, is based on the actual number of females in the firm reported by the employer.<sup>25</sup> In examining the relationship between profitability and the proportion of females in a firm, I include as control variables other demographic characteristics of the workforce, and firm-level characteristics that are likely to affect firm's profitability. The results are reported in table 1.5 and are robust across different specifications. They suggest that irrespective of the set of control variables included in

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<sup>24</sup> The average profit rate after eliminating observations with extreme values (about 1 percent of the sample) is 17%. This is slightly lower than the number reported by Hellerstein et al. (1997) using US manufacturing linked employer-employee data (22%).

<sup>25</sup> Since the question regarding the total number of females in the firm was included in the WES from 2003, the regression is implemented using only pooled 2003 and 2005 firm-level data.

the regression, there is a positive relationship between the proportion of females in the workforce and firm's profitability. For example, the point estimate in column (6) indicates that a ten percentage point increase in female employment in an average firm increases the profit rate by 0.73 percentage point.

Altogether, my results suggest that gender differences in preferences or productivity cannot explain inter-firm gender segregation and therefore the glass ceiling faced by females. My results, however, favor the predictions of efficiency wage theory with higher-paying firms discriminating against females.

## 1.6. Conclusion

I find clear evidence that females face economy-wide glass ceilings that are mainly driven by glass doors (i.e. segregation of females in lower-paying firms). I find similar patterns for different subgroups of the workforce (i.e. females without any dependent child and all males, females with at least one dependent child and all males, workers younger than 44, workers older than 43, and single workers without any dependent children). Females are significantly under-represented (over-represented) at the top (bottom) of the wage distribution, conditional on their observable personal and job characteristics, and these patterns of over/under-representation are partly due to glass doors they face. I also find that females experience substantial wage gaps throughout the conditional wage distribution, even within firms. I find no evidence that these wage patterns can be explained by compensating differentials. However, my results support the predictions of the efficiency wage theory with higher-paying firms discriminating against females.

The policy implications of my results are two-fold. First, policies that aim to identify and eliminate the glass ceiling faced by females will be more effective if they focus on mechanisms that lead women to sort into lower-paying firms. This is possible, for instance, by addressing hiring practices in higher-paying firms. Employment equity policies that target employment decisions directly could be effective in this context and will have a bigger effect in reducing the gender wage gap in high wage regions of the wage distribution. Second, more general policies that try to improve females' labor



market outcomes throughout the wage distribution will be more effective if they focus on practices that improve females' labor market performance within firms. To the extent that the jobs performed by males and females within firms require similar effort, skill, responsibilities and working conditions, policies that target pay decisions directly, such as pay equity programs, could be effective in reducing the within-firm gender wage gap. Finally, the sizable within-firm gender wage gap found in my analysis throughout the wage distribution suggests that further research is required to identify the sources of within-firm gender wage gap.

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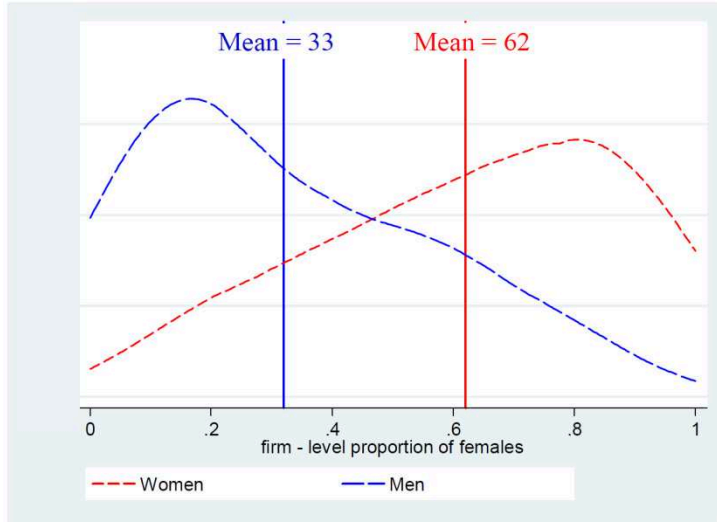
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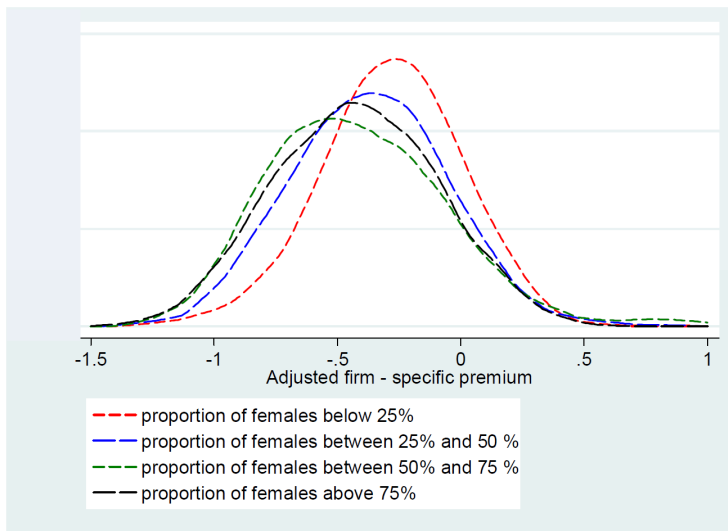
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## 1.8. Tables and Figures

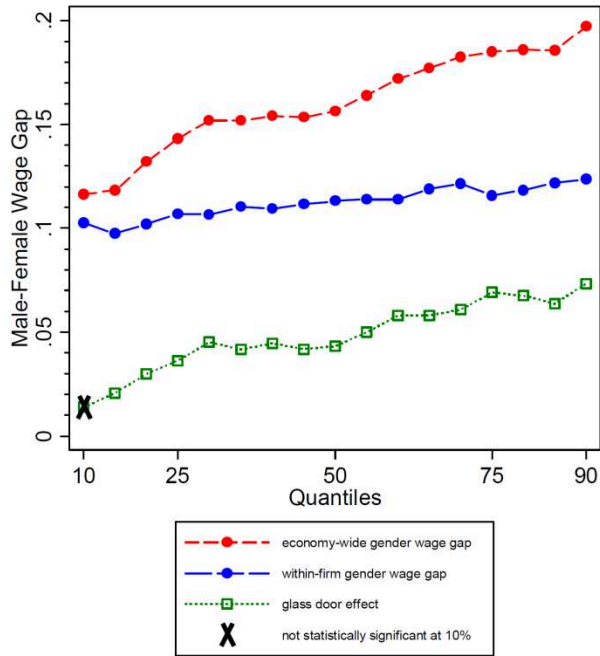
**Figure 1.1. Distribution of Firm-Level Proportion of Females, for Male and Female Employees**



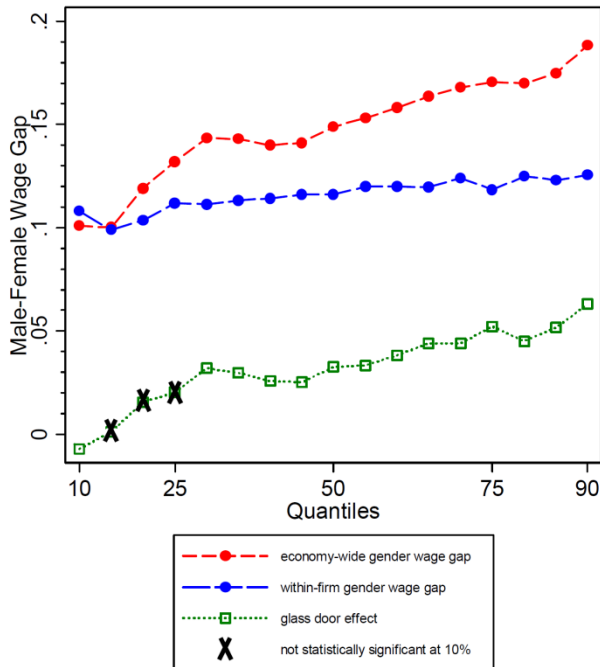
**Figure 1.2. Distribution of Firm Effects by Different Firm-Level Proportion of Females**



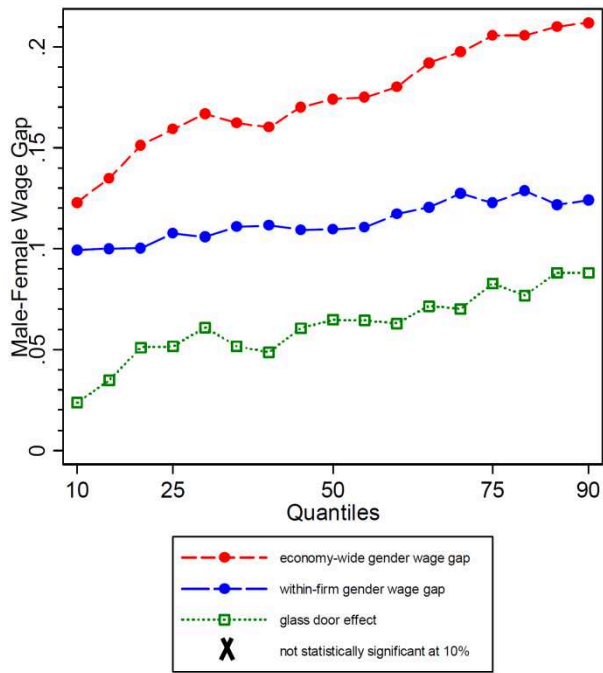
**Figure 1.3. Sample of All Workers**



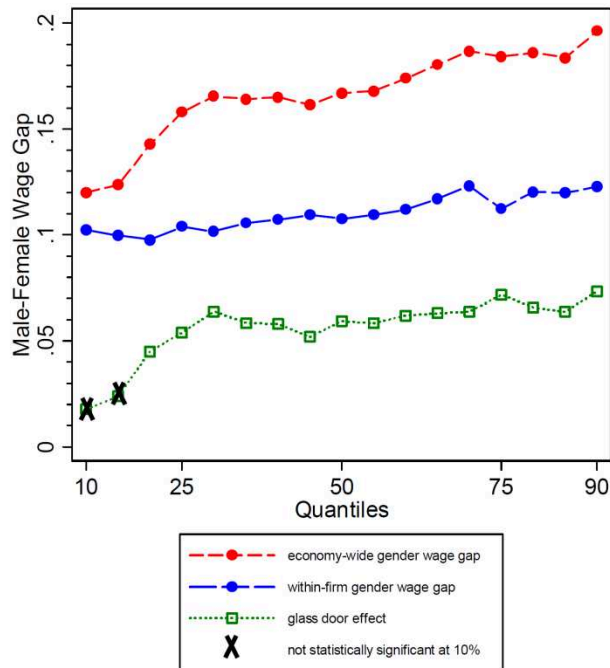
**Figure 1.4. All Female Workers without any Dependent Child and All Male Workers**



**Figure 1.5. All Female Workers with at Least One Dependent Child and All Male Workers**

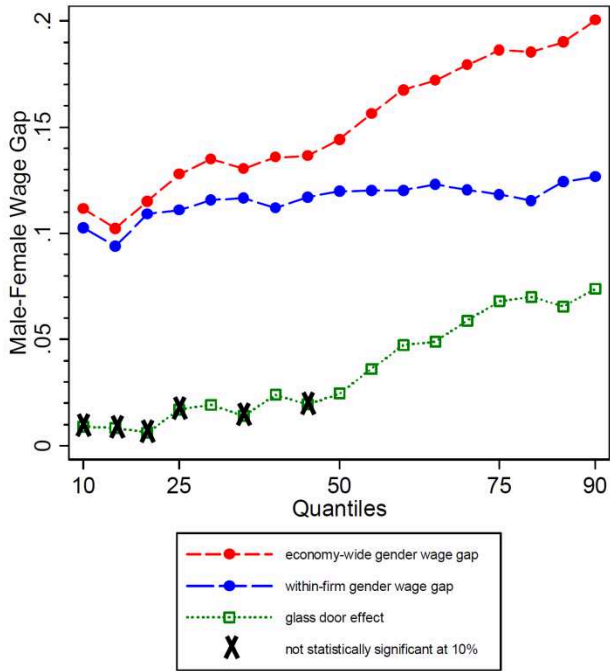


**Figure 1.6. All Workers Younger Than 44**

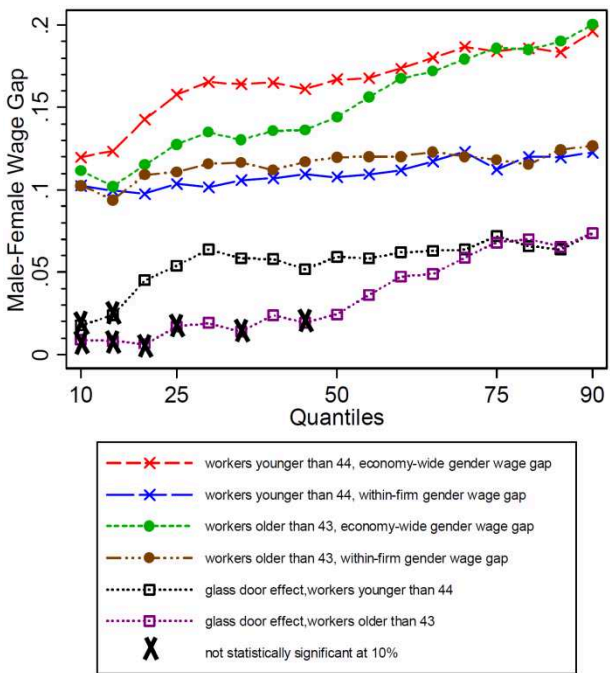




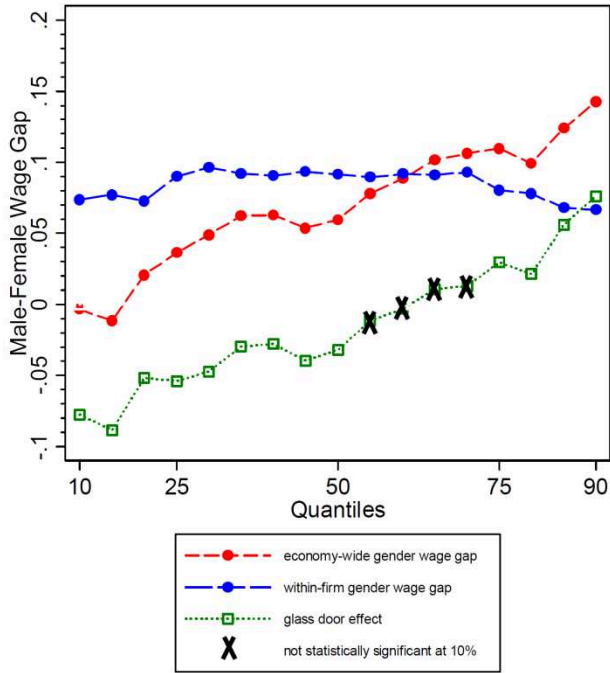
**Figure 1.7. All Workers Older Than 43**



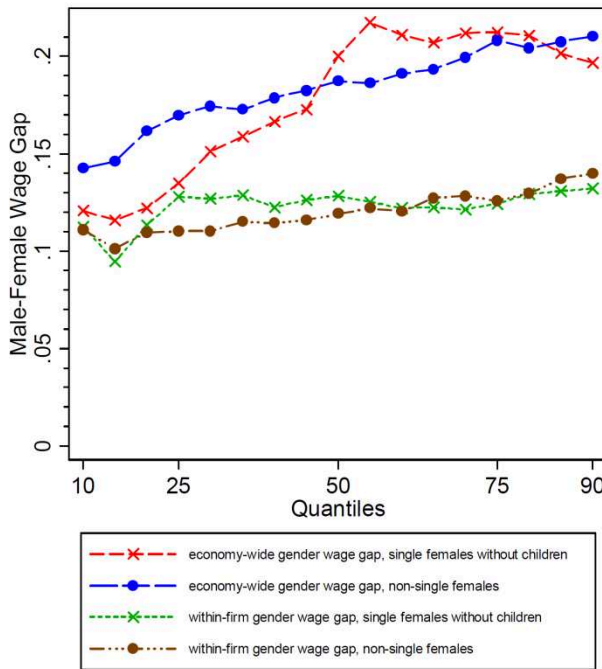
**Figure 1.8. Younger versus Older Workers**



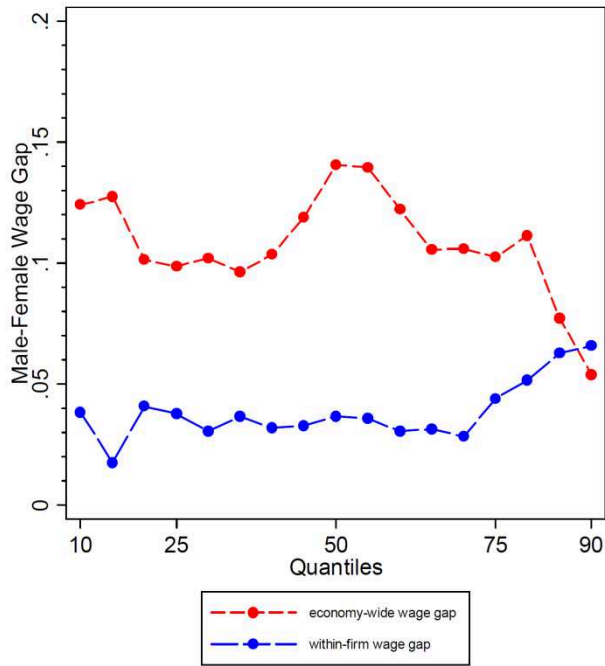
**Figure 1.9. All Single Workers without Dependent Children**



**Figure 1.10. Single Females without Dependent Children and Non-Single Females, Versus Non-Single Males**



**Figure 1.11. Single Males without Dependent Children Versus Non-Single Males**



**Table 1.1. Sample Means**

	<b>Males</b>	<b>Females</b>
Number of observations	40230	30115
<i>Subsamples:</i>		
Workers with at least one dependent child	52.53	50.12
Workers without dependent children	47.47	49.88
Workers younger than 44	43.84	43.95
Workers older than 43	56.16	56.05
Single workers without any child	18.20	18.54
<i>Personal Characteristics:</i>		
Hourly wage	24.12	19.01
Family income excluding worker (from employment) †	25,785	33,916
Family income (from other sources) †	2,486	2,480
Age	42.03	41.99
Years of (actual full-time) experience	20.01	16.70
<i>Ethnicity</i>		
Visible Minority Canadian	0.015	0.017
Visible Minority Immigrants	0.092	0.090
White Immigrants	0.116	0.104
White Canadians*	0.775	0.787
<i>Highest educational attainment</i>		
Ph.D., Master's, or M.D	0.052	0.044
Other graduate degree	0.023	0.024
Bachelor's degree	0.143	0.147
Some university	0.081	0.085
Completed college	0.168	0.253
Some college or trade certificate	0.248	0.204
High school degree	0.162	0.167
Less than high school*	0.119	0.072
<i>Marital Status</i>		
Married	0.623	0.581
Common law	0.144	0.132
Separated	0.023	0.035
Divorced	0.035	0.077
Widowed	0.004	0.015
Single*	0.168	0.157
<i>Number of Dependent Children</i>		
zero*	0.474	0.498
One	0.177	0.182
Two	0.247	0.235
Three	0.078	0.068
Four or more	0.022	0.014
<i>Willing but unable to work more hours because of †</i>		
Childcare not being available	0.001	0.002
Personal and family responsibilities	0.013	0.009
Going to school	0.002	0.003
Transportation problems	0.000	0.000

**Table 1.1. Sample Means (Continued)**

	<b>Males</b>	<b>Females</b>
<b>Job characteristics:</b>		
Fulltime	0.870	0.589
Member of Union or CBA	0.288	0.306
Years of seniority with current employer	9.717	8.817
Possibility to work flexible hours †	0.375	0.322
Possibility to carry out work duties at home †	0.280	0.238
<b>Occupation:</b>		
Manager	0.181	0.093
Professionals	0.155	0.225
Technical/Trades	0.507	0.320
Marketing/Sales	0.029	0.081
Clerical/Administrative	0.060	0.219
Production workers *	0.068	0.062
<b>Pay and benefits satisfaction considering the duties and responsibilities of the job †</b>		
Very Satisfied	0.335	0.346
Satisfied	0.570	0.562
Dissatisfied	0.072	0.071
Very Dissatisfied	0.019	0.017
No opinion	0.002	0.001
<b>Job Satisfaction †</b>		
Very Satisfied	0.270	0.302
Satisfied	0.604	0.582
Dissatisfied	0.091	0.089
Very Dissatisfied	0.028	0.024
No opinion	0.003	0.000
<b>Employer Characteristics †:</b>		
Any employment equity program	0.227	0.257
Any pay equity program	0.236	0.291
Non-profit enterprise	0.136	0.322
log(revenue per worker)	11.945	11.712
<b>Number of employees</b>		
Less than 20*	0.216	0.226
20-99	0.357	0.321
100-499	0.245	0.225
500 or more	0.180	0.226
<b>Number of competing firms</b>		
Zero	0.024	0.018
1 to 5	0.285	0.222
6 to 20	0.288	0.200
More than 20*	0.212	0.185
Missing	0.189	0.373

**Table 1.1. Sample Means (Continued)**

<i>Industry:</i>		
Resource	0.025	0.007
Labour intensive tertiary manufacturing	0.061	0.045
Secondary product manufacturing	0.057	0.022
Capital intensive tertiary manufacturing	0.082	0.031
Construction	0.064	0.013
Transportation, warehousing, wholesale	0.145	0.072
Communication and other utilities	0.027	0.012
Retail trade and consumer services	0.162	0.206
Finance and insurance	0.031	0.066
Real estate, rental and leasing operations	0.015	0.012
Business services	0.106	0.103
Education and health services	0.120	0.356
Information and cultural industries	0.036	0.034
Primary product manufacturing*	0.063	0.014

Notes: \* indicates reference category for regressions. † indicates that the variable is not used in the main regressions and is only used for robustness checks. All the means are computed using sample weights provided in the data (Statistics Canada does not allow the report of these means without using the weights).

**Table 1.2. Gender Wage Gap and Glass Door Estimates**

	(1) All workers			(2) All single workers without any dependent child		
	Economy wide	Within firms	Glass door	Economy wide	Within firms	Glass door
Mean						
Wage Differential	-0.160*** (0.008)	-0.113*** (0.007)	-0.047*** [0.000]	-0.073 *** (0.015)	-0.076 *** (0.011)	0.003 [0.292]
Quantile Differential						
10 <sup>th</sup> percentile	-0.117*** (0.017)	-0.103*** (0.010)	-0.014 [0.335]	0.003 (0.032)	-0.073 *** (0.021)	0.077*** [0.000]
Median	-0.156*** (0.011)	-0.113*** (0.006)	-0.043*** [0.000]	-0.059 *** (0.017)	-0.091 *** (0.011)	0.032*** [0.018]
90 <sup>th</sup> percentile	-0.197*** (0.019)	-0.124*** (0.013)	-0.073*** [0.000]	-0.143*** (0.039)	-0.066 *** (0.024)	-0.076** [0.012]
Number of Observations	70345	70345		70345	70345	
Females'						
Representation Index						
Below 10 <sup>th</sup> percentile	0.121	0.115		0.093	0.109	
Below Median	0.563	0.552		0.532	0.540	
Above 90 <sup>th</sup> percentile	0.067	0.080		0.077	0.093	

**Table 1.2. Gender Wage Gap and Glass Door Estimates (Continued)**

	(3) All female workers without any dependent child and all male workers			(4) All female workers with at least one dependent child and all male workers		
	Economy wide	Within firms	Glass door	Economy wide	Within firms	Glass door
Mean						
Wage Differential	-0.150*** (0.008)	-0.116*** (0.006)	-0.034*** [0.000]	-0.176*** (0.011)	-0.113*** (0.008)	-0.063*** [0.000]
Quantile Differential						
10 <sup>th</sup> percentile	-0.101*** (0.014)	-0.108*** (0.015)	0.007*** [0.000]	-0.123*** (0.015)	-0.099*** (0.012)	-0.024** [0.025]
Median	-0.149*** (0.011)	-0.116*** (0.006)	-0.033*** [0.000]	-0.174*** (0.011)	-0.109*** (0.006)	-0.065*** [0.000]
90 <sup>th</sup> percentile	-0.188*** (0.016)	-0.125*** (0.016)	-0.063*** [0.000]	-0.212*** (0.025)	-0.124*** (0.018)	-0.088*** [0.000]
Number of Observations	70345	70345		70345	70345	
Females'						
Representation Index						
Below 10 <sup>th</sup> percentile	0.110	0.113		0.133	0.118	
Below Median	0.542	0.542		0.584	0.562	
Above 90 <sup>th</sup> percentile	0.073	0.083		0.062	0.076	



**Table 1.2. Gender Wage Gap and Glass Door Estimates (Continued)**

	(5) All workers younger than 44			(6) All workers older than 43		
	Economy wide	Within firms	Glass door	Economy wide	Within firms	Glass door
Mean						
Wage Differential	-0.165*** (0.011)	-0.106*** (0.007)	-0.059*** [0.000]	-0.153*** (0.010)	-0.121*** (0.010)	-0.032*** [0.000]
Quantile Differential						
10 <sup>th</sup> percentile	-0.120*** (0.018)	-0.102*** (0.012)	-0.018 [0.192]	-0.112*** (0.019)	-0.103*** (0.013)	-0.009 [0.527]
Median	-0.167*** (0.013)	-0.108*** (0.008)	-0.059*** [0.000]	-0.144*** (0.014)	-0.120*** (0.008)	-0.024** [0.038]
90 <sup>th</sup> percentile	-0.196*** (0.031)	-0.123*** (0.015)	-0.073*** [0.000]	-0.200*** (0.023)	-0.127*** (0.022)	-0.073*** [0.000]
Number of Observations	70345	70345		70345	70345	
Females' Representation Index						
Below 10 <sup>th</sup> percentile	0.125	0.116		0.116	0.114	
Below Median	0.571	0.553		0.554	0.550	
Above 90 <sup>th</sup> percentile	0.065	0.078		0.071	0.082	

Notes: Standard errors are in parentheses, p-values for glass door test are in brackets. Simulated standard errors for estimates of females' representation are all less than 0.002. Given the precision of our estimates, we omit standard errors from the tables to minimize clutter. Details are available on request. \*\*\* indicates statistically significant at 1%, \*\* indicates statistically significant at 5%, and \* indicates statistically significant at 10%. All regressions are based on pooled samples of all males and females. Gender wage gap estimates for different subsamples are generated using interaction between gender and appropriate indicators.

**Table 1.3. OLS Regression Results, Firm-Specific Premiums and Worker Characteristics**

	All workers	Male only	Female Only
Female	-0.044*** (0.005)		
PhD., Master's, or MD	0.186*** (0.013)	0.166*** (0.018)	0.209*** (0.018)
Other Graduate Degree	0.183*** (0.011)	0.185*** (0.019)	0.190*** (0.018)
Bachelor Degree	0.183*** (0.011)	0.174*** (0.015)	0.198*** (0.014)
Some University	0.112*** (0.014)	0.075*** (0.019)	0.153*** (0.016)
Completed College	0.129*** (0.009)	0.115*** (0.012)	0.151*** (0.013)
Some college or trade certificate	0.094*** (0.008)	0.078*** (0.011)	0.112*** (0.012)
High school diploma	0.053*** (0.008)	0.031** (0.012)	0.079*** (0.012)
Married	0.039*** (0.007)	0.066*** (0.010)	0.009 (0.009)
Common Law	0.009 (0.009)	0.038*** (0.013)	-0.022* (0.011)
Separated	0.020 (0.017)	0.037 (0.027)	0.002 (0.020)
Divorced	0.039*** (0.010)	0.052*** (0.014)	0.016 (0.012)
Widowed	0.008 (0.021)	0.032 (0.059)	-0.016 (0.020)
Very satisfied or satisfied with current job	-0.004 (0.007)	-0.001 (0.011)	-0.008 (0.010)
Indifferent about current job	0.014 (0.053)	0.084 (0.053)	-0.094 (0.077)
Very satisfied with job's pay	0.173*** (0.015)	0.179*** (0.021)	0.160*** (0.017)
Satisfied with job's pay	0.109*** (0.014)	0.106*** (0.020)	0.106*** (0.015)
Dissatisfied with job's pay	0.049*** (0.013)	0.053*** (0.019)	0.043*** (0.015)
Indifferent about job's pay	0.005 (0.051)	-0.002 (0.065)	0.016 (0.080)
One child	-0.013** (0.006)	0.004 (0.007)	-0.032*** (0.009)
Two children	0.005 (0.005)	0.021*** (0.007)	-0.011 (0.008)
Three children	-0.006 (0.012)	0.022 (0.016)	-0.039** (0.016)

**Table 1.3. OLS Regression Results, Firm-Specific Premiums and Worker Characteristics (Continued)**

Four children or more	-0.018 (0.017)	0.010 (0.019)	-0.053 (0.032)
Experience	0.000 (0.003)	0.004 (0.005)	-0.000 (0.004)
Fulltime	0.057*** (0.006)	0.100*** (0.012)	0.032*** (0.006)
Member of Union or CBA	0.102*** (0.006)	0.109*** (0.008)	0.097*** (0.007)
Years of seniority	0.002*** (0.001)	0.001 (0.001)	0.004*** (0.001)
Professionals	0.034** (0.014)	0.013 (0.021)	0.061*** (0.020)
Technical/Traders	0.121*** (0.011)	0.115*** (0.016)	0.129*** (0.016)
Marketing/Sales	0.046*** (0.010)	0.036** (0.016)	0.049*** (0.013)
Clerical/Administrative	-0.122*** (0.015)	-0.074*** (0.026)	-0.131*** (0.018)
Number of observations	70345	40230	30115
Adjusted R-squared	0.208	0.177	0.243

Notes: Standard errors are in parentheses. \*\*\* indicates statistically significant at 1%, \*\* indicates statistically significant at 5%, and \* indicates statistically significant at 10%. All coefficients are estimated using sampling weights provided by Statistics Canada and all the standard errors are computed using 100 sets of bootstrap weights provided by Statistics Canada. The dependent variable is estimated firm effects after controlling for workers and job characteristics (estimates of  $\psi$  from equation 3). The regressions also include control for age (8 categories), quartic in experience and quadratic in years of seniority, immigration status and ethnicity (4 categories).

**Table 1.4. Firm-Specific Premium and Firms Average Characteristics**

Industry:		
Resource	0.150***	(0.020)
Labour intensive tertiary manufacturing	-0.117***	(0.020)
Secondary product manufacturing	0.044***	(0.015)
Capital intensive tertiary manufacturing	0.013	(0.017)
Construction	0.157***	(0.020)
Transportation, warehousing, wholesale	-0.012	(0.017)
Communication and other utilities	0.064***	(0.016)
Retail trade and consumer services	-0.156***	(0.017)
Finance and insurance	0.050**	(0.021)
Real estate, rental and leasing operations	-0.053*	(0.031)
Business services	0.072***	(0.023)
Education and health services	0.109***	(0.028)
Information and cultural industries	0.036*	(0.020)
Number of Employees:		
20-99	0.027**	(0.010)
100-499	0.081***	(0.013)
500 or more	0.122***	(0.031)
Number of competing firms		
Zero	-0.025	(0.025)
1 to 5	-0.066***	(0.018)
6 to 20	-0.047***	(0.016)
Foreign ownership		
1 to 49 percent	-0.008	(0.027)
50 to 90 percent	-0.104	(0.064)
90 to 100 percent	0.028	(0.018)
Existence of any employment equity program	0.007	(0.027)
Existence of any pay equity program	0.052*	(0.028)
Proportion of fulltime workers	0.142***	(0.032)
Proportion of workers covered by a collective bargaining agreement	0.015	(0.023)
Good rating of labor-management relations	-0.009	(0.012)
Existence of any innovative work practices	-0.033**	(0.015)
Quit rate	-0.171***	(0.063)
Log of value added per worker (proxy for productivity)	0.066***	(0.007)
Log of training expenditures per worker	0.006***	(0.002)
z-score measure for provision of different benefits	0.006***	(0.001)
Existence of incentive schemes in the compensation system	0.069***	(0.014)
Number of observations	14015	
Adjusted R-squared	0.416	

Notes: Standard errors are in parentheses. \*\*\* indicates statistically significant at 1%, \*\* indicates statistically significant at 5%, and \* indicates statistically significant at 10%. All coefficients are estimated using sampling weights provided by Statistics Canada and all the standard errors are computed using 100 sets of bootstrap weights provided by Statistics Canada. The dependent variable is estimated firm effects after controlling for workers and job characteristics (estimates of  $\psi$  from equation 3). For a detailed description of variables included in the regression please refer to the data appendix.

**Table 1.5. Firm's Profitability and the Sex Composition of the Workforce**

	(1)	(2)	(3)	(4)	(5)	(6)
% females	0.086*** (0.024)	0.101*** (0.024)	0.089*** (0.024)	0.075*** (0.026)	0.074*** (0.026)	0.073*** (0.026)
% with a bachelors degree or higher	0.000 (0.024)	-0.010 (0.023)	-0.027 (0.025)	-0.031 (0.024)	-0.029 (0.025)	-0.029 (0.025)
% with a college degree or higher	-0.023 (0.023)	-0.025 (0.023)	-0.038 (0.024)	-0.043* (0.024)	-0.043* (0.024)	-0.043* (0.024)
% with a high school degree of higher	0.018 (0.023)	0.017 (0.022)	0.005 (0.026)	0.001 (0.023)	0.002 (0.023)	0.002 (0.023)
% married	-0.007 (0.021)	-0.012 (0.020)	-0.014 (0.019)	-0.015 (0.020)	-0.016 (0.019)	-0.016 (0.019)
% immigrants	-0.006 (0.024)	-0.007 (0.024)	-0.007 (0.022)	-0.005 (0.021)	-0.003 (0.020)	-0.001 (0.020)
% with at least one dependent child	0.021 (0.019)	0.022 (0.018)	0.019 (0.019)	0.020 (0.018)	0.019 (0.018)	0.018 (0.018)
% between the age of 35 and 54	-0.022 (0.023)	-0.029 (0.022)	-0.028 (0.022)	-0.032 (0.021)	-0.032 (0.020)	-0.033 (0.021)
% older than 54	-0.020 (0.039)	-0.021 (0.039)	-0.020 (0.041)	-0.022 (0.038)	-0.024 (0.037)	-0.028 (0.038)
% with 10 to 25 years of experience	-0.006 (0.026)	-0.016 (0.026)	-0.017 (0.026)	-0.016 (0.024)	-0.016 (0.024)	-0.014 (0.024)
% years of experience > 26	0.028 (0.030)	0.010 (0.031)	0.012 (0.031)	0.018 (0.030)	0.020 (0.030)	0.024 (0.030)
% covered by union		-0.041** (0.019)	-0.043** (0.018)	-0.045** (0.018)	-0.040** (0.020)	-0.040** (0.019)
% fulltime		0.038* (0.022)	0.030 (0.020)	0.033 (0.021)	0.034 (0.021)	0.036* (0.021)
% with 10 to 25 years of		0.036* (0.021)	0.034 (0.022)	0.033* (0.019)	0.032* (0.019)	0.031 (0.019)
% with more than 25 years of tenure		0.048* (0.026)	0.048* (0.026)	0.047* (0.025)	0.047* (0.025)	0.045* (0.025)
% managers			0.017 (0.049)	0.017 (0.046)	0.017 (0.046)	0.02 (0.046)
% professionals			0.070 (0.051)	0.061 (0.049)	0.062 (0.050)	0.068 (0.049)
% technical/Trades			0.025 (0.050)	0.019 (0.046)	0.021 (0.046)	0.024 (0.045)
% Marketing/Sales			0.040 (0.053)	0.037 (0.053)	0.035 (0.053)	0.039 (0.051)
% Clerical/Administrative			0.082 (0.052)	0.077 (0.049)	0.078 (0.049)	0.083* (0.048)
Firm size 20 to 99					-0.024* (0.013)	-0.023* (0.012)
Firm size 100 to 499					-0.005 (0.015)	-0.003 (0.015)
Firm size more than 500					-0.031 (0.027)	-0.029 (0.027)

**Table 1.5. Firm's Profitability and the Sex Composition of the Workforce (continued)**

Number of competing firms: zero						0.024 (0.020)
Number of competing firms: 1 to 5						0.004 (0.012)
Number of competing firms:6 to 20						-0.007 (0.013)
Control for Industry (14 categories)	NO	NO	NO	YES	YES	YES
Number of observations	6089	6089	6089	6089	6089	6089

Notes: Standard errors are in parentheses. \*\*\* indicates statistically significant at 1%, \*\* indicates statistically significant at 5%, and \* indicates statistically significant at 10%. All coefficients are estimated using sampling weights provided by Statistics Canada and all the standard errors are computed using 100 sets of bootstrap weights provided by Statistics Canada. The dependant variable is profit rate: (gross operating revenue – gross operating income) / gross operating income. Observations with extreme values on the dependant variable (around 1 percent of the sample) are deleted. The regressions are only based on 2003 and 2005 observations since the actual number of females in a firm was only reported for those years.

## 1.9. Appendices

### 1.9.1. Appendix A: Additional Tables

**Table 1.A1. Economy-wide and within-firm wage disparities, and glass door estimates – Using additional control variables**

	(1) All workers			(2) All single workers without any dependent child		
	Economy wide	Within firms	Glass door	Economy wide	Within firms	Glass door
Mean Wage Differential	-0.161*** (0.008)	-0.108*** (0.006)	-0.053*** [0.000]	-0.075*** (0.015)	-0.078*** (0.011)	0.003 [0.735]
Quantile Differential						
10th Percentile	-0.117*** (0.015)	-0.095*** (0.009)	-0.022* [0.093]	-0.012 (0.030)	-0.074 *** (0.018)	0.062** [0.012]
Median	-0.164*** (0.010)	-0.109*** (0.005)	-0.055*** [0.000]	-0.072*** (0.023)	-0.094 *** (0.009)	0.022 [0.292]
90th Percentile	-0.195*** (0.017)	-0.120*** (0.012)	-0.075*** [0.000]	-0.121*** (0.021)	-0.059*** (0.021)	-0.062*** [0.000]
Observations	70345	70345		70345	70345	
	(3) All female workers without any dependent child and all male workers			(4) All female workers with at least one dependent child and all male workers		
	Economy wide	Within firms	Glass door	Economy wide	Within firms	Glass door
Mean Wage Differential	-0.149*** (0.008)	-0.110*** (0.006)	-0.039*** [0.000]	-0.179*** (0.011)	-0.109*** (0.008)	-0.07*** [0.000]
Quantile Differential						
10th Percentile	-0.105*** (0.019)	-0.101*** (0.010)	-0.004 [0.812]	-0.123*** (0.019)	-0.093*** (0.010)	-0.03* [0.078]
Median	-0.152*** (0.010)	-0.113*** (0.005)	-0.039*** [0.000]	-0.180*** (0.014)	-0.106*** (0.007)	-0.074*** [0.000]
90th Percentile	-0.183*** (0.017)	-0.115*** (0.014)	-0.068*** [0.000]	-0.213*** (0.020)	-0.122*** (0.014)	-0.091*** [0.000]
Observations	70345	70345		70345	70345	

**Table 1.A1. Economy-wide and within-firm wage disparities, and glass door estimates – Using additional control variables (Continued)**

	(5) All workers younger than 44			(6) All workers older than 43		
	Economy wide	Within firms	Glass door	Economy wide	Within firms	Glass door
Mean Wage Differential	-0.167*** (0.011)	-0.102*** (0.007)	-0.065*** [0.000]	-0.154*** (0.009)	-0.116*** (0.010)	-0.038*** [0.000]
Quantile Differential						
10th Percentile	-0.120*** (0.019)	-0.094*** (0.012)	-0.026* [0.099]	-0.113*** (0.021)	-0.099*** (0.011)	-0.014 [0.426]
Median	-0.171*** (0.013)	-0.107*** (0.005)	-0.064*** [0.000]	-0.156*** (0.011)	-0.113*** (0.009)	-0.043*** [0.000]
90th Percentile	-0.193*** (0.027)	-0.121*** (0.016)	-0.072*** [0.000]	-0.198*** (0.021)	-0.116*** (0.019)	-0.082*** [0.000]
Observations	70345	70345		70345	70345	

Notes: Standard errors are in parentheses, p-values for glass door test are in brackets. \*\*\* indicates statistically significant at 1%, \*\* indicates statistically significant at 5%, and \* indicates statistically significant at 10%. All coefficients are estimated using sampling weights provided by Statistics Canada and all the standard errors are computed using 100 sets of bootstrap weights provided by Statistics Canada. All regressions are based on pooled samples of all males and females. Gender wage gap estimates for different subsamples are generated using interaction between gender and appropriate indicators. Additional control variables used in these regressions are: family income from employment (excluding worker), family income from other sources, four indicator for people who are willing but unable to work more hours due to unavailability of childcare/family responsibilities/ going to school/ transportation problems, indicator for possibility to work flexible hours, indicator for possibility to carry our work duties at home.



**Table 1.A2. Economy-wide and within-firm wage disparities, and glass door estimates – Excluding all immigrants**

	(1) All workers			(2) All single workers without any dependent child		
	Economy wide	Within firms	Glass door	Economy wide	Within firms	Glass door
Mean Wage Differential	-0.170*** (0.012)	-0.117*** (0.007)	-0.053*** [0.000]	-0.083*** (0.007)	-0.083*** (0.006)	0.000 [0.964]
Quantile Differential						
10th Percentile	-0.124*** (0.014)	-0.111*** (0.011)	-0.013*** [0.000]	0.000 (0.035)	-0.097*** (0.026)	0.097*** [0.000]
Median	-0.172*** (0.015)	-0.117*** (0.008)	-0.055*** [0.000]	-0.070*** (0.021)	-0.093*** (0.015)	0.022* [0.087]
90th Percentile	-0.216*** (0.017)	-0.133*** (0.013)	-0.083*** [0.000]	-0.156*** (0.037)	-0.074*** (0.028)	-0.081*** [0.000]
Observations	58082	58082		58082	58082	
	-0.170***	-0.117***	-0.053***	-0.083***	-0.083***	0.000
	(3) All female workers without any dependent child and all male workers			(4) All female workers with at least one dependent child and all male workers		
	Economy wide	Within firms	Glass door	Economy wide	Within firms	Glass door
Mean Wage Differential	-0.161*** (0.010)	-0.122*** (0.008)	-0.039*** [0.000]	-0.186*** (0.013)	-0.117*** (0.009)	-0.069*** [0.000]
Quantile Differential						
10th Percentile	-0.119*** (0.017)	-0.112*** (0.011)	-0.007 [0.446]	-0.130*** (0.023)	-0.107*** (0.013)	0 [0.102]
Median	-0.159*** (0.011)	-0.123*** (0.007)	-0.036*** [0.000]	-0.186*** (0.016)	-0.114*** (0.009)	-0.072*** [0.000]
90th Percentile	-0.202*** (0.022)	-0.133*** (0.017)	-0.069*** [0.000]	-0.238*** (0.029)	-0.135*** (0.029)	-0.103*** [0.000]
Pbservations	58082	58082		58082	58082	

**Table 1.A2. Economy-wide and within-firm wage disparities, and glass door estimates – Excluding All Immigrants (Continued)**

	(5) All workers younger than 44			(6) All workers older than 43		
	Economy wide	Within firms	Glass door	Economy wide	Within firms	Glass door
Mean Wage Differential	-0.174*** (0.014)	-0.111*** (0.008)	-0.063*** [0.000]	-0.164*** (0.012)	-0.127*** (0.011)	-0.037*** [0.000]
Quantile Differential						
10th Percentile	-0.129*** (0.021)	-0.109*** (0.013)	-0.020* [0.098]	-0.115*** (0.020)	-0.113*** (0.015)	-0.002 [0.806]
Median	-0.180*** (0.016)	-0.113*** (0.010)	-0.067*** [0.000]	-0.159*** (0.017)	-0.121*** (0.010)	-0.038*** [0.005]
90th Percentile	-0.220*** (0.026)	-0.131*** (0.020)	-0.089*** [0.000]	-0.214*** (0.028)	-0.139*** (0.017)	-0.075*** [0.000]
Observations	58082	58082		58082	58082	

Notes: Standard errors are in parentheses, p-values for glass door test are in brackets. \*\*\* indicates statistically significant at 1%, \*\* indicates statistically significant at 5%, and \* indicates statistically significant at 10%. All coefficients are estimated using sampling weights provided by Statistics Canada and all the standard errors are computed using 100 sets of bootstrap weights provided by Statistics Canada. All regressions are based on pooled samples of all males and females. Gender wage gap estimates for different subsamples are generated using interaction between gender and appropriate indicators

**Table 1.A3. Economy-wide and within-firm wage disparities, and glass door estimates – Allowing returns to be different for subgroups**

	(1) All workers			(2) All single workers without any dependent child		
	Economy wide	Within firms	Glass door	Economy wide	Within firms	Glass door
Mean Wage Differential	-0.160*** (0.008)	-0.113*** (0.007)	-0.047*** [0.000]	-0.072*** (0.015)	-0.074*** (0.014)	0.002 [0.631]
Quantile Differential						
10th Percentile	-0.117*** (0.017)	-0.103*** (0.010)	-0.014 [0.326]	0.007 (0.029)	-0.052*** (0.025)	0.059*** [0.003]
Median	-0.156*** (0.011)	-0.113*** (0.006)	-0.043*** [0.000]	-0.062*** (0.019)	-0.090*** (0.016)	0.028** [0.012]
90th Percentile	-0.197*** (0.019)	-0.124*** (0.013)	-0.073*** [0.000]	-0.157*** (0.036)	-0.063*** (0.019)	-0.094*** [0.002]
Observations	70345	70345		11914	11914	
	(3) All female workers without any dependent child and all male workers			(4) All female workers with at least one dependent child and all male workers		
	Economy wide	Within firms	Glass door	Economy wide	Within firms	Glass door
Mean Wage Differential	-0.112*** (0.009)	-0.113*** (0.007)	0.001 [0.809]	-0.191*** (0.012)	-0.120*** (0.010)	-0.071*** [0.000]
Quantile Differential						
10th Percentile	-0.087*** (0.018)	-0.095*** (0.011)	0.007 [0.574]	-0.152*** (0.019)	-0.115*** (0.011)	-0.037** [0.014]
Median	-0.132*** (0.012)	-0.115*** (0.006)	-0.017 [0.101]	-0.188*** (0.015)	-0.119*** (0.007)	-0.069*** [0.000]
90th Percentile	-0.181*** (0.021)	-0.124*** (0.021)	-0.057*** [0.000]	-0.217*** (0.020)	-0.131*** (0.015)	-0.086*** [0.000]
Observations	55410	55410		55165	55165	

**Table 1.A3. Economy-wide and within-firm wage disparities, and glass door estimates – Allowing returns to be different for subgroups (Continued)**

	(5) All workers younger than 44			(6) All workers older than 43		
	Economy wide	Within firms	Glass door	Economy wide	Within firms	Glass door
Mean Wage Differential	-0.163*** (0.011)	-0.106*** (0.008)	-0.057*** [0.000]	-0.149*** (0.011)	-0.118*** (0.010)	-0.031*** [0.000]
Quantile Differential						
10th Percentile	-0.120*** (0.021)	-0.095*** (0.012)	-0.024 [0.163]	-0.111*** (0.025)	-0.112*** (0.010)	0.001 [0.974]
Median	-0.170*** (0.014)	-0.110*** (0.007)	-0.06*** [0.000]	-0.148*** (0.015)	-0.116*** (0.008)	-0.032** [0.014]
90th Percentile	-0.204*** (0.030)	-0.124*** (0.017)	-0.08*** [0.000]	-0.185*** (0.018)	-0.122*** (0.017)	-0.063*** [0.000]
Observations	38430	38430		31915	31915	

Notes: Standard errors are in parentheses, p-values for glass door test are in brackets. \*\*\* indicates statistically significant at 1%, \*\* indicates statistically significant at 5%, and \* indicates statistically significant at 10%. All coefficients are estimated using sampling weights provided by Statistics Canada and all the standard errors are computed using 100 sets of bootstrap weights provided by Statistics Canada.

**Table 1.A4. Decomposing the Glass Door Effect**

	<b>(1)All workers</b>			
	<b>Mean wage differential</b>	<b>10<sup>th</sup> percentile</b>	<b>Median</b>	<b>90<sup>th</sup> percentile</b>
(1) Economy-wide	-0.16*** (-0.008)	-0.117*** (0.017)	-0.156*** (0.011)	-0.197*** (0.019)
(2) Within-Industry	-0.136*** (0.009)	-0.113*** (0.014)	-0.135*** (0.011)	-0.154*** (0.022)
(3) Within-firm	-0.113*** (0.007)	-0.103*** (0.010)	-0.113*** (0.006)	-0.124*** (0.013)
(4) Sorting across firms, within and across industries [(1)-(3)]	-0.047*** [0.000]	-0.014 [0.335]	-0.043*** [0.000]	-0.073*** [0.000]
(5) Sorting across firms and across industries [(1)-(2)]	-0.024*** [0.000]	-0.004 [0.708]	-0.021*** [0.000]	-0.043*** [0.000]
(6) Sorting across firms and within industries [(2)-(3)]	-0.023*** [0.000]	-0.01 [0.305]	-0.022** [0.029]	-0.03* [0.094]
	<b>(2)All female workers without any dependent child and all male workers</b>			
	<b>Mean wage differential</b>	<b>10<sup>th</sup> percentile</b>	<b>Median</b>	<b>90<sup>th</sup> percentile</b>
(1) Economy-wide	-0.150*** (0.008)	-0.101*** (0.014)	-0.149*** (0.011)	-0.188*** (0.016)
(2) Within-Industry	-0.129*** (0.009)	-0.093*** (0.013)	-0.127*** (0.0104)	-0.148*** (0.020)
(3) Within-firm	-0.116*** (0.006)	-0.108*** (0.015)	-0.116*** (0.006)	-0.125*** (0.016)
(4) Sorting across firms, within and across industries [(1)-(3)]	-0.034*** [0.000]	0.007*** [0.000]	-0.033*** [0.000]	-0.063*** [0.000]
(5) Sorting across firms and across industries [(1)-(2)]	-0.021*** [0.000]	-0.0071* [0.098]	-0.022*** [0.000]	-0.04*** [0.000]
(6) Sorting across firms and within industries [(2)-(3)]	-0.013*** [0.000]	0.0141*** [0.000]	-0.011 [0.176]	-0.023* [0.063]

**Table 1.A4. Decomposing the Glass Door Effect (continued)**

(3) All female workers with at least one dependent child and all male workers				
	Mean wage differential	10 <sup>th</sup> percentile	Median	90 <sup>th</sup> percentile
(1) Economy-wide	-0.176*** (0.011)	-0.123*** (0.015)	-0.174*** (0.011)	-0.212*** (0.025)
(2) Within-Industry	-0.147*** (0.012)	-0.125*** (0.014)	-0.146*** (0.013)	-0.174*** (0.027)
(3) Within-firm	-0.113*** (0.008)	-0.099*** (0.012)	-0.109*** (0.006)	-0.124*** (0.018)
(4) Sorting across firms, within and across industries [(1)-(3)]	-0.063*** [0.000]	-0.024** [0.025]	-0.065*** [0.000]	-0.088*** [0.000]
(5) Sorting across firms and across industries [(1)-(2)]	-0.029*** [0.000]	0.002 [0.777]	-0.028*** [0.000]	-0.038*** [0.000]
(6) Sorting across firms and within industries [(2)-(3)]	-0.034*** [0.000]	-0.025*** [0.000]	-0.037*** [0.002]	-0.05** [0.012]
(4) All workers younger than 44				
	Mean wage differential	10 <sup>th</sup> percentile	Median	90 <sup>th</sup> percentile
(1) Economy-wide	-0.165*** (0.011)	-0.120*** (0.018)	-0.167*** (0.013)	-0.196*** (0.031)
(2) Within-Industry	-0.137*** (0.013)	-0.122*** (0.017)	-0.142*** (0.012)	-0.153*** (0.017)
(3) Within-firm	-0.106*** (0.007)	-0.102*** (0.012)	-0.108*** (0.008)	-0.123*** (0.015)
(4) Sorting across firms, within and across industries [(1)-(3)]	-0.059*** [0.000]	-0.018 [0.192]	-0.059*** [0.000]	-0.073*** [0.000]
(5) Sorting across firms and across industries [(1)-(2)]	-0.028*** [0.000]	0.002 [0.735]	-0.025*** [0.000]	-0.043*** [0.004]
(6) Sorting across firms and within industries [(2)-(3)]	-0.031*** [0.000]	-0.02 [0.109]	-0.034*** [0.000]	-0.03*** [0.000]

**Table 1.A4. Decomposing the Glass Door Effect (continued)**

<b>(5) All workers older than 43</b>				
	<b>Mean wage differential</b>	<b>10<sup>th</sup> percentile</b>	<b>Median</b>	<b>90<sup>th</sup> percentile</b>
(1) Economy-wide	-0.153*** (0.010)	-0.112*** (0.019)	-0.144*** (0.014)	-0.200*** (0.023)
(2) Within-Industry	-0.134*** (0.010)	-0.0988*** (0.018)	-0.123*** (0.015)	-0.158*** (0.024)
(3) Within-firm	-0.121*** (0.010)	-0.103*** (0.013)	-0.120*** (0.008)	-0.127*** (0.022)
(4) Sorting across firms, within and across industries [(1)-(3)]	-0.032*** [0.000]	-0.009 [0.527]	-0.024** [0.038]	-0.073*** [0.000]
(5) Sorting across firms and across industries [(1)-(2)]	-0.019*** [0.000]	-0.013*** [0.000]	-0.021*** [0.000]	-0.042*** [0.000]
(6) Sorting across firms and within industries [(2)-(3)]	-0.013** [0.045]	0.0042 [0.760]	-0.003 [0.817]	-0.031*** [0.000]
<b>(6) All single workers without any dependent child</b>				
	<b>Mean wage differential</b>	<b>10<sup>th</sup> percentile</b>	<b>Median</b>	<b>90<sup>th</sup> percentile</b>
(1) Economy-wide	-0.073 *** (0.015)	0.003 (0.032)	-0.059 *** (0.017)	-0.143*** (0.039)
(2) Within-Industry	-0.0646*** (0.015)	-0.0115 (0.027)	-0.0669*** (0.018)	-0.110*** (0.033)
(3) Within-firm	-0.076 *** (0.011)	-0.073 *** (0.021)	-0.091 *** (0.011)	-0.066 *** (0.024)
(4) Sorting across firms, within and across industries [(1)-(3)]	0.003 [0.292]	0.077*** [0.000]	0.032*** [0.018]	-0.076** [0.012]
(5) Sorting across firms and across industries [(1)-(2)]	-0.008*** [0.000]	0.015 [0.384]	0.007 [0.527]	-0.033* [0.083]
(6) Sorting across firms and within industries [(2)-(3)]	0.012*** [0.000]	0.0624*** [0.000]	0.024* [0.084]	-0.043** [0.050]

Notes: Standard errors are in parentheses, p-values for glass door test are in brackets. \*\*\* indicates statistically significant at 1%, \*\* indicates statistically significant at 5%, and \* indicates statistically significant at 10%. All regressions are based on pooled samples of all males and females. Gender wage gap estimates for different subsamples are generated using interaction between gender and appropriate indicators.

### **1.9.2. Appendix B: Data Appendix**

In this section I provide more details regarding the variables used in our regression analysis reported in table 1.4.

*Non-wage benefits:* Our measure of non-wage benefits is based on the following categories of non-wage benefits provided by employers to all employees: (1) Dental care, (2) Pension plan, (3) Group RRSP, (4) Stock purchase or other saving plans, (5) Life insurance plan, (6) Supplemental medical (7) other non-wage benefits. I use the sum of standardized z-scores of these binary indicators for each firm in every year as our non-wage benefit measure.

*Innovative work practices:* I use an indicator which is equal to one if a given firm in a given year has any of the following innovative work practices: (1) Employee suggestion program, (2) Flexible job design, (3) Information sharing with employees, (4) Problem-solving teams, (5) Joint Labour-management committees, (6) Self-directed work groups.

*Existence of incentive schemes in the compensation system:* I use an indicator which equal to one if a given firm in a given year has any of the following incentives in its compensation system: (1) Productivity/Quality gain-sharing, which are systems that reward individuals on the basis of group output or performance, (2) Individual incentive, such as bonuses, piece-rate, and commissions are systems that reward individuals on the basis of individual output or performance, (3) Merit pay and skill-based pay, which is a reward or honour given for superior qualities, great abilities or expertise that comes from training, practice etc., (4) Profit sharing, which is any plan by which employees receive a share of the profits from the workplace.

*Productivity:* Our productivity measure is based on value added per worker, where value-added is measured as gross revenue minus expenses on materials. I approximate expenses on materials by subtracting payroll expenses and expenses on non-wage benefits and training from gross operating expenditures (which includes payroll, nonwage expenses and the purchase of goods). As it was mentioned before, since the gross revenue is only provided for for-profit firms I can only include our productivity measure in a specification that excludes nonprofit firms.



*Quite rates:* our measure of quit rate is constructed by total number of people resigning between April 1<sup>st</sup> of year t-1 and March 31<sup>st</sup> of year t, divided by sum of employment at April 1<sup>st</sup> of year t-1 and number of employees hired between April 1<sup>st</sup> of year t-1 and March 31<sup>st</sup> of year t. To calculate the sum of employment at April 1<sup>st</sup> of year t-1 and number of employees hired between April 1<sup>st</sup> of year t-1 and March 31<sup>st</sup> of year t I use the sum of the following variables: (1) total employment in the last pay period of March of year t, (2) total number of employees dismissed for a cause between April 1<sup>st</sup> of year t-1 and March 31<sup>st</sup> of year t, (3) total number of employees laid-off between April 1<sup>st</sup> of year t-1 and March 31<sup>st</sup> of year t, (4) total number of employees permanently left the location because of special workforce reduction between April 1<sup>st</sup> of year t-1 and March 31<sup>st</sup> of year t<sup>26</sup>, (5) total number of employees retired between April 1<sup>st</sup> of year t-1 and March 31<sup>st</sup> of year t, (6) total number of employees resigned between April 1<sup>st</sup> of year t-1 and March 31<sup>st</sup> of year t, (7) total number of employees separated permanently for other reasons between April 1<sup>st</sup> of year t-1 and March 31<sup>st</sup> of year t.

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<sup>26</sup> Special workforce reductions include resignations and early retirements induced through special financial incentives (i.e. where employees voluntarily leave).

## 2. How do School “Report Cards” Affect School Choice Decisions?<sup>27</sup>

### 2.1. Introduction

Economists have long argued that policies designed to increase competition in markets for education can improve educational outcomes by increasing disadvantaged students' access to high quality schools, and by causing underperforming schools to become more effective or to shrink as families “vote with their feet” (Friedman 1955, Becker 1995, Hoxby 2003). Recent evidence shows that providing information about school-level achievement directly to parents can influence school choice (Hastings and Weinstein 2008). However, it is unknown whether publicly disseminating information about school achievement through the media has the same effect.<sup>28</sup> On the one hand, widespread dissemination has the potential to influence the choices of many parents, and may therefore substantially increase the effectiveness of school choice policies. However, a large increase in the demand for high-achieving schools will not increase competitive pressure on weaker schools unless preferred schools can actually accommodate more students. Furthermore, children whose parents have poor access to media, or who are not part of well-informed social networks, may not benefit from public dissemination strategies. In addition, if school achievement measures are subject to substantial sampling variation, then parents could be misled or confused when education authorities update public information about achievement. Our study

<sup>27</sup> This chapter is based on a work co-authored with Jane Friesen, Justin Smith and Simon Woodcock and is published in the *Canadian Journal of Economics* (issue 45(2), May 2012).

<sup>28</sup> Information about school achievement is publicly disseminated in jurisdictions including England (West and Pennell 2000), Chile (Urquiola, McEwan and Vegas 2007), New Zealand (Fiske and Ladd 2000), and many U.S. states (Figlio and Lucas 2004) and Canadian provinces (Cowley 2007).

addresses these issues by examining the effect of public information about school achievement on school choice behavior in British Columbia (B.C.). Our estimates are based on student-level longitudinal data for multiple cohorts of students that span the introduction of standardized testing and the subsequent wide dissemination of school-level results. We study the propensity of elementary school students to leave their school in response to new information about school-level performance on those standardized tests. We also investigate whether the response to information about school achievement differs among parents who may face higher costs of accessing the information, such as those with low income or those who do not speak English at home.

School-level achievement measures may be correlated with unmeasured characteristics of schools that influence parents' beliefs about school quality and affect student mobility. We identify parents' response to new information using two separate identification strategies that exploit the timing of testing and the release of test results. The first is a difference-in-differences approach that controls for unobserved factors that jointly determine mobility and test scores by comparing the relationship between mobility and lagged test scores before and after the public release of information about test scores. The second is a control function approach (Navarro 2008) that uses current cohort test scores to control for unobserved factors that jointly determine mobility and test scores. Because test scores are not publicly revealed until the school year following the exam, the current cohort's exam results are a valid control for such unobservables, and new information about the achievement of previous cohorts is a conditionally exogenous shock to parent's information about school quality.

We find that publicly disseminated information about school-level achievement has a substantial effect on the inter-school mobility of some public school students. In general, students are more likely to leave their school when they learn that their schoolmates have performed relatively poorly. Families that speak English at home respond strongly to early information releases, and continue to respond to subsequent releases. Families that speak a language other than English respond only to the later, more highly publicized information releases. The response is most pronounced among English-speaking families in low-income neighborhoods. Arguably, these families may have had poor private information about school quality, and hence valued the new public information more highly than families in higher-income neighborhoods. The delayed

response of non-English speakers suggests they face high costs of accessing public information.

## 2.2. Previous Literature

Hastings and Weinstein (2008) find that parents of children attending low-achieving schools in a North Carolina school district were more likely to enroll their child in a higher-achieving school when the district provided them with information about school achievement. They also find that simplified information sheets distributed randomly to parents in low- and middle-income schools doubled the estimated preference parameter on school test scores in a school choice model. Using data from the same school district, Hastings et al. (2009) find that test scores play a small role in parents' school choice decisions relative to travel distance and peer composition, and that parents' preferences vary substantially with characteristics such as income.

Unlike these studies, we focus on information that is disseminated to all parents, at all schools, through public media. Public information may have different effects on school choice behaviour compared to the private information strategies studied previously, for several reasons. First, newly informed parents, especially those of disadvantaged children, may face less competition for spaces in preferred schools when they are part of a smaller, targeted group. Second, parents of children who attend low-achieving schools may respond differently to new information than those of the broader student population. Third, media dissemination may be a less effective way to inform disadvantaged parents compared to direct communication from schools.

An alternative method for learning about the effect of public information about school-level achievement on school choice is through its effect on housing prices.<sup>29</sup> Figlio and Lucas (2004) and Fiva and Kirkebøen (2010) find that public information about school-level achievement is capitalized into housing prices in Florida and Oslo respectively, but the effect diminishes quickly over time. Kane et al. (2003) find that while housing prices reflect long-run average school-level test scores, they do not respond to year-to-year fluctuations in a given measure of school quality or to the introduction of newly framed test score information.

Housing price studies only capture the effects of information about school achievement on school choice decisions that operate through residential choice. However, the link between residential and school choice decisions in many jurisdictions is weakened by the availability of private schools, charter and magnet schools and/or open enrolment policies. To the extent that information affects school choice decisions along these margins, it will not be reflected in housing prices. Moreover, housing price studies reveal little about the characteristics of the families whose decisions are affected.

Several studies examine the direct effect of public information about achievement on school choice decisions. Mizala and Urquiola (2008) find that, when measures of school achievement are already widely available, receiving a highly publicized *SNED* award has no effect on enrollment levels, tuition fees, or socioeconomic composition of Chilean schools. Hussain (2007) finds that enrollment falls by up to 6 percent in the three years after English schools receive a public “fail” rating, while enrollment increases by up to 2 percent in schools rated “very good.”

Finally, publicly disseminated information in the form of “report cards” or rankings like those examined here has been shown to affect consumer decisions in other

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<sup>29</sup> A large body of literature examines the relationship between school-level achievement measures and real estate prices, but most studies do not focus on the effect of *new information* on prices (e.g. Black 1999; Barrow 2002; Bayer et al. 2004; Gibbons and Machin 2003, 2006; Ries and Somerville 2010). These studies typically find that residential property values are higher in neighborhoods with higher-achieving schools.

markets. These markets include health services (Dranove et al. 2003, Dafny and Dranove 2008, Jin and Sorensen 2006) and restaurant patronage (Jin and Leslie 2003).

## **2.3. Institutional Background**

### **2.3.1. School Access and Funding in B.C.**

As in many other jurisdictions, B.C. students are guaranteed access to their neighborhood “catchment” public school. B.C.’s provincial education authority (the Ministry of Education) instituted an official “open boundaries” policy in July 2002 that allows students to attend any public school that has space and facilities available after catchment area students have enrolled. Provincial legislation requires that school boards give priority to students who reside within the district; boards may elect to give priority to children whose siblings are already enrolled, and must establish policies for allocating spaces among students within a priority category. Entry into most public magnet programs is restricted to students entering Kindergarten or Grade 1, and space in popular programs is often allocated by lottery. Finally, students may choose a private school.

Along with capital funding, the B.C. Ministry of Education provides districts with operating funds in proportion to total district enrolment. Supplementary funding is provided for each student who is Aboriginal, is gifted or disabled, or who qualifies for English as a Second Language (ESL) instruction. Public districts are not authorized to raise their own revenue. Private schools receive per-student operating grants of up to 50% of the base public school rate, and are responsible for teaching the provincial curriculum and meeting various provincial administrative requirements (B.C. Ministry of Education 2005).

### **2.3.2. Testing and Information**

Prior to 1999, the BC Ministry of Education administered standardized Provincial Learning Assessment Program (PLAP) exams, in various subject areas on a rotating schedule, to students in grades 4, 7, and 10. These were replaced by standardized Foundation Skills Assessment (FSA) exams in the 1999/2000 school year. The FSAs

are administered in the spring of each year to students in grades 4, 7, and 10 in reading comprehension, writing, and numeracy.<sup>30</sup> Neither the PLAP or FSA exams has any academic consequences, and teachers and schools face no financial incentives related to students' exam performance.

PLAP exam results were never disseminated to parents or the public. The Ministry of Education first released individual and provincial, district, and school-level FSA exam results to schools in fall 2000 (based on the 1999/2000 exam). Schools were instructed to share this information with parents upon request (B.C. Ministry of Education 2000). School-level results of the 1999/2000 and 2000/2001 FSA exams were first posted on the Ministry's website in October 2001 (B.C. Ministry of Education 2001). Subsequent exam results have been posted on the Ministry's website in the following fall of each year. Since 2003, schools have been required to share individual students' exam results with parents prior to September 30. Note that in each case, FSA results are released in the school year following the year of the exam.

The Fraser Institute, an independent research and educational organization (Fraser Institute 2008),<sup>31</sup> began issuing annual "report cards" on B.C.'s elementary schools in June 2003 (Cowley and Easton 2003).<sup>32</sup> These include school scores and rankings based on FSA results. From the outset, the school report cards have received widespread media coverage in the province's print, radio and television media.<sup>33</sup>

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<sup>30</sup> The grade 10 FSA exams were discontinued after the 2002/2003 school year.

<sup>31</sup> The authors are not affiliated with the Fraser Institute in any way.

<sup>32</sup> The Fraser Institute scores released in 2003 were based on school-average exam results in reading, writing and numeracy in Grades 4 and 7, and the average gap between male and female scores on the Grade 7 reading and numeracy exams. The scores released in 2004 were constructed using different weights and included the percentage of students that did not "meet expectations" according to provincial standards (see Cowley and Easton (2008, p. 96) for details).

<sup>33</sup> A ProQuest search of Vancouver's two most widely-read daily newspapers (the Vancouver Sun and the Province) returned twelve articles (including editorial content) published about the Fraser Institute's first elementary school report cards in June, 2003.

## 2.4. The Effect of New Information on School Choice

### 2.4.1. Basic Model

We present a highly simplified model of school choice that accounts for uncertainty about school quality and focuses attention on the effects of new information.<sup>34</sup> Assume parent  $i$ 's utility ( $U_{is}$ ) depends on the quality ( $q_s$ ) of their child's school  $s$ ,

$$(1) \quad U_{is} = q_s + \varepsilon_{is}$$

where  $\varepsilon_{is}$  is a random taste-shifter with mean zero. We interpret  $q_s$  as an index of school characteristics that determine parents' utility, such as teacher experience, peer ability, the state of technology at the school, the quality of sports programs, and class size.

We assume that parents cannot perfectly observe  $q_s$ . They consequently form beliefs about each school's quality based on directly observable school characteristics  $X_s$ , such as neighbourhood income and the demographic composition of the student body. Their prior beliefs are normally distributed with mean  $X'_s\beta$  and precision  $h_{qi}$ , where  $\beta$  is the vector of weights given to observable characteristics. Parents are assumed to know  $h_{qi}$ . Although prior precision is the same for all schools, it varies between parents to reflect the idea that some (e.g., new immigrants) may have less precise beliefs about school quality than others (e.g., a native born individual who has lived in the area for many years).

Absent any additional information and given a set of available schools  $\Sigma$ , a parent chooses school  $s$  if

$$(2) \quad E[U_{is} | X'_s\beta] - c_{is} > E[U_{ik} | X'_k\beta] - c_{ik} \quad \forall k \in \Sigma, k \neq s$$

<sup>34</sup> The notation is adapted from Moretti (2010), where a similar model is used to study peer effects in movie consumption.



where  $c_{is}$  reflects the direct (e.g., tuition) and indirect (e.g., commuting distance) costs of attending school  $s$ . Given our assumed prior beliefs and utility function, this implies that the average parent chooses school  $s$  if

$$(3) \quad X'_s \beta - c_{is} > X'_k \beta - c_{ik} \quad \forall k \in \Sigma, k \neq s.$$

Now suppose that parents also observe a noisy signal  $S_s$  of each school's quality, such as standardized test scores aggregated to the school level,

$$(4) \quad S_s = q_s + \eta_s$$

where  $\eta_s \sim N(0, h_{\eta_i}^{-1})$ . The noise component  $\eta_s$  has zero mean, implying that test scores provide unbiased information about school quality. The precision of test scores as a signal of school quality,  $h_{\eta_i}$ , is known but varies across parents. This reflects the possibility that test scores are more informative signals of school quality for some parents than others.

Parents are assumed to update their expectations about each school's quality using Bayes' rule.<sup>35</sup> Their posterior beliefs are normally distributed with mean  $m_s$  and precision  $h_{q_i} + h_{\eta_i}$ , where

$$(5) \quad m_s \equiv E[q_s | X'_s \beta, S_s] = \frac{h_{q_i}}{h_{\eta_i} + h_{q_i}} X'_s \beta + \frac{h_{\eta_i}}{h_{\eta_i} + h_{q_i}} S_s.$$

Parents' updated expectation of school quality is a precision-weighted average of the signal and their prior expectation. The greater is the precision of test scores relative to prior information, the greater is the weight that parents will place on test scores. If test

<sup>35</sup> For recent applications of Bayesian learning, see Moretti (2010), Ichino and Moretti (2009), Erdem and Keane (1996), Altonji and Pierret (2001), Lange (2007), Chernen et al. (2008), and Woodcock (2010).

scores are very noisy, prior information will continue to dominate parents' beliefs about school quality.

Defining  $\theta_i = h_{\eta_i} (h_{\eta_i} + h_{q_i})^{-1}$  as the weight that parents place on test scores, and rearranging equation (5), we can write the average parent's expected utility from choosing school  $s$  as

$$(6) \quad E[U_{is} | X'_s \beta, S_s] = \theta_i (S_s - X'_s \beta) + X'_s \beta.$$

Define  $S_s^* = (S_s - X'_s \beta)$  to be the test score "shock," which represents the new information acquired from the signal. Parents will choose to enroll their child in school  $s$  if

$$(7) \quad \theta_i (S_s^* - S_k^*) > (X'_k - X'_s) \beta - (c_{ik} - c_{is}) \quad \forall k \in \Sigma, k \neq s.$$

Parents choose school  $s$  if the information shock is sufficiently good relative to other schools that it outweighs any relative differences in the schools' other characteristics and attendance costs. Conversely, parents will choose school  $s$  even if they receive a relatively poor information shock, provided its characteristics are good enough and attendance costs low enough to outweigh the "bad news" about school-level test scores. Note also that test score information only affects school choice if it is sufficiently precise to be useful ( $\theta_i > 0$ ). Furthermore,  $\theta_i$  varies across individuals because of interpersonal differences in the precision of prior beliefs, and differences in the precision of test scores as a signal of school quality.

## 2.4.2. Model Dynamics

We now extend the model to accommodate a sequence of signals rather than a one-time event. Suppose that in each period  $T$ , parents observe an unbiased signal of school quality  $S_{sT}$  that conforms to equation (4), such as the results of an annual standardized test that are revealed to the public in each school year. We define parents' beliefs about school quality recursively. After observing  $T$  signals, parents' beliefs are normally distributed with mean  $m_{sT}$  and precision  $h_{q_i} + Th_{\eta_i}$ , where

$$\begin{aligned}
(8) \quad m_{sT} &= E[q_s | X'_s \beta, S_{s1}, S_{s2}, \dots, S_{sT}] = \frac{h_{qi} + (T-1)h_{\eta_i}}{h_{qi} + Th_{\eta_i}} m_{sT-1} + \frac{h_{\eta_i}}{h_{qi} + Th_{\eta_i}} S_{sT} \\
&= \frac{h_{qi}}{h_{qi} + Th_{\eta_i}} X'_s \beta + \frac{Th_{\eta_i}}{h_{qi} + Th_{\eta_i}} \bar{S}_{sT}
\end{aligned}$$

and  $\bar{S}_{sT} = T^{-1} \sum_{t=1}^T S_{st}$  is the average of all observed signals.

From the first line of equation (8) we see that, as in the case of a single signal, parents' revised expectations about school quality are a precision-weighted average of the new signal ( $S_{sT}$ ) and expected quality prior to observing the signal ( $m_{sT-1}$ ). We also see that each new signal receives successively smaller weight in parents' Bayesian update, because the previous  $T - 1$  signals have already contributed to the precision of their beliefs, and consequently increased the weight assigned to  $m_{sT-1}$ . From the second line of equation (8), however, we see that the combined weight assigned to the average of all signals ( $T\theta_{iT}$ , where  $\theta_{iT} = h_{\eta_i} (h_{qi} + Th_{\eta_i})^{-1}$ ) increases with  $T$ , and the weight assigned to observable school characteristics  $X_s$  consequently decreases.

Defining  $S_{sT}^{**} = (S_{sT} - m_{sT-1})$  to be the information shock embodied in the new signal, and rearranging the first line of equation (8), parents choose school  $s$  over school  $k$  if

$$(9) \quad \theta_{iT} (S_{sT}^{**} - S_{kT}^{**}) > (m_{kT-1} - m_{sT-1}) - (c_{ik} - c_{is}).$$

The intuition behind this maximization condition is the same as before: parents choose school  $s$  if the information shock contains sufficient "good news" about school quality relative to what was previously believed and attendance costs.

## 2.5. Methodology

### 2.5.1. Empirical Model

For tractability and because of data limitations, we treat residential location as exogenous and examine inter-school mobility conditional on residential choice. Specifically, we model the probability that a student separates from their current school after September 30 of year  $t$  and enrolls in a new school before September 30 of year  $t + 1$ , conditional on their residential location. In terms of our theoretical model, students will separate from their current school  $s$  if some alternative school satisfies equation (9).

The fundamental identification issue is that school-level achievement measures may be correlated with unmeasured characteristics of schools that influence parents' beliefs about school quality and affect student mobility. Our first estimator addresses this problem by comparing the relationship between lagged school-average test scores and the probability of separating from the current school, conditional on observable characteristics, before and after lagged test scores were first released to the public in fall 2000. Under some identifying assumptions described below, this strategy allows us to estimate the effect of the 1999/2000 test score information on separations in the year it was released.<sup>36</sup> The estimating equation takes the form

(10)

$$y_{ist} = \alpha_0 + \alpha_1 S_{st-1} + \alpha_2 d_t^{t=2000} + \alpha_3 S_{st-1} d_t^{t=2000} + Z'_{it} \gamma + X'_{st} \beta + C'_{ist} \delta + \psi_s + \nu_{st} + \varepsilon_{ist}$$

where  $y_{ist}$  is a binary variable indicating whether student  $i$  separated from school  $s$  at the end of school year  $t$ ;  $S_{st-1}$  is a measure of lagged test scores;  $d_t^{t=2000}$  is a binary indicator for the 2000/2001 school year;  $Z_{it}$  is a vector of observable student

<sup>36</sup> According to our theoretical model, FSA scores will continue to affect school choice decisions in subsequent school years, but with a smaller weight. Estimating the effect of information on separations in years after 1999/2000 in the difference-in-differences framework therefore would require us to include higher order lags of test scores in our specification. This approach is not feasible because numeracy and reading exams were not administered regularly during the 1990s.

characteristics;  $X_{st}$  is a vector of observable school characteristics;  $C_{ist}$  is a vector of proxies for the student's cost of attending school  $s$ ;  $\psi_s$  is a fixed school effect,  $U_{st}$  is a random school-by-year effect that captures any unmeasured correlation among students' separation behavior in a given school and year;<sup>37</sup>  $\varepsilon_{ist}$  is a stochastic error term; and  $\alpha_0, \alpha_1, \alpha_2, \alpha_3, \gamma, \beta, \delta$  are coefficients to be estimated. The coefficient of interest,  $\alpha_3$ , measures how the relationship between lagged test scores and separations differs before and after the release of test score information to parents.

Since FSA testing began in 1999/2000, there is no lagged FSA score from which to identify the baseline relationship between lagged test scores and separations in 1999/2000. Instead, we use the results of the PLAP reading exam as our measure of pre-policy achievement, and use the FSA reading scores as our measure of post-policy achievement. The use of the PLAP results as a proxy for baseline achievement raises two issues. First, although the exams were not identical, they tested similar skills (Raptis and Fleming 2006: 1204), so we expect that their underlying relationship with mobility behavior would be similar. Second, because the PLAP reading test was not administered in 1998/1999, we use the 1997/1998 PLAP reading results as a proxy for the lagged baseline score. Our identifying assumption therefore is that the relationship between the 2000/2001 separations and the 1999/2000 FSA test scores (written one year previously) would have been the same as the relationship between the 1999/2000 separations and the 1997/1998 PLAP test scores (written two years previously), had information about FSA performance not been released.

We estimate a second specification that allows us to identify the effects of a series of information shocks on inter-school mobility, while separately identifying the effect of new information versus the lagged effect of previously released information, and that does not rely on proxy test score measures. This estimator includes the *current* cohort's average FSA score,  $S_{st}$ , as a control for unobserved time-varying school

<sup>37</sup> Stated differently, our reported standard errors account for clustering at the school-by-year level.

characteristics that jointly affect test scores and separations. We estimate the following specification using data from the 1999/2000 through 2003/2004 school years:

(11)

$$y_{ist} = \alpha_0 + \sum_{j=1999}^{2002} \alpha_3^j S_{sj} d_t^{j=t-1} + \sum_{j=1999}^{2002} \alpha_4^j S_{sj} d_t^{j<t-1} + \alpha_5 S_{st} + Z'_{it} \gamma + X'_{st} \beta_t + C'_{ist} \delta + \tau_t + \psi_s + \nu_{st} + \varepsilon_{ist}$$

As before,  $S_{sj}$  is a school-level aggregate of test scores. Here, however, we have no need for test scores prior to 1999/2000, and therefore all test scores are aggregates of FSA reading and math results. Each test score measure  $j$  is interacted with a pair of binary indicator variables:  $d_t^{j=t-1}$  equals one when  $j = t - 1$  and zero otherwise; similarly  $d_t^{j<t-1}$  equals one when  $j < t - 1$ . We call  $\alpha_3^j$  “news” coefficients because they measure how each information release affected students’ separation probability in the year in which that particular information first became available to parents. Each information release also takes a separate “old news” coefficient  $\alpha_4^j$  that measures its effect on separation probabilities in subsequent school years. As discussed in more detail below,  $S_{st}$  is the current cohort’s FSA score and takes coefficient  $\alpha_5$ ; and  $\tau_t$  is a fixed year effect. All other terms are as previously defined. Note, however, that  $\beta_t$  now varies over time.<sup>38</sup> This reflects our theoretical model’s prediction that parents will give less weight to observable school characteristics as more test-based information becomes available to them. As with the difference-in-differences estimator, we include fixed school effects that control for any between-school differences in average separation rates that may be correlated with between-school differences in average achievement.

<sup>38</sup> Specifically,  $\beta_t$  varies across three information “regimes” that reflect the nature of information available to parents. During the first regime (1999/2000), parents observed no formal measures of school-level achievement. Parents could observe school-average FSA exam results during the second regime (2000/2001 and 2001/2002), and they could observe both school-average FSA exam results and the Fraser Institute scores and rankings during the third regime (2002/2003 and 2003/2004).

We include the current cohort's FSA score ( $S_{st}$ ) in equation (11) to control for unmeasured time-varying school characteristics that have persistent effects on student achievement and separation probabilities. Suppose, for example, that a school hires an unusually bad grade 4 teacher in year  $t - 1$  who produces lower FSA results. If her continuing presence at the school negatively influences parents' beliefs about school quality in year  $t$ , this *directly* increases students' year  $t$  separation probability. Absent an adequate control, the bad teacher's independent effect on year  $t - 1$  FSA scores and year  $t$  separations will be confounded with parents' year  $t$  response to information about year  $t - 1$  FSA scores. It is reasonable to assume, however, that if the bad teacher influences students' separation probability in  $t$  then she also influences students' FSA performance in  $t$ . Because year  $t$  FSA scores are not observed by parents until year  $t + 1$ , they are a valid control for the "bad teacher effect" in year  $t$ , as well as any other school-level unobservables that jointly affect mobility and performance and have persistent effects over time. Controlling for the current cohort's FSA scores ( $S_{st}$ ) thus allows us to identify parents' response to *information* from lagged test scores, under the identifying assumption that unobserved time-varying factors that influenced previous cohorts' achievement are only correlated with current-year unmeasured heterogeneity in separations ( $U_{st}$  and  $\varepsilon_{ist}$ ) via their persistent effect on achievement. When this assumption is satisfied, lagged FSA scores are exogenous in the separation equation conditional on current FSA scores. The formal proof of identification is provided in an Appendix.

If parents at low-achieving schools were more constrained by neighborhood enrolment policies than parents in high-achieving schools, then separations from low-achieving schools might have increased relative to separations from high-achieving schools when the open boundaries enrolment policy took effect in 2002/2003. We therefore allow the coefficient on  $S_{st}$  to differ before and after 2002/2003. Under our maintained assumption that unobserved time-varying factors that influenced previous cohorts' achievement are only correlated with  $U_{st}$  and  $\varepsilon_{ist}$  via their persistent effect on achievement, this identifies the effect of information released in 2002/2003 separately from the effect of the change in enrolment policy.

### 2.5.2. Data

Our investigation focuses on B.C.'s Lower Mainland region, a large metropolitan area with a population of approximately 2.5 million that includes the city of Vancouver and its suburbs. It encompasses fourteen public school districts with a total annual enrollment of roughly 375,000 students in Kindergarten through Grade 12 (B.C. Ministry of Education 2007:8).<sup>39</sup>

Our student-level data are based on two administrative databases, integrated via a unique student identifier: an enrollment database (collected for each student on September 30 of each year), and an FSA exam database. Our analysis is based on an extract of the enrollment database that includes all students in the Lower Mainland who entered Kindergarten between 1994/1995 and 2003/2004. We restrict our analysis to public school students who made regular progress through the grades and remained in the Lower Mainland through grade 5. Our regression estimates are based on the subset of this population enrolled in grade 4, because the FSA exam is administered in this grade.<sup>40,41</sup> We create our indicator of separations,  $y_{ist}$ , by comparing the school at which the student was enrolled on September 30 of their grade 4 year and the school at which they were enrolled on September 30 of the following year. Because FSA results are released in October,  $y_{ist}$  measures separations during or at the completion of the grade 4 year, following the release of FSA results.

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<sup>39</sup> The region is geographically isolated from other populated areas by the U.S. border to the south, the Strait of Georgia to the west, and rugged mountains to the north and east.

<sup>40</sup> Our control function approach relies on current cohort FSA scores to control for unobserved time-varying factors that have persistent effects on FSA scores and separations. This identification strategy is most credible for those students in the current FSA cohort (grade 4). Focusing on grade 4 also allows us to control for students' own FSA scores.

<sup>41</sup> To test the hypothesis that parents' response to new information might be strongest upon initial school entry, we have also used a difference-in-differences specification to estimate how kindergarten enrollment changed in response to the release of FSA test scores. We do not report these estimates for two reasons. First, they were too imprecise for us to be able to draw any reliable conclusions. Second, impacts on enrollment levels (unlike separations) might be muted by capacity constraints, and a full analysis under such constraints is beyond the scope of this paper.



We augment these data with: (1) school-by-grade average student characteristics; (2) selected characteristics of each student's neighborhood as measured in the Census of Population; (3) school-average 1997/98 PLAP reading scores; (4) annual Fraser Institute school scores and rankings for the 1999/2000 through 2003/2004 school years, and a three-year average score released in 2003; and (5) geographic coordinates associated with each school's postal code and each student's residential postal code.<sup>42</sup>

The complete set of information shocks and the variables we use to capture them in our control function specification are summarized in Table 2.1. In each case, these variables are based on school-average performance on the FSA reading and numeracy exams. The first set of FSA results was released by the Ministry at the beginning of the 2000/2001 school year, and a new set was released in each subsequent year. The Fraser Institute released their first scores and rankings in June 2003, based on the FSA exams written in 1999/2000, 2000/2001 and 2001/2002. That release included overall scores (out of 10) for each school in each of the three years, the three-year average score (also out of 10), and school rankings based on the 2001/2002 score and the three-year average score.<sup>43</sup> The three-year average was arguably the most salient measure, since schools were ordered on this measure in the ranking published in local newspapers.<sup>44</sup> The Fraser Institute released an additional set of scores and rankings based on the 2002/2003 FSA exams in spring 2004. We normalize all information shock variables in Table 2.1 to have mean zero and variance one over schools in each year.

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<sup>42</sup> We use these geographic coordinates to calculate measures of distance between the student's home and various schools. Details of how we construct these measures are provided in the Data Appendix (Appendix C).

<sup>43</sup> Our estimation sample includes only students who attended schools for which a full set of Fraser Institute scores was released in both 2003 and 2004. See the Data Appendix (Appendix C) for details.

<sup>44</sup> See, for example, "Elementary school rankings one useful tool for B.C.," in *The Province* newspaper, June 8, 2003: pg. A.20. Also "Elementary schools get their grades, by Janet Steffenhagen in *The Vancouver Sun* newspaper, June 9, 2003: pg. B.1.

The specific control variables included in our regressions are listed in the table notes and described further in Appendix C.

## 2.6. Results

### 2.6.1. Descriptive Statistics

Our estimation sample consists of 65,180 students who attend 361 public elementary schools.<sup>45</sup> We report sample means and mean separation rates for some key characteristics in Table 2.2 (sample means for all control variables are reported in Table 2.A1 in Appendix B). Almost five percent of students self-report as Aboriginal, and these students have significantly higher separation rates than average (18.4% vs. 8.9%). Almost one-third of students speak a language at home other than English, and overall these students have a higher than average separation rate. Only a small fraction (3.6%) has been diagnosed with disabilities at this early stage of their education and approximately 7% of students attend a French Immersion program. The separation rate of disabled students is higher than average (13.6%) and that of French Immersion students is lower than average (6.4%).

Table 2.3 shows school separation rates by grade for the five Kindergarten cohorts that we are able to follow through grade 5. Over 60% of students remain in the same school throughout these grades, and about 30% separate once. The remaining students experience multiple separations between Kindergarten and grade 5. The separation rate is highest following Kindergarten, but is still fairly high (between 8% and 10%) following grade 4.

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<sup>45</sup> Students with missing data are excluded. In particular, note that our sample includes only students who made regular progress through grades K-5 in a Lower Mainland school. This excludes students who separate and move to a school outside of the province. See the Data Appendix (Appendix C) for information about the nature and frequency of missing data.

## **2.6.2. Econometric Estimates**

Our theoretical model contains a number of testable implications. Most fundamentally, when parents observe new information about school quality, they may alter their original school choice if the information shock makes an alternative school appear more attractive. For this to occur, the shock must provide new information about school quality rather than simply confirming what they already know, and the signal cannot be so noisy relative to prior information that parents ignore it.

### **2.6.2.1. Difference-in-differences Estimates of Response to First Information Shock**

We begin by investigating parents' response to the first public release of information about school-level achievement. On the one hand, we expect parents to respond most strongly to this first shock, since our model predicts that parents' response to new releases of test score information gets weaker over time as information accumulates and their beliefs about school quality become increasingly precise. On the other hand, this first information release was not as widely publicized as subsequent releases, so its effect may have been muted if some parents did not absorb and act on this information.

Selected coefficient estimates from our difference-in-differences estimator (eq. 10) are presented in Table 2.4.<sup>46</sup> Column 1 presents estimates for the full sample of grade 4 students in 1999/2000 and 2000/2001. The estimated coefficient of interest (the lagged test score interacted with an indicator for the first year test score information was publicly released) is negative. This indicates that students' separation probability declined at public schools that received better news (higher school-average test scores),

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<sup>46</sup> Complete coefficient estimates are given in Appendix B, Table 2.A3. All else equal, the probability of separation is higher among disabled students, and is strikingly higher among Aboriginal students. It is lower among high-achieving students and students in English as a Second Language programs. Distance to school has a significant positive effect on separations, but the magnitude is small. Unsurprisingly, prior mobility is a strong predictor of current separation. Students who live in neighborhoods where a greater proportion of household heads have a university degree are substantially more likely to leave their school.

relative to public schools where the news was worse. However the estimate is small and imprecise and we cannot reject the null of no effect at conventional levels.

The remaining columns of Table 2.4 explore possible heterogeneity in parents' response to the first information release. In columns 2 and 3, we divide the sample into students who report speaking English at home and those who report speaking another language. Language barriers may impede some parents' access to information, reducing the precision of test scores as signals of school quality.<sup>47</sup> Indeed, we find no evidence that non-English speakers responded to the first information release. In contrast, we observe a substantive and statistically significant response among parents who speak English at home: all else equal, a one standard deviation improvement in a school's average test score reduced students' separation probability by a full percentage point on a baseline separation rate of 8.3%.

In the remaining columns of Table 2.4, we investigate how parents' responses to the first information release varied by neighborhood income. Parents who live in disadvantaged communities may have relatively poor access to private information (i.e., imprecise prior beliefs) or fewer school choice opportunities, both of which could mediate their response to information about school achievement. We consequently break out families who reside in Census EA/DAs in the top (richest) and bottom quartiles of the distribution of average household income. The results in columns 4 and 6 suggest that parents in top quartile neighborhoods do not respond to test score information, regardless of home language. Families in high-income neighborhoods may already have had good access to private information, so that the new public information did not cause them to update their beliefs about schools in any meaningful way. In contrast, English-speaking families in low-income neighborhoods responded quite strongly to new information (column 5). We investigate this further below.

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<sup>47</sup> Home language may also proxy for preferences or cultural norms.

### 2.6.2.2. Control Function Estimates

Our estimates of parents' response to the first release of school-average test scores suggest that either this information did not reach certain groups, or the quantity or quality of the news it contained was not sufficient to alter their school choices. Further insight into the factors that shape parents' heterogeneous responses can be gained by investigating how they responded to subsequent releases of test scores, when this information was more widely disseminated. We consequently turn to estimates for the full series of information shocks, based on our control function specification. This specification allows us to distinguish between the lingering effects of previous information releases versus the effect of newly released information. Recall that our theoretical model predicts that even after new information about school quality is observed, "old news" continues to influence parents' beliefs (via  $m_{sT-1}$ ) and hence their choices.

The first column of Table 2.5 presents selected coefficient estimates for the full sample of grade 4 students.<sup>48</sup> We restrict the specification to a single information measure in each year: FSA exam scores in the first two years (when these were the only information measures available) and Fraser Institute scores in the latter two years (since these were published in the media, and therefore are arguably more salient).<sup>49</sup> In three of four years, the coefficient estimates are negative, indicating that students' separation probability declined at schools where the news was better. The exception is the second release of Fraser Institute scores, where the coefficient is effectively zero. The point estimates imply that a one standard deviation increase in the 1999/2000 FSA score relative to other schools reduced students' separation probability by 0.9 percentage

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<sup>48</sup> Complete coefficient estimates are given in Appendix B, Table 2.A4.

<sup>49</sup> Estimates for specifications that include the full set of information measures released in each year (for those years where multiple measures were released, e.g., 2002/2003 when the Ministry published school-average FSA scores via its website and the Fraser Institute released their first set of scores and rankings) are available on request. Because contemporaneous information measures are highly correlated (see Appendix B, Table 2.A2), estimates from specifications that include multiple information measures for each year are imprecise and difficult to interpret. Hence we prefer the reported estimates.

points. This is almost identical to the corresponding point estimate from the difference-in-differences estimator. The corresponding figure for the 2000/2001 FSA score is 1.1 percentage points, and 3.5 percentage points for the first release of Fraser Institute scores. Only the latter release had any effect beyond the initial year and, as predicted by our model, the “old news” effect was smaller than the “news” effect (-0.027 versus -0.035). The estimated “old news” effects associated with the other information releases are all statistically insignificant, and the point estimates are small.

The coefficient on the current-year mean FSA score is statistically insignificant, indicating no systematic relationship between current-year achievement and separations.<sup>50</sup> The sign of the point estimate on the interaction between the current-year mean FSA score and an indicator for those years that the open enrolment policy was in effect is positive, indicating that if anything open enrolment *increased* separations from high-achieving schools relative to low-achieving schools. Thus we are confident that the estimated negative effect of the first Fraser Institute release, which coincided with the introduction of open enrolment, captures parents’ response to the release of the Fraser Institute report cards, and not unobserved heterogeneity that jointly affects achievement and mobility, or changes in behavior associated with the introduction of open enrolment. Furthermore, the statistically significant response to FSA scores released by the Ministry in 2000 and 2001, which predate the introduction of the open boundaries policy, reinforces the impression that some parents were able to respond to new information about school-level achievement even absent official open enrolment policies.

As with the difference-in-differences estimates, the point estimates in columns 2 and 3 indicate that parents of children who speak English at home responded to the first release of FSA exam scores, while non-English speaking parents did not. The magnitude of the point estimate is slightly larger than from the difference-in-differences estimator, and implies that when a school scored one standard deviation higher in the distribution of published school-average FSA scores, students’ separation probability

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<sup>50</sup> In other specifications reported below, the coefficient on current-year FSA scores differs significantly from zero.

declined by 1.3 percentage points. On a base separation rate of about 8.3% per year, this is quite a large response. Parents in this group responded further to the first release of information by the Fraser Institute in 2002. The magnitude of the point estimate implies that when a school scored one standard deviation higher in the distribution of Fraser Institute scores, students' separation probability declined by 3.1 percentage points. Again, this is quite a large response.

As before, parents of children who report speaking a language other than English at home did not respond to the release of FSA scores in 2000/01 and 2001/02. However, they did respond to the release of Fraser Institute scores. The point estimate implies that a one standard deviation increase in the first Fraser Institute score relative to other schools reduced these students' separation probability by 4.6 percentage points. Such a large response suggests poor access to previously released information, rather than resources or preferences, explains these parents' delayed response to information about school-level achievement.

A potential concern is that language barriers may not be the genuine cause of observed heterogeneity in responses. Rather, heterogeneity could be driven by correlates of language, such as income. In Table 2.6, we present estimates broken out by quartiles of the distribution of neighborhood income. The results follow essentially the same pattern as the difference-in-difference estimates for the first information release. Parents in top quartile neighborhoods, both in the full sample and in the English-speaking sub-sample, do not respond to test score information. In contrast, those in low-income neighborhoods respond strongly. Public information releases evidently contained substantial news for these parents, leading them to update their beliefs about school quality and respond substantively. Non-English speaking parents do not respond to the first or second release of FSA scores by the Ministry, regardless of neighborhood income. However they do respond to subsequent releases of Fraser Institute scores, although the timing of the response differs by neighborhood income. Overall, it seems clear that access to information about test scores, rather than school choice opportunities, preferences or financial resources, is the essential factor determining how parents respond.

We explore the sensitivity of our results to sample composition and specification in Table 2.A5 in Appendix B. These robustness checks show that English-language parents' estimated response to information is not driven by the behavior of Aboriginal parents or parents of French Immersion students (as shown in Table 2.2, both of these groups had unconditional separation rates significantly different from the average student); nor are our estimates sensitive to specifying information measures based on schools' Fraser Institute rankings instead of Fraser Institute scores.

Under our identifying assumptions, our reported estimates can be interpreted as causal. We cannot test these identifying assumptions directly. We therefore look for contradictory evidence via two falsification tests for each specification reported in Tables 2.A6 and 2.A7. In each, we replace our "news" variables with false information measures based on year  $t + 1$  and year  $t$  test scores respectively, and correspondingly update the "oldnews" variables. Parents could not directly observe these false news measures at the time they were making school choice decisions, and consequently there should be no systematic relationship between them and separations. Estimates, reported in Tables 2.A6 and 2.A7 in Appendix B confirm this to be true.

## 2.7. Conclusion

We find that the public release of information about school-level achievement had a substantial effect on the inter-school mobility of some public school students in the Lower Mainland of B.C. A substantial proportion of parents appear to revise their beliefs about the relative quality of their child's school in response to this information, and "vote with their feet" by moving their child to a preferred school. This response is observed primarily among parents who reside in low-income neighborhoods, and occurs the first time that school-level achievement measures are placed in the public domain. While both English and non-English language parents respond strongly to public information about school achievement, non-English parents appear to face higher costs of accessing school achievement information. They respond strongly to school achievement information, but only when the media provided widespread coverage to the Fraser Institute's school report cards. These results suggest that high-profile dissemination can



play a crucial role in ensuring access to publicly provided information in environments with culturally and linguistically diverse populations.

Jurisdictions that publicize school-level results typically update this information annually, raising concerns that parents may respond to year-to-year fluctuations that are largely noise (Kane and Staiger 2002, Mizala, Romaguera and Urquiola 2007). Our results show that English-speaking parents in low-income neighborhoods respond immediately to the first release of information, and continue to respond to subsequent releases in later years. Our data provide no way to determine whether these ongoing responses are a series of reactions to noisy information updates, or whether they simply reflect the time it takes for information to reach all members of the community. Likewise, the delayed response of non-English-speaking parents suggests substantial heterogeneity in parents' access to public information. Consequently, annual releases of school achievement information that elicit ongoing media coverage may play an important role in communicating that information to all segments of the community, including recent immigrants.

Our results add to a growing body of evidence that information about school-level achievement affects behavior in ways that may have real consequences for educational outcomes. In addition to ensuring that all parents are able to access the information provided, educational authorities should therefore take care to ensure that widely disseminated information brings competitive pressure to bear on schools that are ineffective, rather than on schools that serve disadvantaged populations. As a growing literature attests, designing meaningful measures of school effectiveness continues to be a challenge (Hægeland et al. 2004, Mizala, Romaguera and Urquiola 2007).

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## 2.9. Tables

**Table 2.1. Information Shocks and Information Variables**

Information	Date	"News" Variables	"Old News" Variables
1999/2000 cohort school mean FSA exam results released to parents on request	Oct. 2000	(1999 Mean FSA Score)*(Yr=2000)	(1999 Mean FSA Score)*(Yr>2000)
2000/2001 cohort school mean FSA exam results released on Ministry of Education website	Oct. 2001	(2000 Mean FSA Score)*(Yr=2001)	(2000 Mean FSA Score)*(Yr>2001)
2001/2002 cohort school mean FSA exam results released on Ministry of Education website	Oct. 2002	(2001 Mean FSA Score)*(Yr=2002)	(2001 Mean FSA Score)*(Yr>2002)
1999/2000, 2000/2001 and 2001/2002 cohort Fraser Institute (FI) scores and rankings released	June 2003	(1999-2001 Mean FI Score)*(Yr=2002);(2001 FI Score)*(Yr=2002)	(1999-2001 Mean FIScore)*(Yr>2002); (2001 FI Score)*(Yr>2002)
2002/2003 cohort school mean FSA exam results released on Ministry of Education website	Oct. 2003	(2002 Mean FSA Score)*(Yr=2003)	out of sample
2002/2003 cohort Fraser Institute scores and rankings released	June 2004	(2002 FI Score)*(Yr=2003)	out of sample

Source: See text.

Note: Calendar years in "News" and "Old news" variable names refer to the calendar year in which the school year began. For instance, "2001 FI Score" refers to the Fraser Institute score based on the FSA exam administered in the 2001/2002 school year. This measure was released in June 2003, and hence could first affect separations at the end of the 2002/2003 school year (Yr=2002).

**Table 2.2. Sample Percentages and School Separation Rates**

	Sample Percent	Separation Rate
All	100	8.9
Male	50.6	8.9
Non-English Home Language	32.4	10.1
English Home Language	67.6	8.3
English as a Second Language	30.7	10.1
Aboriginal	4.7	18.4
Disabled	3.6	13.6
Attends French Immersion	6.8	6.4

Source: Authors' calculations based on B.C. Ministry of Education enrollment database.

**Table 2.3. Frequency of Separations by Year of Kindergarten Entry**

Kindergarten Entry Year	Never Separated Before Grade 5	Separated Once Before Grade 5	Separated After...				
			Kindergarten	Grade 1	Grade 2	Grade 3	Grade 4
1995	0.610	0.292	0.151	0.120	0.107	0.094	0.091
1996	0.606	0.294	0.165	0.117	0.103	0.099	0.080
1997	0.618	0.292	0.147	0.111	0.096	0.090	0.097
1998	0.617	0.294	0.141	0.106	0.086	0.100	0.099
1999	0.605	0.305	0.138	0.098	0.109	0.103	0.103

Source: Authors' calculations based on B.C. Ministry of Education enrollment database.

**Table 2.4. Difference-in-Differences Estimates of the Effect of Information about School-level Achievement on Separation Probability**

	(1)	(2)	(3)	(4)	(5)	(6)	(7)
	Full Sample		Non-English	English		Non-English	
	All	English		Top Quartile	Bottom Quartile	Top Quartile	Bottom Quartile
Lagged Score	-0.003 (0.004)	-0.003 (0.004)	-0.001 (0.007)	0.003 (0.007)	-0.009 (0.014)	-0.016 (0.035)	-0.019 (0.012)
Lagged Score*(Yr=2000)	-0.007 (0.004)	-0.010** (0.005)	0.003 (0.008)	0.000 (0.009)	-0.024* (0.014)	-0.010 (0.033)	0.021* (0.013)
Number of Observations	26360	18599	7761	6207	3323	995	2709
Number of Schools	361	361	347	254	306	191	238

*Source:* Authors' calculations based on B.C. Ministry of Education enrollment database and auxiliary data.  
*Notes:* "Lagged score" refers to the school-average 1998 PLAP reading score in 1999; and the school-average 1999/2000 FSA reading score in 2000. All scores are normalized to have mean zero and variance one over schools in each year. Additional control variables in these regressions are: main effects for student characteristics (non-English home language; Aboriginal; enrolled in ESL program; male; disabled; gifted; changed schools prior to Grade 4; enrolled in French Immersion, own FSA reading and numeracy scores, travel distance to school, and the numbers of public and private schools nearby), school proportions of student characteristics (non-English home language; Aboriginal; enrolled in ESL program; male; disabled; enrolled in French immersion) fully interacted with year dummy, school proportion excused from the FSA reading exam, Census characteristics for the student's EA/DA of residence (mean and dispersion of household income; proportion visible minority; proportion one-parent families; unemployment rate; average dwelling value; proportion of dwellings owned; proportion moved last year and in last 5 years; proportion of household heads with less than grade 9 education, some high school, high school, and bachelor's degree or higher; proportion immigrant), and fixed main effects for year and school. See Table 2.A3 in Appendix B for complete coefficient estimates for specifications in columns 1-3 and additional information. Complete coefficient estimates for all other specifications available from the authors on request. Robust standard errors in parentheses, clustered at the school-by-year level. \*\*\*indicates statistically significant at the 1% level, \*\*indicates significant at the 5% level, \*indicates significant at the 10% level.



**Table 2.5. Control Function Estimates of Effect of Information about School-Level Achievement on Separation Probability**

	(1) Full Sample	(2) English	(3) Non-English
"News" Measures 1999 FSA Score*(Yr=2000)	-0.009** (0.005)	-0.013*** (0.005)	0.003 (0.007)
2000 FSA Score*(Yr=2001)	-0.011* (0.006)	-0.011 (0.007)	-0.015 (0.010)
1999-2001 FI Score*(Yr=2002)	-0.035*** (0.010)	-0.031*** (0.011)	-0.046*** (0.015)
2002 FI Score*(Yr=2003)	0.001 (0.007)	0.006 (0.009)	-0.011 (0.009)
"Old News" Measures 1999 FSA Score*(Yr>2000)	-0.001 (0.005)	-0.003 (0.006)	0.006 (0.008)
2000 FSA Score*(Yr>2001)	0.009 (0.007)	0.006 (0.008)	0.016* (0.009)
1999-2001 FI Score*(Yr>2002)	-0.027*** (0.010)	-0.024** (0.011)	-0.032** (0.016)
Current FSA Score	-0.005 (0.004)	-0.002 (0.004)	-0.011* (0.006)
Current FSA Score*(Yr>2001)	0.009* (0.005)	0.003 (0.006)	0.020** (0.009)
Number of Observations	65180	44077	21103
Number of Schools	361	361	360

*Source:* Authors' calculations based on B.C. Ministry of Education enrollment database and auxiliary data.  
*Notes:* "FSA Score" refers to the school-average of FSA Reading and Numeracy scores. "FI Score" refers to the Fraser Institute school score. All scores are normalized to have mean zero and variance one over schools in each year. Additional control variables in these regressions are: main effects for student characteristics (as described in notes to Table 2.4), school proportions of student characteristics (as described in notes to Table 2.4) interacted with dummies for three information regimes (1999/2000, 2000/2001-2001/2002, 2002/2003-2003/2004), the school proportion excused from each FSA reading and numeracy exam interacted with the same "news" and "old news" year dummies as the corresponding test scores, Census characteristics for the student's EA/DA of residence (as described in notes to Table 2.4), and fixed main effects for year and school. See Table 2.A4 in Appendix B for complete coefficient estimates for all three specifications. Robust standard errors in parentheses, clustered at the school-by-year level. \*\*\*indicates statistically significant at the 1% level, \*\*indicates significant at the 5% level, \*indicates significant at the 10% level.

**Table 2.6. Effect of Information about School-level Achievement on Separation Probability, by Home Language and Quartile of Distribution of Neighborhood Income**

	(1)		(2)		(3)	
	All		English		Non-English	
	Top Quartile	Bottom Quartile	Top Quartile	Bottom Quartile	Top Quartile	Bottom Quartile
<i>"News" Measures</i>						
1999 FSA Score*(Yr=2000)	-0.003 (0.009)	-0.018** (0.008)	0.001 (0.010)	-0.038*** (0.011)	-0.022 (0.023)	0.009 (0.012)
2000 FSA Score*(Yr=2001)	-0.000 (0.010)	-0.024** (0.012)	-0.002 (0.011)	-0.033** (0.013)	-0.008 (0.026)	-0.028 (0.019)
1999-2001 FI Score*(Yr=2002)	-0.002 (0.010)	-0.045*** (0.013)	0.006 (0.010)	-0.078*** (0.018)	-0.046* (0.027)	-0.015 (0.018)
2002 FI Score*(Yr=2003)	0.005 (0.011)	-0.031*** (0.012)	0.001 (0.011)	-0.036* (0.018)	0.022 (0.031)	-0.033** (0.014)
<i>"Old News" Measures</i>						
1999 FSA Score*(Yr>2000)	-0.008 (0.009)	0.002 (0.010)	-0.003 (0.010)	-0.006 (0.014)	-0.023 (0.023)	0.012 (0.013)
2000 FSA Score*(Yr>2001)	-0.008 (0.011)	0.012 (0.011)	-0.018 (0.013)	0.024 (0.017)	0.028 (0.027)	0.001 (0.014)
1999-2001 FI Score*(Yr>2002)	-0.016 (0.016)	-0.007 (0.016)	-0.001 (0.015)	-0.027 (0.023)	-0.078 (0.047)	0.019 (0.020)
Current FSA Score	-0.010 (0.007)	0.000 (0.007)	-0.004 (0.008)	0.001 (0.010)	-0.029 (0.019)	0.007 (0.009)
Current FSA Score*(Yr>2001)	0.009 (0.009)	0.013 (0.009)	0.002 (0.009)	0.021 (0.013)	0.045* (0.025)	0.002 (0.013)
Number of Observations	17592	14928	14783	7705	2809	7223
Number of Schools	332	350	303	344	281	289

*Source:* Authors' calculations based on B.C. Ministry of Education enrollment database and auxiliary data.

*Notes:* For details of this specification refer to notes to Table 2.5. Complete estimates of all coefficients are available from the authors on request. Robust standard errors in parentheses, clustered at the school-by-year level. \*\*\* indicates statistically significant at the 1% level, \*\* indicates significant at the 5% level, \* indicates significant at the 10% level.

## 2.10. Appendices

### 2.10.1. Appendix A: Identification via the Control Function Estimation

For illustrative purposes, consider a simplified version of equation (11):

$$(A1) \quad y_{ist} = X'_{ist}\beta_t + \alpha_3 S_{st-1} + \nu_{st} + \varepsilon_{ist}.$$

We have subsumed all observables, including the constant, fixed school and year effects, and student characteristics, into  $X_{ist}$ . We have also omitted longer lags of test scores for expositional clarity, and omitted the current test score,  $S_{st}$ , to illustrate the potential endogeneity problem. We assume observables are exogenous in the sense that  $X_{ist}$  and  $X_{ist-1}$  are uncorrelated with  $\nu_{st}$  and  $\varepsilon_{ist}$ .

Consider the projection of school-average test scores onto contemporaneous observables:

$$(A2) \quad S_{st} = X'_{ist}\gamma + \chi_{st}$$

where  $X_{st}$  has mean zero and is orthogonal to  $X_{ist}$  by construction. It is helpful to think of  $X_{st}$  as a mean-zero “shock” that represents the effect of teachers and other time-varying school-specific unobservables on test scores. Equation (A2) implies  $S_{st-1} = X'_{ist-1}\gamma + \chi_{st-1}$ . Given exogeneity of  $X_{ist-1}$ , lagged test scores are therefore endogenous in (A1) if and only if past shocks to achievement,  $X_{ist-1}$ , are correlated with unobserved heterogeneity in separations ( $\nu_{st}$  or  $\varepsilon_{ist}$ ).

Suppose that shocks to achievement are correlated with unobserved time-varying school-specific heterogeneity in separation probabilities. We represent this via the projection:

$$(A3) \quad \nu_{st} = \kappa\chi_{st} + \xi_{st}$$

where  $E[\xi_{st}] = E[\chi_{st}\xi_{st}] = 0$  by construction. Suppose further that shocks to achievement are persistent, as represented via the projection:

$$(A4) \quad \chi_{st} = \rho\chi_{st-1} + \zeta_{st}$$

where  $\rho \neq 0$  and  $E[\zeta_{st}] = E[\chi_{st-1}\zeta_{st}] = 0$ . It is easy to see that lagged test scores are now endogenous in (A1), because  $E[\chi_{st-1}\nu_{st}] = \kappa\rho Var[\chi_{st-1}] \neq 0$ .

Consider the “long” regression, analogous to (11), which includes current test scores as a control:

$$(A5) \quad y_{ist} = X'_{ist}\beta_t + \alpha_3 S_{st-1} + \alpha_4 S_{st} + \eta_{ist}$$

where  $\eta_{ist}$  is the compound statistical error that arises when (A1) is the DGP.

Proposition:

Under the identifying assumption  $E[\chi_{st-1}\xi_{st} | X_{ist}, S_{st}] = E[\chi_{st-1}\varepsilon_{ist} | X_{ist}, S_{st}] = 0$ , the least squares estimate of  $\alpha_3$  in the long regression (A5) is unbiased.<sup>51</sup> In words, our identifying assumption is that conditional on observables and current test scores, unobserved time-varying school-specific factors that influenced previous cohorts' achievement are only correlated with current-year unmeasured heterogeneity in separations via their persistent effect on achievement.

Proof: *Substituting (A3) into (A1), we can write the DGP as:*

$$(A6) \quad y_{ist} = X'_{ist}\beta_t + \alpha_3 S_{st-1} + \kappa\chi_{st} + \xi_{st} + \varepsilon_{ist}.$$

<sup>51</sup> For equation (11), where the model also includes longer lags of test scores, a more complete statement of our identifying assumption is  $E[\chi_{st-j}\xi_{st} | X_{ist}, S_{st}] = E[\chi_{st-j}\varepsilon_{ist} | X_{ist}, S_{st}] = 0$  for each included lag of test scores  $S_{st-j} = X'_{ist-j}\gamma + \chi_{st-j}$ .

The least squares estimate of  $\alpha_3$  from the long regression (A5) satisfies:

$$E[\hat{\alpha}_3] = \alpha_3 + \kappa V^{-1} E[S_{st-1} \chi_{st} | X_{ist}, S_{st}] + V^{-1} E[S_{st-1} \xi_{st} | X_{ist}, S_{st}] + V^{-1} E[S_{st-1} \varepsilon_{ist} | X_{ist}, S_{st}]$$

where  $V = \text{Var}[S_{st-1} | X_{ist}, S_{st}]$ .  $E[S_{st-1} \chi_{st} | X_{ist}, S_{st}]$  is the covariance between  $S_{st-1}$  and residuals from the regression of  $\chi_{st}$  on  $X_{ist}$  and  $S_{st}$ . These residuals are zero from the definition of  $\chi_{st}$  in (A2), and hence  $E[S_{st-1} \chi_{st} | X_{ist}, S_{st}] = 0$  also. Similarly,

$$E[S_{st-1} \xi_{st} | X_{ist}, S_{st}] = E[(X'_{ist-1} \gamma + \chi_{st-1}) \xi_{st} | X_{ist}, S_{st}] = E[\chi_{st-1} \xi_{st} | X_{ist}, S_{st}] = 0$$

where the second equality follows from exogeneity of  $X_{ist-1}$ , and the final equality is our identifying assumption. An identical argument gives,

$$E[S_{st-1} \varepsilon_{ist} | X_{ist}, S_{st}] = E[(X'_{ist-1} \gamma + \chi_{st-1}) \varepsilon_{ist} | X_{ist}, S_{st}] = E[\chi_{st-1} \varepsilon_{ist} | X_{ist}, S_{st}] = 0$$

and hence  $E[\hat{\alpha}_3] = \alpha_3$ .

The intuition underlying this result is straightforward. Since  $X_{ist-1}$  is exogenous, only the “shock” component of lagged test scores,  $\chi_{st-1}$ , is potentially endogenous. Equation (A2) implies that  $S_{st}$  is a valid control function for  $\chi_{st}$ . Thus the only potential source of endogeneity in the long regression is conditional covariation between  $\chi_{st-1}$  and unobserved heterogeneity that is orthogonal to current test scores, i.e.,  $\xi_{st}$  and the component of  $\varepsilon_{ist}$  that is orthogonal to  $S_{st}$ . Our identifying assumption rules this out.

Our identifying assumption would be violated under the following conditions. First,  $E[\chi_{st-1} \xi_{st} | X_{ist}, S_{st}] \neq 0$  if there are time-varying unobserved school-specific factors (including school-level policy and teacher quality) that are correlated with lagged test scores and current separations, *but uncorrelated with current test scores* (and  $X_{ist}$ ). Similarly,  $E[\chi_{st-1} \varepsilon_{ist} | X_{ist}, S_{st}] \neq 0$  if there are unobserved student characteristics that are correlated with lagged test scores and current separations, *but uncorrelated with current test scores* (and  $X_{ist}$ ). It is difficult to construct realistic examples where these conditions

would arise. We nevertheless implement several falsification tests (see the Results section and Appendix B) to assess the validity of our identifying assumption, and find no systematic evidence to the contrary.

## 2.10.2. Appendix B: Additional Tables

**Table 2.A1. Sample Means of Control Variables**

	(1) Sample Mean or Proportion	(2) Sample Standard Deviation
<i>Individual Characteristics</i>		
Male	0.506	0.500
Aboriginal	0.047	0.211
Non-English Home Language	0.324	0.468
Disabled	0.036	0.187
Gifted	0.017	0.128
Enrolled in ESL Program	0.307	0.461
Changed Schools Prior to Grade 4	0.348	0.476
Own FSA Reading Score	0.050	0.964
Own FSA Numeracy Score	0.062	0.983
<i>School Characteristics</i>		
Proportion Excused from FSA Reading	0.084	0.069
Proportion Excused from FSA Numeracy	0.086	0.070
Proportion Male	0.514	0.074
Proportion Aboriginal	0.038	0.048
Proportion Non-English Home Language	0.323	0.266
Proportion Disabled	0.060	0.045
Proportion Enrolled in ESL Program	0.250	0.245
Proportion Enrolled in French Immersion	0.062	0.168
<i>Cost of Changing Schools</i>		
Enrolled in French Immersion	0.068	0.251
Number of Public Schools Nearby	2.60	1.42
Number of Private Schools Nearby	8.64	6.05
Travel Distance to School (km)	1.19	2.20
<i>Census Characteristics</i>		
Mean Household Income / \$1000	64.9	25.5
Proportion Visible Minority	0.329	0.257
Proportion One-Parent Families	0.146	0.088
Proportion of those Aged 25+ Unemployed	0.065	0.052
Average Value of Dwelling / \$1000	292	133
Proportion Dwellings Owned	0.717	0.211
Proportion Moved Last Year	0.159	0.090
Proportion Moved in Last 5 Years	0.484	0.160
Proportion Less than Grade 9 Education	0.072	0.065
Proportion Some High School	0.185	0.082
Proportion with High School Diploma	0.131	0.051
Proportion with BA or higher	0.175	0.117
Proportion Immigrant	0.337	0.168

Source: Authors' calculations based on B.C. Ministry of Education enrollment database and auxiliary data.

Notes: "Nearby" is defined as a circle with radius equal to the 75<sup>th</sup> percentile of travel distance to school.

**Table 2.A2. Distribution of School Achievement Measures**

	Mean	Std. Dev	Correlation						
			School-Average FSA Score				Fraser Institute Score		
			1999 / 2000	2000 / 2001	2001 / 2002	2002 / 2003	3 Year Avg.	2001 / 2002	2002 / 2003
<i>Public Schools</i>									
1999/2000 FSA	0	1	1						
2000/2001 FSA	0	1	0.708	1					
2001/2002 FSA	0	1	0.637	0.672	1				
2002/2003 FSA	0	1	0.563	0.619	0.665	1			
3 Year Avg. FI	0	1	0.790	0.808	0.784	0.669	1		
2001/2002 FI	0	1	0.616	0.639	0.813	0.619	0.886	1	
2002/2003 FI	0	1	0.667	0.632	0.661	0.801	0.782	0.713	1

Source: Authors' calculations based on B.C. Ministry of Education enrollment database and auxiliary data.  
 Notes: "FSA" refers to the school-average of FSA reading and numeracy scores. "FI Score" refers to the Fraser Institute school score. All scores are normalized to have mean zero and variance one over schools in each year.



**Table 2.A3. Complete Coefficient Estimates, Difference-in-Differences Estimator**

	(1) Full Sample	(2) English	(3) Non-English
Lagged Score	-0.003 (0.004)	-0.003 (0.004)	-0.001 (0.007)
Lagged Score*(Yr=2000)	-0.007 (0.004)	-0.010** (0.005)	0.003 (0.008)
Yr = 2000	-0.047* (0.024)	-0.073** (0.028)	0.033 (0.050)
Proportion Disabled	0.015 (0.060)	0.059 (0.079)	-0.093 (0.102)
Proportion Non-English Home Language	0.017 (0.045)	0.062 (0.061)	-0.107 (0.070)
Proportion Aboriginal	-0.133 (0.087)	-0.077 (0.106)	-0.330** (0.130)
Proportion Enrolled in ESL Program	-0.002 (0.056)	0.042 (0.076)	-0.027 (0.077)
Proportion Male	-0.046 (0.033)	-0.127*** (0.041)	0.165*** (0.062)
Proportion Enrolled in French Immersion	-0.165** (0.072)	-0.122 (0.080)	-0.356** (0.154)
Proportion Disabled*(Yr≥2000)	-0.029 (0.079)	0.097 (0.108)	-0.291*** (0.110)
Proportion Non-English*(Yr≥2000)	0.071** (0.034)	0.092** (0.043)	0.028 (0.061)
Proportion Aboriginal*(Yr≥2000)	0.022 (0.073)	0.016 (0.084)	0.088 (0.126)
Proportion Enrolled in ESL Program*(Yr≥2000)	-0.052 (0.037)	-0.057 (0.053)	-0.025 (0.058)
Proportion Male*(Yr≥2000)	0.060 (0.045)	0.096* (0.053)	-0.047 (0.090)
Proportion French Immersion*(Yr≥2000)	0.027* (0.015)	0.026 (0.018)	0.076** (0.036)
Proportion Excused from FSA	-0.040 (0.037)	-0.113** (0.053)	0.005 (0.046)
Non-English Home Language	0.011 (0.008)	0.000 (0.000)	0.000 (0.000)
Aboriginal	0.074*** (0.010)	0.073*** (0.010)	0.055 (0.049)
Enrolled in ESL Program	-0.019** (0.009)	-0.041*** (0.013)	-0.003 (0.011)
Male	-0.002 (0.004)	-0.003 (0.004)	-0.004 (0.007)
Disabled	0.025** (0.011)	0.021* (0.012)	0.032 (0.022)
Gifted	0.000 (0.011)	0.004 (0.013)	0.002 (0.023)
Changed Schools Prior to Grade 4	0.064***	0.072***	0.041***

	(0.004)	(0.005)	(0.007)
Own FSA Reading Score	-0.005*	-0.006*	-0.005
	(0.003)	(0.003)	(0.005)
Own FSA Numeracy Score	-0.006**	-0.007**	-0.002
	(0.002)	(0.003)	(0.005)
Mean Household Income / \$1000	-0.000*	-0.000	-0.001
	(0.000)	(0.000)	(0.001)
SE of Mean Household Income / \$1000	0.001	0.000	-0.001
	(0.001)	(0.001)	(0.002)
Proportion Visible Minority	0.001	0.006	0.011
	(0.030)	(0.038)	(0.052)
Proportion One-Parent Families	0.014	-0.017	0.071
	(0.034)	(0.042)	(0.059)
Proportion of those Aged 25+ Unemployed	0.015	0.042	0.001
	(0.054)	(0.069)	(0.087)
Average Value of Dwelling / \$1000	0.000	0.000	0.000
	(0.000)	(0.000)	(0.000)
Proportion of Dwellings Owned	-0.016	-0.031	0.012
	(0.017)	(0.021)	(0.031)
Proportion Moved Last Year	0.047	0.054	0.008
	(0.030)	(0.040)	(0.052)
Proportion Moved in Last 5 Years	0.001	0.018	-0.032
	(0.021)	(0.024)	(0.044)
Proportion Less than Grade 9 Education	0.048	0.062	-0.029
	(0.069)	(0.093)	(0.109)
Proportion Some High School	0.013	0.028	-0.066
	(0.044)	(0.057)	(0.079)
Proportion with High School Diploma	-0.010	0.030	-0.135
	(0.051)	(0.062)	(0.093)
Proportion with Bachelor's or Higher	0.172***	0.199***	0.142
	(0.046)	(0.056)	(0.088)
Proportion Immigrant	-0.009	-0.027	-0.002
	(0.041)	(0.049)	(0.082)
Travel Distance to School (km)	0.005***	0.005***	0.003
	(0.001)	(0.001)	(0.002)
Enrolled in French Immersion	-0.019*	-0.016	-0.033
	(0.010)	(0.011)	(0.035)
Number of Public Schools Nearby	-0.002	-0.004	0.002
	(0.002)	(0.002)	(0.003)
Number of Private Schools Nearby	0.001	0.001	-0.001
	(0.001)	(0.002)	(0.002)
Constant	0.078**	0.084*	0.138*
	(0.037)	(0.044)	(0.078)

Notes: This table reports all coefficient estimates for the specifications reported in columns 1-3 of Table 2.4. Robust standard errors in parentheses, clustered at the school-by-year level. \*\*\*indicates statistically significant at the 1% level, \*\*indicates significant at the 5% level, \*indicates significant at the 10% level.

**Table 2.A4. Complete Coefficient Estimates, Control Function Estimator**

	(1)	(2)	(3)
	Full Sample	English	Non-English
1999 FSA Score*(Yr=2000)	-0.009** (0.005)	-0.013*** (0.005)	0.003 (0.007)
2000 FSA Score*(Yr=2001)	-0.011* (0.006)	-0.011 (0.007)	-0.015 (0.010)
1999-2001 FI Score*(Yr=2002)	-0.035*** (0.010)	-0.031*** (0.011)	-0.046*** (0.015)
2002 FI Score*(Yr=2003)	0.001 (0.007)	0.006 (0.009)	-0.011 (0.009)
1999 FSA Score*(Yr>2000)	-0.001 (0.005)	-0.003 (0.006)	0.006 (0.008)
2000 FSA Score*(Yr>2001)	0.009 (0.007)	0.006 (0.008)	0.016* (0.009)
1999-2001 FI Score*(Yr>2002)	-0.027*** (0.010)	-0.024** (0.011)	-0.032** (0.016)
Current FSA Score	-0.005 (0.004)	-0.002 (0.004)	-0.011* (0.006)
Current FSA Score*(Yr>2001)	0.009* (0.005)	0.003 (0.006)	0.020** (0.009)
Proportion Male	-0.047 (0.030)	-0.083** (0.035)	0.048 (0.051)
Proportion Disabled	0.044 (0.064)	0.113 (0.069)	-0.079 (0.098)
Proportion Non-English Home Language	-0.039 (0.041)	0.026 (0.047)	-0.122** (0.056)
Proportion Aboriginal	-0.100 (0.070)	-0.067 (0.088)	-0.172 (0.109)
Proportion Enrolled in ESL Program	0.016 (0.043)	0.030 (0.053)	0.016 (0.053)
Proportion Enrolled in French Immersion	0.014 (0.040)	0.009 (0.042)	0.066 (0.107)
Proportion Disabled*(Yr ≥ 2000)	0.048 (0.079)	-0.001 (0.097)	0.110 (0.111)
Proportion Non-English*(Yr ≥ 2000)	0.038 (0.038)	-0.037 (0.047)	0.125** (0.053)
Proportion Aboriginal*(Yr ≥ 2000)	0.022 (0.086)	-0.026 (0.106)	0.071 (0.125)
Proportion Enrolled in ESL Program*(Yr ≥ 2000)	-0.044 (0.040)	0.017 (0.049)	-0.113** (0.054)
Proportion Male*(Yr ≥ 2000)	0.061 (0.042)	0.106** (0.050)	-0.037 (0.075)
Proportion French Immersion*(Yr ≥ 2000)	0.017 (0.019)	0.025 (0.022)	-0.015 (0.037)
Proportion Disabled*(Yr ≥ 2002)	-0.043	0.051	-0.199

	(0.099)	(0.125)	(0.131)
Proportion Non-English*(Yr≥2002)	0.050	0.120**	-0.034
	(0.046)	(0.058)	(0.057)
Proportion Aboriginal*(Yr≥2002)	0.184	0.188	0.346**
	(0.134)	(0.160)	(0.165)
Proportion Enrolled in ESL Program*(Yr≥2002)	-0.060	-0.115**	-0.002
	(0.044)	(0.058)	(0.055)
Proportion Male*(Yr≥2002)	-0.059	-0.023	-0.141
	(0.074)	(0.091)	(0.099)
Proportion French Immersion*(Yr≥2002)	-0.047***	-0.034*	-0.095**
	(0.017)	(0.018)	(0.044)
Prop. Excused from 1999 Reading FSA*(Yr=2000)	0.052	0.078	-0.038
	(0.246)	(0.217)	(0.570)
Prop. Excused from 2000 Reading FSA*(Yr=2001)	0.003	-0.015	0.186
	(0.208)	(0.255)	(0.326)
Prop. Excused from 2001 Reading FSA*(Yr=2002)	-0.234*	-0.266**	-0.162
	(0.127)	(0.132)	(0.223)
Prop. Excused from 2002 Reading FSA*(Yr=2003)	-0.020	0.026	-0.137
	(0.081)	(0.100)	(0.141)
Prop. Excused from 1999 Numeracy FSA*(Yr=2000)	-0.049	-0.062	-0.002
	(0.275)	(0.235)	(0.613)
Prop. Excused from 2000 Numeracy FSA*(Yr=2001)	-0.036	-0.002	-0.228
	(0.201)	(0.248)	(0.318)
Prop. Excused from 2001 Numeracy FSA*(Yr=2002)	0.156	0.210*	0.048
	(0.112)	(0.123)	(0.189)
Prop. Excused from 2002 Numeracy FSA*(Yr=2003)	-0.084	-0.200	0.064
	(0.107)	(0.123)	(0.157)
Prop. Excused from 1999 Reading FSA*(Yr>2000)	0.054	0.132	-0.269
	(0.202)	(0.172)	(0.478)
Prop. Excused from 2000 Reading FSA*(Yr>2001)	-0.003	-0.224	0.473*
	(0.181)	(0.220)	(0.268)
Prop. Excused from 2001 Reading FSA*(Yr>2002)	-0.141	0.009	-0.333*
	(0.119)	(0.142)	(0.174)
Prop. Excused from 1999 Numeracy FSA*(Yr>2000)	0.107	0.055	0.388
	(0.231)	(0.190)	(0.526)
Prop. Excused from 2000 Numeracy FSA*(Yr>2001)	-0.059	0.143	-0.490*
	(0.175)	(0.213)	(0.265)
Prop. Excused from 2001 Numeracy FSA*(Yr>2002)	0.164*	0.054	0.347**
	(0.094)	(0.108)	(0.150)
Year=2000	-0.009	-0.011	-0.001
	(0.006)	(0.007)	(0.011)
Year=2001	-0.037	-0.052*	-0.004
	(0.024)	(0.029)	(0.041)
Year=2002	-0.022	-0.039	0.020
	(0.026)	(0.031)	(0.042)
Year=2003	0.008	-0.037	0.112*
	(0.040)	(0.046)	(0.058)
Non-English Home Language	0.009*	0.000	0.000

	(0.005)	(0.000)	(0.000)
Aboriginal	0.069***	0.066***	0.077**
	(0.007)	(0.008)	(0.037)
Enrolled in ESL Program	-0.013**	-0.034***	0.005
	(0.005)	(0.008)	(0.007)
Male	-0.001	-0.002	-0.002
	(0.002)	(0.003)	(0.004)
Disabled	0.025***	0.025***	0.010
	(0.007)	(0.008)	(0.015)
Gifted	0.005	0.008	-0.002
	(0.008)	(0.009)	(0.017)
Changed Schools Prior to Grade 4	0.060***	0.066***	0.046***
	(0.003)	(0.004)	(0.005)
Own FSA Reading Score	-0.004**	-0.005**	-0.002
	(0.002)	(0.002)	(0.003)
Own FSA Numeracy Score	-0.006***	-0.009***	-0.003
	(0.002)	(0.002)	(0.003)
Mean Household Income / \$1000	-0.000*	-0.000*	-0.000
	(0.000)	(0.000)	(0.000)
SE of Mean Household Income / \$1000	0.000	0.001	-0.000
	(0.000)	(0.000)	(0.001)
Proportion Visible Minority	0.032*	0.034	0.036
	(0.016)	(0.021)	(0.027)
Proportion One-Parent Families	0.002	0.009	-0.015
	(0.018)	(0.021)	(0.032)
Proportion of those Aged 25+ Unemployed	-0.000	-0.026	0.051
	(0.032)	(0.039)	(0.051)
Average Value of Dwelling	0.000	0.000	0.000
	(0.000)	(0.000)	(0.000)
Proportion of Dwellings Owned	-0.013	-0.010	-0.021
	(0.010)	(0.013)	(0.018)
Proportion Moved Last Year	0.039**	0.033	0.037
	(0.020)	(0.025)	(0.033)
Proportion Moved in Last 5 Years	-0.005	0.002	-0.017
	(0.012)	(0.013)	(0.023)
Proportion Less than Grade 9 Education	0.013	0.038	-0.013
	(0.036)	(0.046)	(0.056)
Proportion Some High School	0.044*	0.048	0.005
	(0.026)	(0.031)	(0.043)
Proportion with High School Diploma	0.010	0.023	-0.028
	(0.027)	(0.032)	(0.051)
Proportion with Bachelor's or Higher	0.062***	0.059**	0.068
	(0.023)	(0.027)	(0.041)
Proportion Immigrant	-0.025	-0.029	-0.029
	(0.022)	(0.027)	(0.039)
Travel Distance to School (km)	0.005***	0.005***	0.003**
	(0.001)	(0.001)	(0.001)
Enrolled in French Immersion	-0.014	-0.006	-0.038**

	(0.009)	(0.010)	(0.018)
Number of Public Schools Nearby	-0.000	-0.000	0.000
	(0.001)	(0.001)	(0.002)
Number of Private Schools Nearby	-0.001	-0.001	-0.002
	(0.001)	(0.001)	(0.001)
Constant	0.088***	0.070**	0.130**
	(0.025)	(0.028)	(0.054)

Source: Authors' calculations based on B.C. Ministry of Education enrollment database and auxiliary data.  
Notes: This table reports all coefficient estimates for the specifications reported in Table 2.5 in the main text. Robust standard errors in parentheses, clustered at the school-by-year level. \*\*\*indicates statistically significant at the 1% level, \*\*indicates significant at the 5% level, \*indicates significant at the 10% level.

**Table 2.A5. Robustness Checks for Control Function Estimator**

	(1)	(2)	(3)	(4)	(5)
	English only			Fraser Institute Rankings	
	All	Without Aboriginals	Without Fr.Imm.	English	Non- English
1999 FSA Score*(Yr=2000)	-0.013*** (0.005)	-0.011** (0.005)	-0.014*** (0.005)	-0.013** (0.005)	0.003 (0.007)
2000 FSA Score*(Yr =2001)	-0.011 (0.007)	-0.008 (0.008)	-0.010 (0.008)	-0.010 (0.007)	-0.015 (0.010)
1999-2001 Mean FI Score*(Yr =2002)	-0.031*** (0.011)	-0.030*** (0.011)	-0.027*** (0.010)		
2002 FI Score*(Yr=2003)	0.006 (0.009)	0.008 (0.009)	0.007 (0.009)		
1999-2001 Mean FI Ranking*(Yr =2002)				0.027** (0.012)	0.048*** (0.015)
2002 FI Ranking*(Yr =2003)				-0.005 (0.007)	0.010 (0.008)
1999 FSA Score*(Yr >2000)	-0.003 (0.006)	-0.006 (0.006)	-0.005 (0.006)	-0.005 (0.006)	0.006 (0.008)
2000 FSA Score*(Yr >2001)	0.006 (0.008)	0.010 (0.008)	0.007 (0.008)	0.005 (0.008)	0.018* (0.010)
1999-2001 Mean FI Score*(Yr>2002)	-0.024** (0.011)	-0.026** (0.011)	-0.022* (0.011)		
1999-2001 Mean FI Rank*(Yr >2002)				0.018* (0.010)	0.033** (0.015)
Current Mean FSA Score	-0.002 (0.004)	-0.004 (0.005)	-0.003 (0.005)	-0.001 (0.004)	-0.011* (0.006)
Current Mean FSA Score*(Yr>2001)	0.003 (0.006)	0.002 (0.006)	0.002 (0.006)	0.001 (0.006)	0.020** (0.008)
Number of Observations	44077	41149	40182	44077	21103
Number of Schools	361	361	357	361	360

Source: Authors' calculations based on B.C. Ministry of Education enrollment database and auxiliary data. Notes: Column (1) reproduces estimates from column (2) of Table 2.5 in the main text. Column (2) excludes Aboriginal students and column (3) excludes French Immersion students. Columns (4) and (5) replace the school's Fraser Institute score with the school's rank based on the Fraser Institute score. "FSA Score" refers to the school-average of FSA reading and numeracy scores. "FI Score" is the Fraser Institute school score, and "FI Rank" is the school's published Fraser Institute ranking based on FI Scores. Note that larger values of FSA Score and FI Score indicate better performance, whereas larger values of FI Rank indicate worse performance. See notes to Table 2.5 in the main text for additional control variables. Robust standard errors in parentheses, clustered at the school-by-year level. \*\*\* indicates statistically significant at the 1% level, \*\* indicates significant at the 5% level, \* indicates significant at the 10% level.

**Table 2.A6. Falsification Test 1 for Control Function Estimator**

	(1)	(2)	(3)
	Full Sample	English	Non-English
<i>False "News" Measures</i> 2000 FSA Score*(Yr=2000)	-0.005 (0.005)	-0.010* (0.006)	0.008 (0.007)
2001 FSA Score*(Yr=2001)	-0.009 (0.008)	-0.009 (0.008)	-0.011 (0.010)
2002 FSA Score*(Yr=2002)	-0.011 (0.007)	-0.012 (0.008)	-0.005 (0.011)
2003 FSA Score*(Yr=2003)	-0.012 (0.007)	-0.015* (0.008)	-0.001 (0.012)
<i>False "Old News" Measures</i> 2000 FSA Score*(Yr>2000)	-0.001 (0.006)	-0.004 (0.007)	0.005 (0.008)
2001 FSA Score*(Yr>2001)	-0.001 (0.005)	-0.003 (0.006)	-0.001 (0.006)
2002 FSA Score*(Yr>2002)	0.005 (0.008)	0.009 (0.009)	-0.002 (0.008)
Current Mean FSA Score	0.007 (0.005)	0.010* (0.006)	0.000 (0.009)
Number of Observations	65180	44077	21103
Number of Schools	361	361	360

Source: Authors' calculations based on B.C. Ministry of Education enrollment database and auxiliary data.

Notes: These estimates replicate the specifications reported in Table 2.5, except that all genuine "news" measures (based on lagged test scores that parents could observe) have been replaced with false "news" measures based on contemporaneous test scores (which parents could not observe until the following school year). All genuine "old news" measures have also been replaced with corresponding false measures. The interaction between the current mean FSA score and Year>2001 was dropped because of collinearity with the false news measures. Given the high degree of inter-temporal correlation between school-average test scores (see Table 2.A2 in this Appendix), it is not surprising that some estimates in column (2) are weakly statistically significant. On the whole, however, there is little evidence of a systematic relationship between false "news" and separations; and the overall pattern of results differs substantially from those reported in Table 2.5. See notes to Table 2.5 for details of specification. Complete coefficient estimates for these specifications are available from the authors on request. Robust standard errors in parentheses, clustered at the school-by-year level. \*\*\*indicates statistically significant at the 1% level, \*\*indicates significant at the 5% level, \*indicates significant at the 10% level.



**Table 2.A7. Falsification Test 2 for Control Function Estimator**

	(1)	(2)	(3)
	Full Sample	English	Non-English
<i>False "News" Measures</i> 2001 FSA Score*(Yr=2000)	-0.007 (0.004)	-0.010* (0.005)	0.003 (0.006)
2002 FSA Score*(Yr=2001)	-0.004 (0.005)	-0.007 (0.006)	0.004 (0.007)
2003 FSA Score*(Yr=2002)	-0.010* (0.006)	-0.014** (0.007)	-0.003 (0.009)
<i>False "Old News" Measures</i> 2001 FSA Score*(Yr>2000)	-0.008 (0.005)	-0.010 (0.007)	-0.006 (0.007)
2002 FSA Score*(Yr>2001)	0.002 (0.005)	-0.001 (0.007)	0.009 (0.008)
Current Mean FSA Score	0.003 (0.003)	0.006 (0.004)	-0.002 (0.005)
Number of Observations	52381	35900	16481
Number of Schools	361	361	360

Source: Authors' calculations based on B.C. Ministry of Education enrollment database and auxiliary data. Notes: These estimates replicate the specifications reported in Table 2.5, except that all genuine "news" measures (based on lagged test scores that parents could observe) have been replaced with false "news" measures based on future test scores (which parents could not observe). All genuine "old news" measures have also been replaced with corresponding false measures. The interaction between the current mean FSA score and Year>2001 was dropped because of collinearity with the false news measures. Because of the structure of false news measures, and because we have no 2004 FSA scores, this specification was estimated for 1999/2000-2002/2003 only. Given the high degree of inter-temporal correlation between school-average test scores (see Table 2.A2 in this Appendix), it is not surprising that some reported estimates are statistically significant. On the whole, however, there is little evidence of a systematic relationship between false "news" and separations; and the overall pattern of results differs substantially from those reported in Table 2.5. See notes to Table 2.5 for details of specification. Complete coefficient estimates for these specifications are available from the authors on request. Robust standard errors in parentheses, clustered at the school-by-year level. \*\*\*indicates statistically significant at the 1% level, \*\*indicates significant at the 5% level, \*indicates significant at the 10% level.

### **2.10.3. Appendix C: Data Appendix**

#### **2.10.3.1. Control Variables**

Controls for individual characteristics include an indicator of whether the student separated from their school in an earlier school year, and indicators for gender, Aboriginal identity, language spoken at home (any language besides English), disability, giftedness, ESL status, and the student's own FSA exam score. We also control for a set of socioeconomic characteristics of the Census Enumeration or Dissemination Area (EA or DA, respectively) in which the student resides as proxies for unobserved student background characteristics. Specifically, we control for the proportion of household heads in the EA/DA who immigrated to Canada in the previous five years; whose education level was less than grade 9, without a high school diploma, with a high school diploma, and with a bachelor's degree or higher (the omitted category is those with more than high school but less than a bachelor's degree); who are visible minority; who are single parents; who moved into the EA or DA in the last year or in the last five years; and the unemployment rate among those over age 25, the average dwelling value, average household income, and the fraction who own their dwelling. Details of the construction of these variables are provided below.

Controls for school characteristics include the proportion of grade 4 students who are Aboriginal, speak a language other than English at home, are male, are disabled, are in an ESL program, were excused from the reading or numeracy test, or are enrolled in French Immersion. Finally, we include several proxies for students' cost of changing schools: their travel distance to school, the number of public and private schools within the 75<sup>th</sup> percentile of the distribution of student travel distance to school, and an indicator for attending a French Immersion program (because this program is offered in a limited set of schools). French Immersion programs, which are the most popular form of magnet programs in the Lower Mainland, provide French-only instruction to non-francophone students.

#### **2.10.3.2. Coding of Neighborhood Characteristics**

Neighborhood characteristics are based on public-use aggregates of the Census of Population "long form," administered by Statistics Canada to one in five households in 1996 and 2001. The lowest level of geography for which Statistics Canada produced

aggregate statistics based on the 1996 Census is an Enumeration Area (EA). Statistics based on the 2001 Census were produced at the Dissemination Area (DA) level. EAs are geographic areas designated for the *collection* of Census data. Prior to the 2001 Census, EAs were used for both Census data collection and dissemination. In the 2001 Census, they were replaced by DAs for dissemination purposes. In the 1996 Census, EAs were composed of one or more neighboring blocks containing between 125 and 440  *dwellings* (in rural and urban areas, respectively). In the 2001 Census, DAs were composed of one or more neighboring blocks with a population of 400 to 700  *persons*. These definitions are sufficiently similar for our purposes.

EA/DA-level Census characteristics were integrated with our enrollment data via students' residential postal code in each year. The integrated EA/DA characteristics are based on the most recently administered Census for each year of our sample. We link postal codes and EAs/DAs using Statistics Canada's Postal Code Conversion File (PCCF). The PCCF contains a complete longitudinal correspondence between postal codes and EAs/DAs (postal codes are occasionally retired and subsequently recycled). Postal codes are smaller than EAs/DAs and usually lie entirely within an EA/DA. In cases where postal code boundaries span multiple EAs/DAs, we use the PCCF's Single Link Indicator (which identifies the best link to an EA/DA) to link to a unique EA/DA.

In a small number of cases, we were unable to assign EA/DA-level characteristics to residential postal codes. This arose when residential postal codes did not appear in the PCCF (most likely due to mis-reported postal codes), or when EA/DA-level characteristics were suppressed by Statistics Canada for confidentiality reasons. Overall, these cases comprised about 1 percent of grade 4 students in the enrollment database.

### **2.10.3.3. Coding of Distance and School Density Measures**

Our measures of the distance between students' residence and the school they attended are based on reported postal codes. We obtained postal codes for all schools attended by grade 4 students who met our other sample restrictions from public sources (most notably, school and district websites). We used the PCCF to assign a latitude and longitude to each postal code in each year, and calculated the great circle distance (in km) between the student's residence and schools. For each residential postal code in

each year, we then calculated the number of active public and private schools within a circle centered on the residential postal code and with radius equal to the 75<sup>th</sup> percentile of in-sample travel distance to public and private schools, respectively.

#### **2.10.3.4. Coding of Other Key Variables**

In all regressions, the reference category for home language is students who always report speaking English at home. Students are coded as speaking a non-English language at home if they report speaking a language other than English at home in any year between kindergarten and grade 5. Similarly, students are coded as Aboriginal, disabled, or gifted if they ever report that status. Students are coded as ESL if they are designated as such in the current school year. Annual school-by-grade averages of these variables were computed by aggregating the student-level data.

#### **2.10.3.5. Missing Data and Other Sample Restrictions**

As reported in the main text, we restrict our analysis sample to students who entered kindergarten at a Lower Mainland school between 1995/1996 and 1999/2000, subsequently made regular progress through grade 5 at Lower Mainland schools, and were enrolled in grade 4 at a public school between 1999/2000 and 2003/2004. By regular progress, we mean students advanced through each grade level with their entry cohort, and were observed attending a school in BC in each year from kindergarten through grade 5. We excluded 6,681 observations where a student did not progress through the grades along with her cohort, and we excluded 64 observations where the measured distance between the student's residence and the school they attended exceeded 50km (since it is likely that this distance indicates measurement error in the postal code). Our sample comprises 106,344 Grade 4 students after applying these sample restrictions. Of these, 41,164 additional observations were excluded because of missing data. The most commonly missing data items, including those described elsewhere in this Appendix, were:

- the Fraser Institute school score/ranking, because the Fraser Institute only generated scores for schools with at least 15 students enrolled in both grade 4 and grade 7, and because two public school districts (Coquitlam and Chilliwack) were excluded from the 2003 report card (the three-year average Fraser Institute score is missing for 22,277 observations, the Fraser Institute

score based on the 2001/2002 exam is missing for 19,529 observations, and the score based on the 2002/2003 exam is missing for 4,313 observations);

- neighborhood characteristics, as described above (876 observations); and
- students' own FSA exam result (6,849 observations were missing either a reading or numeracy score).

### 3. Noise or News? Learning About the Content of Test-Based School Achievement Measures

#### 3.1. Introduction

Proponents of school choice argue that the structure of the public educational system – where education is mainly provided by government with substantial monopoly power and largely no competition – leaves educational consumers with limited choice among schools. They further suggest that this may result in a disconnect between school quality and parents' preferences. There is a growing literature in economics that suggests that expanding school choice could improve educational outcomes by increasing disadvantaged children's access to high quality schools, and by causing underperforming schools to become more effective or to shrink as families "vote with their feet" (Friedman 1955; Becker 1995; Hoxby 2003; Belfield and Levin 2003).<sup>1</sup> These ideas have gained strong currency in education policy circles, leading to policy innovations such as open enrollment systems, magnet and charter schools, private school vouchers, and expanded public school choice for students in poorly performing schools.

One suggested approach to make these policies more effective is to increase parents' access to information about school quality and performance. A growing body of evidence suggests that information about school-level achievement affects behavior in ways that may have real consequences for educational outcomes (Hastings et al. 2007; Hastings and Weinstein 2008). For example, Friesen, Javdani, Smith and Woodcock (2012) find that the public release of information about school-level achievement had a substantial effect on the inter-school mobility of Grade 4 public school students.

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<sup>1</sup> However, it should be also mentioned that there are some concerns regarding these kinds of policies. For instance, some people argue that issues of equity will be passed over in the push for school choice, causing at-risk students to fall further behind.

However it remains an open question whether measures of school-level achievement actually provide parents with meaningful information about school quality, or whether they are too imprecise to do so.

A growing body of literature (Kane and Staiger 2002; Mizala, Romaguera and Urquiola 2007), suggests that there are two sources of transitory variation in school average test scores. The first is sampling variation which is purely a statistical phenomenon. It is the variation in a school's test score arising from random year-to-year variation in the composition of its student body. In this context, we can think of different cohorts of students entering a school over time as random draws from a local population feeding that school. The magnitude of sampling variation depends on school size: it is decreasing in the number of students who write the test. The second source of transitory variation is idiosyncratic factors that generate non-persistent differences in schools' mean test scores; for example a school-wide illness at the time of the exam, existence of a few disruptive students in a class, special chemistry between a teacher and a cohort of students, inclement weather, etc. Throughout the paper, I refer to this second source of transitory variance as "other transitory factors" to distinguish it from sampling variation.

It is well-understood that mobility decisions are costly. Cullen et al. (2000) find little evidence that students systematically achieve higher school quality (measured by value-added of schools to student outcomes) by choosing a non-neighborhood school. Hanushek et al. (1999) find that family-initiated moves with district changes, which are largely the consequence of parents changing district in pursuit of a higher quality school, reduce achievement growth. They also find that mobility generates negative externalities for students who attend schools with high turnover rates. Together, these results suggest that basing school choice decisions on highly transitory information about school-average achievement might make many students worse off.

A related literature shows that information about school-average achievement affects real estate prices (Figlio and Lucas 2004; Fiva and Kirkebøen 2008; and others). Again, if test-based measures of school-average achievement are highly transitory, then making costly location decisions to obtain access to (currently) high-achieving schools

could generate a lot of costly churning in the real estate market, making families worse off.

I investigate the content of published information about schools' average test scores to determine whether they provide parents with meaningful information about persistent or permanent inter-school differences in achievement and school quality. I extend the work of Kane and Staiger (2002) with a more rigorous statistical model that shows how one can separately measure the effect of sampling variation and other transitory factors on the cross-sectional variance of school mean test scores. I find that sampling variation and one-time mean reverting shocks are a significant source of observed variation in schools' average test scores.

### **3.2. Previous Literature**

Not much is known about the statistical properties of school-level measures of test-based achievement. Kane and Staiger (2001) find that test-based elementary school rankings in North Carolina resemble a lottery, and argue that small within-school sample size is the main cause. They decompose the variance of school-level test scores and find that gain scores tend to have less signal variation and more variation due to non-persistent factors than test score levels. Therefore, they caution against the use of gain scores in evaluating schools' or teachers' performance. They also find little evidence that schools with significant improvement in their test scores over time improved on any measures of student engagement. In their 2002 study, Kane and Staiger estimate that 14 to 15 percent of the variation in 4<sup>th</sup> grade math and reading test scores for an average school in their sample is due to sampling variation. They also find that 50 to 80 percent of the variance in the change in 4<sup>th</sup> grade mean test scores is due to nonpersistent factors.

Mizala, Romaguera and Urquiola (2007) find evidence that test-based rankings mostly reflect socioeconomic status. They also argue that the more correlated are test-based achievement and socioeconomic status, the lower is the year-to-year volatility in rankings based on test-based achievement. Finally, using evidence from Chile's P-900 program, Chay, McEwan and Urquiola (2005) show that noise and mean-reverting



shocks in schools' test scores complicate evaluation of policies to improve schools' quality. They find that for a median-sized school, 33 percent and 21 percent of the variance in language and math scores, respectively, are due to transitory factors. They argue that such noise in mean test scores might limit the ability to identify "good" schools from "bad" schools.

### **3.3. Institutional Background and Data**

#### **3.3.1. Testing and Information**

Since the 1999/2000 school year, all public and provincially-funded private schools in the province of British Columbia (B.C.) have been required to administer standardized Foundation Skills Assessment (FSA) exams to students in Grades 4 and 7 in May of each year. Students are examined in Reading Comprehension, Writing, and Numeracy. The FSA exams do not contribute to students' academic records and play no role in grade completion, and there are no financial incentives for teachers or schools related to student performance.

The Ministry of Education first provided individual and provincial-, district-, and school-level FSA exam results to schools in fall 2000, and instructed them to share the information with parents upon request (B.C. Ministry of Education 2000). The results of the 1999/2000 and 2000/2001 FSA exams were first posted on the Ministry's website in October 2001 (B.C. Ministry of Education 2001), and each subsequent set of FSA results has been posted the following fall. Beginning in 2003, schools were required to share individual students' exam results with parents before September 30<sup>th</sup> of each school year.

The Fraser Institute, an independent research and advocacy organization (Fraser Institute 2008), began issuing annual "report cards" on B.C.'s elementary schools in June 2003 (Cowley and Easton 2003). These include school scores constructed by the Fraser Institute from FSA exam results, and rankings based on these scores. From the outset, the Fraser Institute's school report cards have received widespread media coverage.

### **3.3.2. School Choice in B.C.**

In 2002, the government of British Columbia made school catchment boundaries permeable and gave B.C. parents and students the right to choose between schools. However, students in a local catchment area still have the first priority to enroll in their neighborhood school and cannot be displaced. This legislation was a departure from the previous neighborhood school policy that offered uniform education service to all students. Because students in the local catchment area still retain priority access to schools under the new policy, however, residential location choice remains an important component of school choice in British Columbia.

### **3.3.3. Data**

The student-level data used in this study are derived from two administrative files maintained by the B.C. Ministry of Education: an enrollment database and an FSA exam database. The two databases are linked by a unique student identifier. Records in the enrollment database are based on an annual enrollment form collected on September 30 of each year for all students in the public and private school system between 1999 and 2006. It includes personal characteristics including gender, aboriginal status, home language, English as a second language (ESL) status, special education status, and postal code.<sup>2</sup> I use the postal code information to augment the raw data with selected characteristics of each student's neighborhood as measured in 2001 and 2006 Canadian Census of Population at the Dissemination Area (DA) level.<sup>3</sup> These proxy for parental income, education, and demographic information not measured in the administrative data.

Records in the FSA exam database include the student's grade 4 and grade 7 reading and numeracy exam results in each year. All students who were registered in grade 4 or grade 7 in a British Columbia public or private school between the 1999/2000 and 2006/2007 school years are included in the database, whether or not they wrote the

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<sup>2</sup> A postal code is an area as small as one side of the street on a city block in urban locations.

<sup>3</sup> DA is the name given to a relatively stable area targeted to contain 400-700 people.

FSA exam. Each student has two indicators: whether or not the student was excused from writing the test, and whether or not the student actually wrote the test.

I exclude public and private schools with fewer than 5 students with valid reading and numeracy scores in any year between 1999 and 2006. Individual test scores are normalized to have a mean of zero and standard deviation of one in each year. Table 3.1 provides summary statistics for some variables of interest. There are 1067 grade 4 schools and 798 grade 7 schools in my sample. Among schools that offer grade 4 and meet my sample restriction, 87 percent are public and 13 percent are private. For grade 7, the numbers are 84 percent and 16 percent, respectively. Average enrolment among schools offering grade 4 is 41, and 50 for grade 7. The proportion of aboriginal students in my final sample is 8.5 percent in both grade 5 and grade 7. The proportion of students who report a language other than English as their home language is 22.4 percent in grade 7 and 21 percent in grade 4. Other socioeconomic characteristics obtained from the census such as neighborhood-level average family income, incidence of low income and education seem to be very similar between grade 4 and grade 7 students.

### **3.4. Volatility in School Mean Test Scores**

I begin with a descriptive analysis of variability in school-average test scores. Then I decompose the variation in school-average test scores to two different components: the variation that is due to sampling variation and the variation that is due to other nonpersistent factors.

Figures 3.1.1 and 3.1.2 portray the distribution of regression-adjusted average grade 4 and grade 7 reading and numeracy test scores by grade enrollment between

1999 and 2006.<sup>4</sup> It is immediately apparent that there is more variation in average test scores among small schools than big schools. The most likely cause is sampling variation, since its magnitude is a decreasing function of school size. We return to this hypothesis below. Although one might argue to the contrary that higher variability in mean test scores among small schools is due to long-term differences between small and large schools or unobserved heterogeneity, figures 3.2.1 and 3.2.2 suggest otherwise. Specifically, they show that small schools also experience more year-to-year fluctuation in their grade 4 and grade 7 average test scores compared to big schools, which rules out this hypothesis.

Tables 3.2.1 and 3.2.2 further illustrate transitory year-to-year variation in grade 4 and grade 7 average test scores. They are based on the idea that if mean test scores are strongly influenced by transitory factors, a ranking based on these scores will be similar to a ranking based on a pure lottery. The upper panel of each table uses FSA reading scores and the lower panel uses FSA numeracy scores to compare school rankings under different scenarios.

Column 1 illustrates the case where school-average test scores are completely stable over time. Under this scenario, 20 percent of schools will always appear in the top 20 percent of the distribution of school-average test scores, and 80 percent of schools will never appear in the top 20 percent.<sup>5</sup> In contrast, column 2 illustrates the case where schools are assigned to different percentiles based on a pure lottery: all schools have an independent 20 percent probability of appearing in the top 20 percent of the distribution of school-average test scores in each year. Under this scenario, we expect nearly 17 percent of schools to never appear in the top 20 percent, only 0.1

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<sup>4</sup> School-average test scores are adjusted by regressing individual test scores on a series of observable socioeconomic status variables (indicators for: sex, aboriginal status, ESL status, whether the student is French Immersion, special need status, 3 categories of home language (Chinese, Punjabi, English), neighbourhood-level average family income, incidence of low income, proportion of total immigrants, proportion of parents without high school degree, with high school degree and with bachelor degree or higher) and fixed school effects.

<sup>5</sup> It is clear that total stability of schools' performance will never happen under any useful school achievement measure, but it will allow me to lay out a framework with two extreme scenarios to explore the extent to which different test-based rankings resemble a lottery.

percent appear in the top 20 percent 6 times out of 8, and none to appear in the top 20 percent in all 8 years.

Column 3 ranks schools based on their actual school-average FSA scores. The data lie somewhere between the two extremes of complete stability and a lottery. Looking at grade 4 results, 46 percent of schools never appear in the top 20 percent of average FSA reading scores and 2.2 percent appear in the top 20 percent for all 8 years, these numbers are 39 percent and 6 percent for grade 7, respectively. The results are almost identical for numeracy scores. However, one should bear in mind that the ranking based on simple levels does not account for differences in socioeconomic status of students across schools. Controlling for students' observable characteristics, columns 4 results more closely resemble a lottery.<sup>6</sup> Columns 5 and 6 also control for students' observable characteristics, but restrict the sample to schools with enrolment less than 30 and 20 students, respectively. The results suggest that among smaller schools, the volatility in schools-average test scores is even more similar to a lottery. The most likely cause is sampling variation, whose magnitude decreases with sample size.

Finally, as column 8 illustrates, school gain scores (the change in school-average test score from one year to the next) are even more volatile than score levels, and consequently rankings based on gain scores are even more similar to a lottery.<sup>7</sup> This is potentially due to the fact that gain scores are based on differences in test scores over two consecutive years, which magnifies the effect of nonpersistent factors on variation in schools' test scores.

### **3.4.1. Sampling Variation**

If we think of successive cohorts of students entering a school as random draws from a local population feeding that school, then school-average test scores will vary

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<sup>6</sup> Adjusted levels are the vector of school-specific intercepts ( $\mathbf{b}$ ) in the regression

$Y_{ij} = \mathbf{b} + X'_{ij}\boldsymbol{\beta} + U_{ij}$  where  $X_{ij}$  is the vector of student characteristics explained in footnote 4.

<sup>7</sup> These results are in line with Kane and Staiger (2001) finding that gain scores exhibit more volatility due to transitory factors compared to average test scores (levels).

from year to year due to sampling variation. There are two factors that determine the magnitude of sampling variation: the number of students who write the test in the school, and the variance of individual test scores in the local population. Conditional on all other factors that could influence a school's average test score over time, smaller schools will experience more volatility in their mean test scores due to sampling variation than bigger schools.

I apply basic sampling theory to estimate the expected amount of variance in a school's average test score due to sampling variation. Consider a simple model of test score determination:

$$(1) \quad Y_{ijt} = \lambda_j + \delta_{jt} + \theta_i + U_{ijt}$$

Here,  $y_{ijt}$  denotes student  $i$ 's test score at school  $j$  in year  $t$ ,  $\lambda_j$  is the school-level permanent component of a student's score,  $\delta_{jt}$  is the school-level time-varying component (decomposed below into a persistent component and a transitory component),  $\theta_i$  is student-level permanent component (representing test-taking ability, socioeconomic characteristics, and other factors), and  $U_{ijt}$  is a student-level transitory shock.

Assumption 1: Transitory shocks are idiosyncratic:  $U_{ijt} \sim \text{iid}(0, \sigma_u^2)$ .

Assumption 2: Different cohorts of students entering a school in a given year are analogous to random draws from a local population feeding that school, so that  $\theta_i \sim \text{iid}(\mu_\theta, \sigma_\theta^2)$  for a local population.

Given equation (1), the average test score for a given school  $j$  in year  $t$  has the form:

$$(2) \quad \bar{Y}_{jt} = \sum_{ie|j} \frac{Y_{ijt}}{N_{jt}} = \lambda_j + \delta_{jt} + \sum_{ie|j} \frac{1}{N_{jt}} \theta_{it} + \sum_{ie|j} \frac{1}{N_{jt}} U_{ijt}.$$

Where  $N_{jt}$  is enrolment level at school  $j$  at time  $t$ . The cross-sectional variance in average test scores over all schools in a given year is:

$$(3) \quad \text{Var}(\bar{Y}_{jt}|t) = \text{Var}(\lambda_j) + \text{Var}(\delta_{jt}|t) + \text{Var}(\bar{\theta}_{i(t)}|t) + \text{Var}(\bar{U}_{ijt}|t)$$

$$= \sigma_\lambda^2 + \sigma_\delta^2 + [\sigma_\theta^2 + \sigma_U^2] E_j \left( \frac{1}{N_{jt}} \right).$$

Defining  $\varepsilon_{ijt} = \theta_i + U_{ijt}$ , I can re-write equation (1) as:

$$(4) \quad Y_{ijt} = \lambda_j + \delta_{jt} + \varepsilon_{ijt}.$$

An unbiased estimator of the within-school variance of individual test scores at a given school is:

$$(5) \quad \text{Var}(\widehat{y_{ijt}}|j, t) = S_{jt}^2 = \frac{1}{N_{jt}-1} \sum_{i=1}^{N_j} (y_{ijt} - \bar{y}_{jt})^2 = \frac{1}{N_{jt}-1} \sum_{i \in j} (\varepsilon_{ijt} - \bar{\varepsilon}_{jt})^2$$

$$= S_\varepsilon^2 = S_\theta^2 + S_U^2.$$

Therefore, the expected variance in school-average test scores due to sampling variation is:

$$(6) \quad \text{Var}(\widehat{\bar{y}_{jt}}|j, t) = \frac{S_{jt}^2}{N_{jt}} = \frac{1}{N_{jt}} (S_\theta^2 + S_U^2),$$

Averaging equation (6) over all schools gives the expected variance in mean test scores due to sampling variation for an average school:

$$(7) \quad \frac{\sum_{j=1}^J \widehat{\text{var}}(\bar{y}_{jt}|j, t)}{J} = [S_\theta^2 + S_U^2] \left[ \left( \sum_{j=1}^J \frac{1}{N_{jt}} \right) / J \right].$$

Note this is an unbiased estimator of the last component in equation (3). The average within-school variance of FSA reading and numeracy scores is 0.88 and 0.83, respectively, for both grade 4 and grade 7. Since the overall variance of individual FSA reading and numeracy scores is normalized to one, this implies that within the average

school, heterogeneity in students' test scores is nearly as large as in the overall population.<sup>8</sup> In other words, on average, the test scores of two students drawn randomly from a given school are likely to differ nearly as much as two students drawn from the population of B.C. students at large.

The estimated expected variance in mean FSA reading and numeracy scores for an average school due to sampling variation, from equation (7), is 0.028 (reading) and 0.025 (numeracy) for grade 4, and 0.026 (reading) and 0.024 (numeracy) for grade 7.<sup>9</sup> If we focus on schools of average size by looking only at the two middle quartiles of enrolment by grade, the overall cross-sectional variance of school-average FSA reading and numeracy scores is 0.13 and 0.17, respectively, for grade 4; and 0.13 and 0.19, respectively, for grade 7. It follows that for these average-sized schools, 21.5 and 14.7 percent of the total variation in 4<sup>th</sup> grade mean FSA reading and numeracy scores, respectively, is due to sampling variation. For grade 7, the figures are 20 and 12.6 percent, respectively. These estimates are similar in magnitude to those reported by Kane and Staiger (2002) for grade 4 students.

In order to gain a better understanding of the importance of sampling variation, I calculate the 95 percent confidence interval for an average school's mean test score using the estimated expected variance due to sampling variation:

$$CI_{95}^{Grade4\_Reading} = \bar{Y}_{Re}^{G4} \pm 1.96(\sqrt{E_j [Var(\bar{Y}_j)]}) = [-0.35, 0.34]$$

$$CI_{95}^{Grade7\_Reading} = \bar{Y}_{Re}^{G7} \pm 1.96(\sqrt{E_j [Var(\bar{Y}_j)]}) = [-0.30, 0.32]$$

Where  $\bar{Y}_{Re}$  is the overall mean of school-average FSA reading scores. The confidence interval extends from roughly the 17<sup>th</sup> to 84<sup>th</sup> percentile of the distribution of

<sup>8</sup> Here we are averaging over all years between 1999 and 2006. A similar result holds in each of those years.

<sup>9</sup> As it is also pointed out by Staiger and Kane (2002), with any peer effects, the effect of sampling variation will be amplified and these calculations will underestimate sampling variation.



school-average FSA reading scores for grade 4, and from the 19<sup>th</sup> to 80<sup>th</sup> percentile for grade 7. This implies that for an average grade 4 school in our sample, we cannot rule out with 95 percent probability that its average score the following year is as large as the 84<sup>th</sup> percentile, or as small as the 17<sup>th</sup> percentile, due to variability induced by sampling variation alone.

A more conservative measure is based on the 50 percent confidence interval for an average school's mean test score given sampling variation, which measures the degree of variability induced by sampling variation with the probability of a coin toss. This confidence interval extends from the 36<sup>th</sup> to 63<sup>rd</sup> percentile of the distribution of school-average reading scores for both grade 4 and grade 7. This remains a very wide interval.

### **3.4.2. Other Transitory Factors**

Sampling variation is only one of the transitory factors that can affect school-average test scores. There are other transitory shocks that generate nonpersistent changes in schools' mean test scores in addition to sampling variation. Specifically, the school-level time-varying component of student test scores (i.e.,  $\delta_{jt}$  in equation 1) will also induce nonpersistent variation in school-average test scores. Real-world examples include the existence of a disruptive student in a class, a dog barking in the playground or construction noise on the day of the exam, a school-wide illness, or special chemistry between a teacher and a class of students, etc.

Following Kane and Staiger (2002) and given the framework developed in section 2.4.1, I apply an indirect method to estimate the nonpersistent variation in test scores attributed to these other transitory factors. First, I estimate the total variation in mean test scores due to all transitory factors by measuring the degree of persistence in change in test scores between two consecutive years. Then I back out the portion due to sampling variation. The remainder is component attributable to other transitory factors.

I first decompose the school-level time-varying effect on student scores in equation (1) into two components:

$$(8) \quad \delta_{jt} = v_{jt} + \tau_{jt}$$

where  $v_{jt}$  is the persistent component which is assumed to pick up from where it left off last year in addition to a new innovation each year ( $v_{jt} = v_{jt-1} + \rho_{jt}$ ), and  $\tau_{jt}$  is the transitory component.

**Assumption 3:**  $\rho_{jt} \sim iid(0, \sigma_\rho^2)$  and  $\tau_{jt} \sim iid(0, \sigma_\tau^2)$

The average test score for a given school  $j$  in year  $t$  will therefore have the form:

$$(9) \quad \bar{y}_{jt} = \lambda_j + v_{jt} + \tau_{jt} + \bar{\theta}_{i(t)} + \bar{U}_{ijt}$$

$$(10) \quad \Delta \bar{y}_{jt} \equiv \bar{y}_{jt} - \bar{y}_{jt-1} = \rho_{jt} + \tau_{jt} - \tau_{jt-1} + \bar{\theta}_{i(t)} - \bar{\theta}_{i(t-1)} + \bar{U}_{ijt} - \bar{U}_{ijt-1}$$

The correlation between test score gains this year and last year can be written as:

$$(11) \quad Corr(\Delta \bar{y}_{jt}, \Delta \bar{y}_{jt-1}) = \frac{Cov(\Delta \bar{y}_{jt}, \Delta \bar{y}_{jt-1})}{\sqrt{Var(\Delta \bar{y}_{jt})} * \sqrt{Var(\Delta \bar{y}_{jt-1})}} = \frac{-\{E_j(\sigma_\tau^2) + [\sigma_\theta^2 + \sigma_u^2]E_j[\frac{1}{N_{jt}}]\}}{Var(\Delta \bar{y}_{jt})}$$

The numerator is the negative of the total variance of all transitory factors and the denominator is the total variance of gain scores ( $\Delta \bar{y}_{jt}$ ). Since I can calculate the left hand side of equation (11) directly, as well as  $Var(\Delta \bar{y}_{jt})$ , I can recover the total variance of all transitory factors from their product. Subtracting from this our earlier estimate of the magnitude of sampling variation (from equation 7), I can back out the variance of all other transitory factors.

Tables 3.3.1 and 3.3.2 summarize the results for different quartiles of grade 4 and grade 7 enrolment for both FSA reading and numeracy scores. The analysis is done separately for different years, while the bottom panel of each table presents the results of the variance decomposition for all years. As expected, the estimated sampling variance is bigger for small schools than bigger schools and the magnitudes are stable over time. The estimated variance of other transitory factors however varies over time, which is due to the random nature of the events that generate them. Overall, the results

suggest that school-average FSA reading and numeracy scores are not very reliable measures of persistent or permanent differences in school-average achievement, particularly among small schools. Looking at the bottom panel of each table, nearly 47 percent of the variance of school-average grade 4 FSA reading scores and 40 percent of FSA numeracy scores among schools in the smallest quartile of enrollment size is due to sampling variation and other nonpersistent factors. For grade 7 the estimates are 38 percent and 34 percent respectively. As expected, transitory factors account for a smaller share of the cross-sectional variance among larger schools. For the two middle quartiles, 33 percent and 29 percent of the cross-sectional variance in grade 4 and grade 7 average FSA reading scores is due to nonpersistent factors respectively. The corresponding numbers are 30 percent and 23 percent for numeracy scores. For schools in the largest quartile, 23 percent of the variance across schools in grade 4 and grade 7 average FSA reading scores is due to transient factors, while for numeracy scores these numbers are 21 percent and 17 percent for grade 4 and grade 7 respectively. It also worth mentioning that almost across the board, the amount of imprecision in average FSA numeracy scores due to nonpersistent factors is smaller than average FSA reading scores.

### **3.5. Conclusion**

I find that sampling variation and one-time mean reverting shocks are a significant source of observed variation in schools' average test scores. This is of critical importance because there is growing evidence that suggests providing information about school-level achievement has real effects on parents' school choice decisions. Since these decisions are inherently costly, if they are shaped by imprecise or noisy measures of school performance, they could potentially impose a net cost on parents and make them worse off. Moreover, if it becomes apparent to parents that these measures are very noisy and fluctuate significantly from one year to the next, they might stop paying attention to new information about school-level achievement, undermining the effectiveness of school choice policies that hinge upon ability to distinguish high-achieving schools from low-achieving schools.

Nonpersistent factors induce greater year-to-year variation in average test scores of small schools than bigger schools. This suggests that families should treat significant changes in average test scores of big schools as a stronger signal about changes in long-term performance compared to small schools.

These results also warn educational authorities against naïve policies or interventions that attach monetary/nonmonetary rewards or sanctions to schools based on noisy measures of school performance. As a growing literature attests, designing meaningful measures of school effectiveness continues to be a challenge (Hægeland et al. 2004; Mizala, Romaguera and Urquiola 2007).<sup>10</sup> As Chay et al. (2005) suggest, it is also critical to bear in mind that policy evaluations based on such noisy measures of school effectiveness have the potential to be misleading.

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<sup>10</sup> Kane and Staiger (2001) propose a filtered estimation to generate a more reliable measure of school achievement over time by exploiting the time-series dimension of them.

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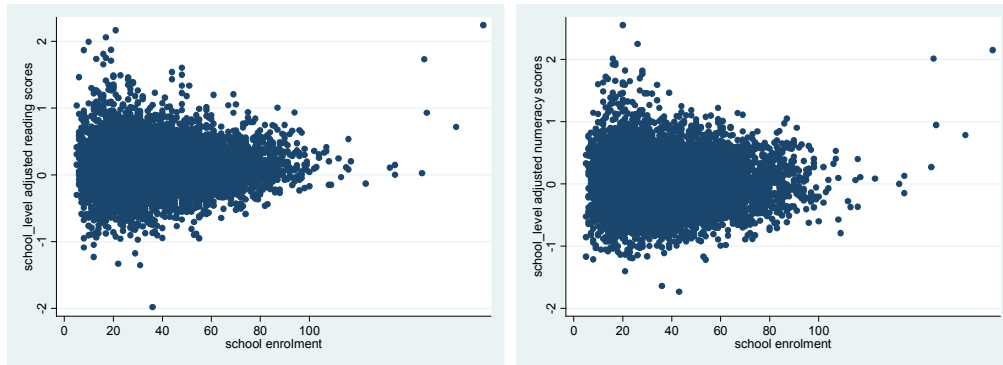
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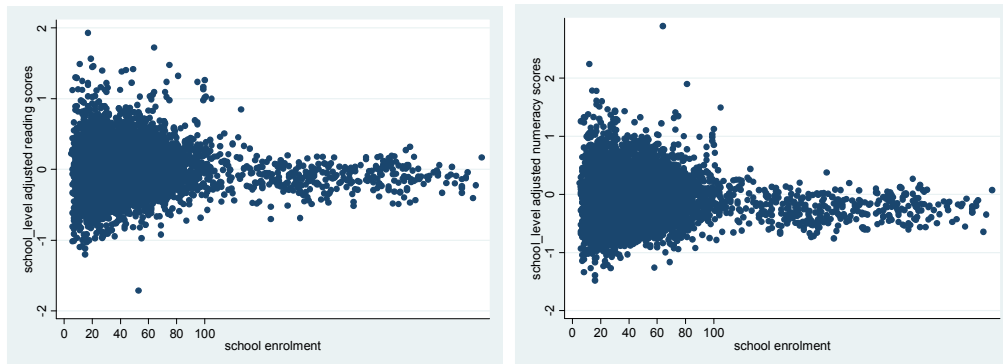
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### 3.7. Tables and Figures

**Figure 3.1.1. Grade 4 Adjusted Reading and Numeracy Average Test Scores by Enrolment Level (1999-2006)**

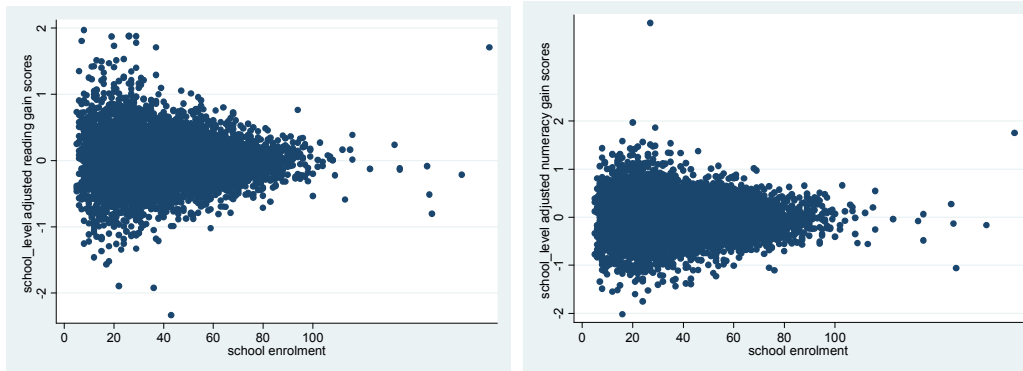


**Figure 3.1.2 Grade 7 Adjusted Reading and Numeracy Average Test Scores by Enrolment Level (1999-2006)**

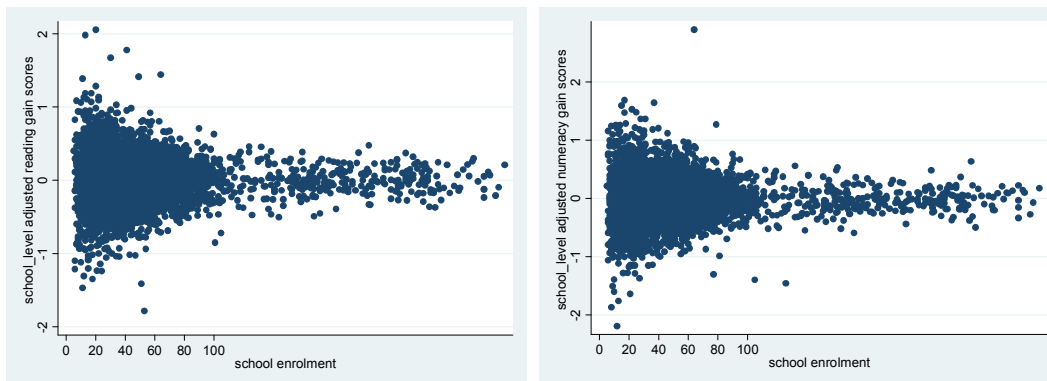




**Figure 3.2.1** *Grade 4 Adjusted Reading and Numeracy Gains by Enrolment Level (1999-2006)*



**Figure 3.2.2** *Grade 7 Adjusted Reading and Numeracy Gains by Enrolment Level (1999-2006)*



**Table 3.1. Sample Characteristics. Grade 4 Schools with valid FSA test scores between 1999-2006**

Variable	Grade 4 Sample percent	Grade 7 Sample percent
Number of schools in each year	1067	798
% Public Schools	87%	84%
% Private Schools	13%	16%
Average enrolment	41	50
School-level average proportion of students:		
excused from reading test	4.4%	4.1%
excused from numeracy test	4.3%	4.2%
excused from both	3.9%	3.6%
Not excused and test written but no reading score	3.0%	2.3%
Not excused and test written but no numeracy score	2.6%	2.9%
% of aboriginal students	8.5%	8.5%
% of special need students	6.6%	8.0%
% of gifted students	1.4%	2.4%
% of students in French Immersion programs	5.5%	6.1%
% of students reporting non-English home language	21.0%	22.4%
% Chinese home language	6.7%	8.2%
% Punjabi home language	4.5%	3.6%
% other home language	9.7%	10.6%
% English as a second language (ESL)	15.0%	7.0%
Average Family Income (in 2000 C\$)	C\$66034	C\$67015
Average percentage of Incidence of low income	15.1%	15.2 %
Average proportion of parents with education:		
Without high school	14.0%	14.0%
With high school	14.0%	14.3 %
With bachelor or higher	12.6 %	13.2 %

**Table 3.2.1. Proportion Ranking in the Top 20% on 4<sup>th</sup> Grade Test Scores 1999-2006**

# of years in top 20	Certainty	Lottery	Actual average scores	Actual Adjusted average scores			Lottery	Gain Scores
				All schools	Enrol. < 30 (N=328)	Enrol. < 20 (N=116)		
	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)
<b>School Ranking Based on Average Reading Scores</b>								
Never	80.0	16.7	45.8	37.6	27.1	24.1	20.9	16.4
1 year	0.0	33.5	19.1	22.6	23.4	20.6	36.7	40.9
2 years	0.0	29.3	9.5	15.7	21.0	21.5	27.5	30.9
3 years	0.0	14.6	7.9	9.4	11.2	14.6	11.4	9.9
4 years	0.0	2.6	5.6	4.5	5.1	5.1	2.8	1.7
5 years	0.0	0.9	3.8	4.0	4.8	7.7	0.4	0.0
6 years	0.0	0.1	2.8	3.0	4.5	5.1	0.0	0.0
7 years	0.0	0.0	3.0	1.6	1.8	0.0	0.0	0.0
8 years	20.0	0.0	2.2	1.0	0.6	0.8	NA	NA
<b>School Ranking Based on Average Numeracy Scores</b>								
Never	80.0	16.7	44.3	38.8	30.4	25.0	20.9	16.6
1 year	0.0	33.5	19.9	23.1	22.5	22.4	36.7	40.5
2 years	0.0	29.3	10.5	13.6	17.3	19.8	27.5	31.3
3 years	0.0	14.6	8.3	9.1	13.4	13.7	11.4	9.1
4 years	0.0	2.6	4.8	5.0	4.8	6.9	2.8	2.2
5 years	0.0	0.9	4.4	4.1	3.9	6.9	0.4	0.0
6 years	0.0	0.1	2.7	2.6	3.6	2.5	0.0	0.0
7 years	0.0	0.0	2.5	1.9	2.7	1.7	0.0	0.0
8 years	20.0	0.0	2.2	1.4	0.9	0.8	NA	NA

**Table 3.2.2. Proportion Ranking in the Top 20% on 7<sup>th</sup> Grade Test Scores 1999-2006**

# of years in top 20	Certainty	Lottery	Actual average scores	Actual Adjusted average scores			Lottery	Gain Scores
				All schools	Enrol. < 30 (N=241)	Enrol. < 20 (N=86)		
	(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)
<b>School Ranking Based on Average Reading Scores</b>								
Never	80.0	16.7	38.85	33.21	23.24	20.93	20.9	7.27
1 year	0.0	33.5	17.17	18.30	19.5	22.09	36.7	27.69
2 years	0.0	29.3	11.78	14.16	16.18	16.28	27.5	40.10
3 years	0.0	14.6	7.52	9.90	15.35	20.93	11.4	20.93
4 years	0.0	2.6	4.64	7.02	6.64	1.16	2.8	3.88
5 years	0.0	0.9	4.64	5.51	5.39	6.98	0.4	0.13
6 years	0.0	0.1	5.26	5.14	5.81	3.49	0.0	0.0
7 years	0.0	0.0	4.26	3.38	2.49	3.49	0.0	0.0
8 years	20.0	0.0	5.89	3.38	5.39	4.65	NA	NA
<b>School Ranking Based on Average Numeracy Scores</b>								
Never	80.0	16.7	38.22	32.46	21.58	19.77	20.9	7.52
1 year	0.0	33.5	15.66	18.92	22.41	20.93	36.7	26.82
2 years	0.0	29.3	11.9	13.53	16.60	18.60	27.5	40.98
3 years	0.0	14.6	8.65	10.28	10.79	16.28	11.4	20.80
4 years	0.0	2.6	7.02	8.02	13.28	9.30	2.8	3.76
5 years	0.0	0.9	4.76	6.02	5.39	6.98	0.4	0.13
6 years	0.0	0.1	4.39	4.26	2.07	1.16	0.0	0.0
7 years	0.0	0.0	5.26	3.13	2.90	2.33	0.0	0.0
8 years	20.0	0.0	4.14	3.38	4.98	4.65	NA	NA

**Table 3.3.1. Decomposition of Variance in Schools' Mean FSA Scores (Grade 4)**

School enrolment quartile	Average size	Total variance	Sampling variance	Other non-persistent variance	Total proportion non-persistent	Total variance	Sampling variance	Other non-persistent variance	Total proportion non-persistent
<b>Grade 4 FSA Reading Scores</b>									
Year = 2000									
Bottom quartile	21	0.156	0.051	0.042	0.600	0.175	0.045	0.054	0.571
2 Middle quartiles	41	0.100	0.022	0.020	0.435	0.126	0.022	0.026	0.380
Top quartile	66	0.081	0.013	0.014	0.343	0.105	0.013	0.010	0.225
Year = 2001									
Bottom quartile	20	0.202	0.049	0.036	0.424	0.267	0.045	0.048	0.349
2 Middle quartiles	40	0.151	0.022	0.026	0.326	0.187	0.021	0.037	0.317
Top quartile	68	0.109	0.013	0.012	0.234	0.137	0.012	0.014	0.197
Year = 2002									
Bottom quartile	20	0.221	0.049	0.033	0.374	0.276	0.043	0.043	0.313
2 Middle quartiles	39	0.137	0.023	0.020	0.318	0.166	0.022	0.026	0.295
Top quartile	65	0.104	0.014	0.004	0.182	0.129	0.013	0.004	0.140
Year = 2003									
Bottom quartile	20	0.178	0.051	0.037	0.499	0.234	0.042	0.051	0.402
2 Middle quartiles	40	0.131	0.023	0.020	0.333	0.167	0.022	0.021	0.261
Top quartile	67	0.115	0.013	0.016	0.259	0.156	0.013	0.017	0.199
Year = 2004									
Bottom quartile	19	0.226	0.052	0.069	0.540	0.336	0.043	0.123	0.495
2 Middle quartiles	39	0.144	0.023	0.024	0.332	0.209	0.021	0.035	0.271
Top quartile	67	0.115	0.013	0.008	0.191	0.146	0.013	0.021	0.239
Year = 2005									
Bottom quartile	19	0.235	0.052	0.051	0.440	0.244	0.043	0.040	0.345
2 Middle quartiles	39	0.140	0.023	0.025	0.344	0.175	0.022	0.030	0.300
Top quartile	66	0.099	0.013	0.005	0.193	0.133	0.013	0.019	0.246
All Years (2000-2005)									
Bottom quartile	20	0.203	0.050	0.046	0.475	0.253	0.044	0.058	0.406
2 Middle quartiles	40	0.132	0.023	0.022	0.339	0.171	0.021	0.029	0.299
Top quartile	66	0.104	0.013	0.010	0.230	0.134	0.013	0.015	0.213

**Table 3.3.2. Decomposition of Variance in Schools' Mean FSA Scores (Grade 7)**

School enrolment quartile	Average size	Total variance	Sampling variance	Other non-persistent variance	Total proportion non-persistent	Total variance	Sampling variance	Other non-persistent variance	Total proportion non-persistent
					Grade 7 FSA Reading Scores				
					Year = 2000				
Bottom quartile	20	0.142	0.050	0.010	0.418	0.183	0.047	0.027	0.401
2 Middle quartiles	42	0.109	0.022	0.028	0.456	0.130	0.021	0.013	0.267
Top quartile	97	0.064	0.010	0.014	0.371	0.108	0.011	0.009	0.184
					Year = 2001				
Bottom quartile	20	0.182	0.051	0.016	0.368	0.252	0.042	0.042	0.335
2 Middle quartiles	42	0.125	0.022	0.003	0.206	0.186	0.022	0.021	0.232
Top quartile	97	0.119	0.011	0.012	0.194	0.179	0.011	0.014	0.141
					Year = 2002				
Bottom quartile	20	0.188	0.048	0.004	0.276	0.250	0.042	0.032	0.295
2 Middle quartiles	44	0.137	0.021	0.015	0.268	0.189	0.021	0.030	0.266
Top quartile	98	0.114	0.011	0.010	0.179	0.170	0.011	0.006	0.098
					Year = 2003				
Bottom quartile	20	0.235	0.047	0.053	0.425	0.270	0.044	0.054	0.363
2 Middle quartiles	43	0.150	0.022	0.011	0.219	0.198	0.020	0.021	0.206
Top quartile	99	0.116	0.011	0.016	0.232	0.214	0.010	0.035	0.212
					Year = 2004				
Bottom quartile	20	0.270	0.048	0.058	0.393	0.327	0.043	0.048	0.280
2 Middle quartiles	43	0.141	0.021	0.021	0.298	0.218	0.020	0.029	0.225
Top quartile	99	0.119	0.011	0.015	0.217	0.194	0.010	0.025	0.182
					Year = 2005				
Bottom quartile	19	0.232	0.052	0.047	0.427	0.278	0.048	0.065	0.405
2 Middle quartiles	43	0.144	0.022	0.023	0.309	0.214	0.020	0.018	0.177
Top quartile	98	0.104	0.011	0.014	0.246	0.169	0.011	0.013	0.142
					All Years (2000-2005)				
Bottom quartile	20	0.210	0.050	0.031	0.385	0.262	0.045	0.044	0.341
2 Middle quartiles	42	0.135	0.022	0.017	0.289	0.190	0.021	0.022	0.226
Top quartile	97	0.105	0.011	0.014	0.232	0.169	0.011	0.018	0.167